

Introduction to Elementary Particles (TN2811) Theory Lecture 7

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Today's lecture

More on the **weak interaction**

The **Higgs boson** and symmetry breaking

Collider phenomenology and **Statistics** for particle physics

The Wboson continued

Taking into account these properties, some of the physically allowed reactions involving **quarks** and **W bosons** will be:

$$\begin{split} & u + W^- \to d \,, \quad u + W^- \to s \,, \quad d + W^+ \to u \,, \quad s + W^+ \to u \,, \\ & \bar{u} + W^+ \to \bar{d} \,, \quad \bar{u} + W^+ \to \bar{s} \,, \quad \bar{d} + W^- \to \bar{u} \,, \quad \bar{s} + W^- \to \bar{u} \,, \\ & W^+ \to u + \bar{d} \,, \quad W^+ \to u + \bar{s} \,, \quad W^- \to d + \bar{u} \,, \quad W^- \to s + \bar{u} \,, \end{split}$$

Electric charge is always conserved

You can always replace a given quark by the corresponding quark of a different generation: for example a down antiquark by a strange antiquark

If a given reaction is allowed, the corresponding reaction involving the antiparticles is also physically allowed

$$\bar{u} + W^+ \to \bar{s} \quad \Rightarrow \quad u + W^- \to s$$

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Taking into account these properties, some of the physically allowed reactions involving **leptons** and **W bosons** will be:

$$e^+ + W^- \to \bar{\nu}_e , \quad e^- + W^+ \to \nu_e , \quad \nu_e + W^+ \to e^- , \quad \bar{\nu}_e + W^+ \to e^+$$

 $W^+ \to e^+ + \nu_e , \quad W^- \to e^- + \bar{\nu}_e , \quad e^+ + \nu_e \to W^+ , \quad e^- + \bar{\nu}_e \to W^-$

Electric charge is always conserved

- Each interaction vertex involves a charged and a neutral lepton that belong to the same lepton generation
- You can always **replace** the two leptons of a given generation for the corresponding two leptons of **another generation**

The individual leptonic quantum numbers are always conserved in weak reactions



Draw the Feynman diagram for the following process

$$\pi^+ \to \mu^+ + \nu_\mu \qquad \pi^+ = \left(u \, \bar{d} \right)$$



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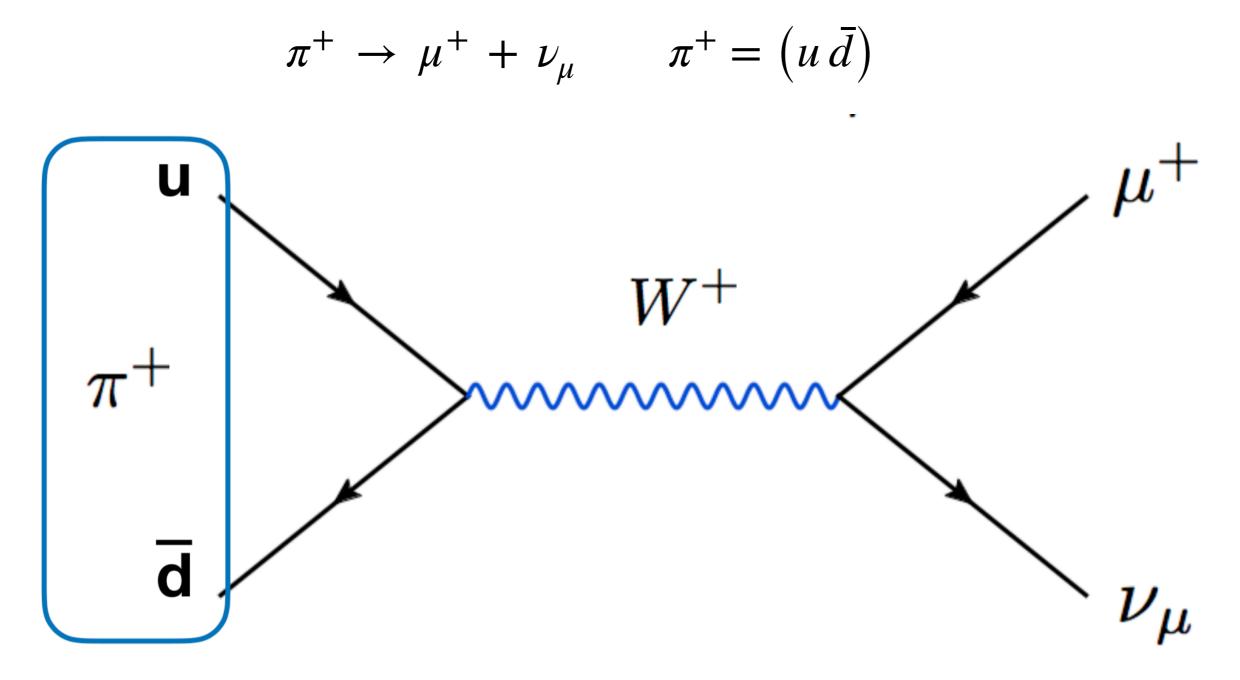
We have a neutrino in the final state: the weak interaction must be involved

Quarks and leptons only interact indirectly via either photons or W, Z bosons

Since the electric charge is *Q***=+-1**, then a positively charged *W* **boson** is involved

We know what vertices are allowed involving quarks or leptons and a W boson





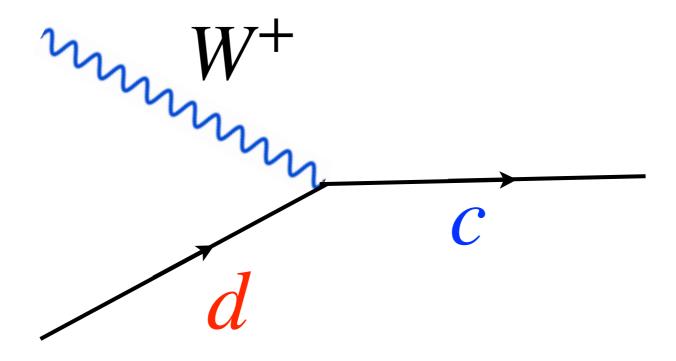
You can check that all relevant quantum numbers are conserved: L, B, Q, ...

exercise

We have seen that in processes mediated by the weak gauge boson *W* the **flavour** of the quarks will **change**

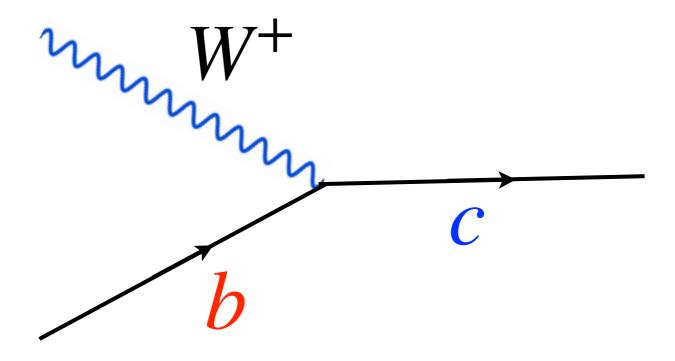
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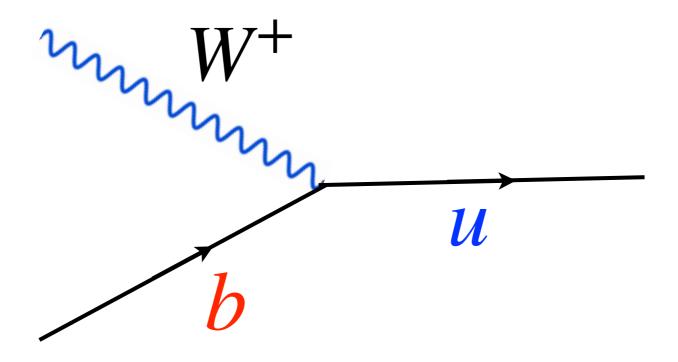
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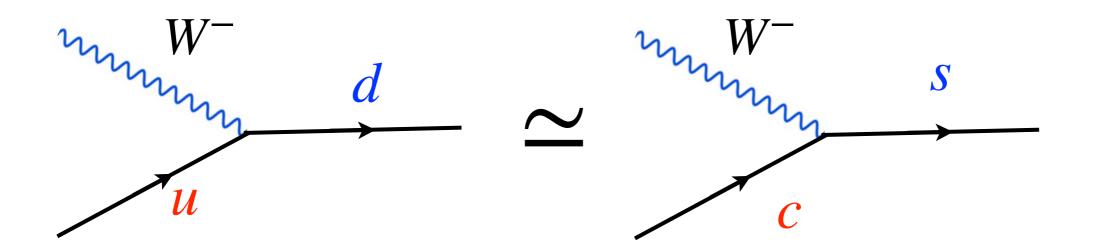
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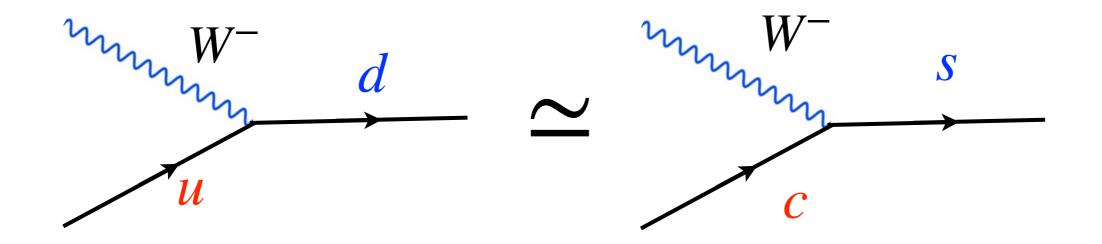
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The weak interactions mediates transitions between quarks of different generations

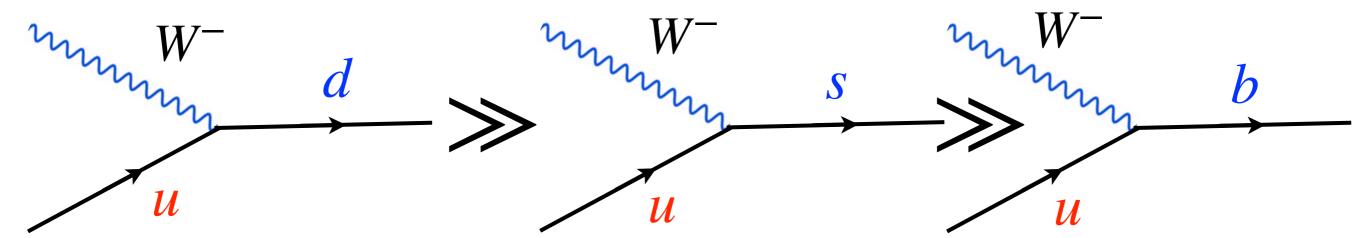
The strength of the weak coupling is similar between quarks of the same generation



The strength of the weak coupling is similar between quarks of the same generation



The strength of the weak coupling is smaller between quarks of different generation



Weak coupling between gens 1 and 2 bigger than between gens 1 and 3

Drawing Feynman diagrams

✓ If the scattering reaction involves composite particles (hadrons) first of all determine their quark decomposition making sure all quantum numbers add up consistently

✓Then put at the left of the diagram the initial-state particles and at the right of the diagram the final-state particles

Attempt to connect the initial and final state particles among them. Note that some particles will not interact and will be just **spectators** in the reaction

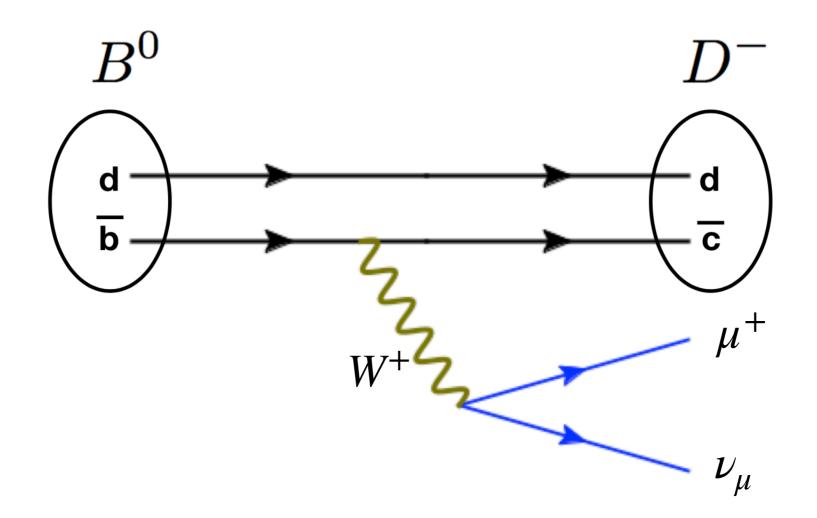
Make sure that all interaction vertices conserve the corresponding quantum **numbers:** for example, if gluons or photons are conserved, then *Q*, *B*, *S*, *C*, *b*, ... should be conserved

exercises This hierarchy of the weak couplings between quark generations is particularly important in order to understand the decays of hadrons that contain heavy quarks

$$B^0 \to D^- + \mu^+ + \nu_\mu \qquad B^0 = (d\,\bar{b}) \qquad D^- = (d\bar{c})$$

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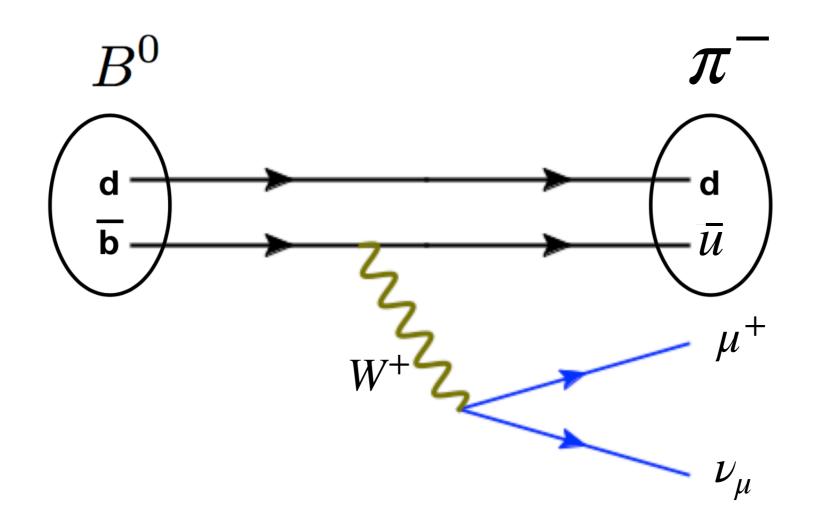


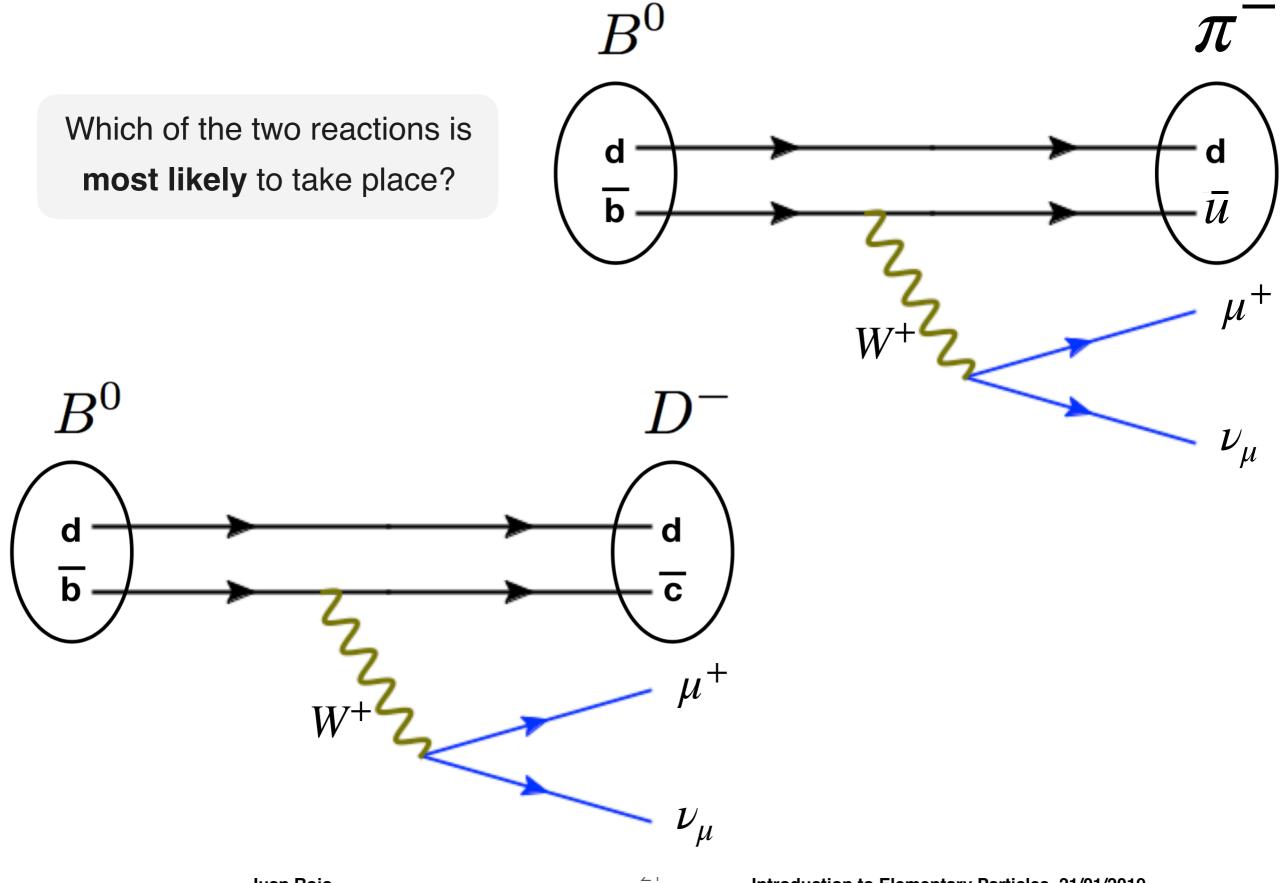
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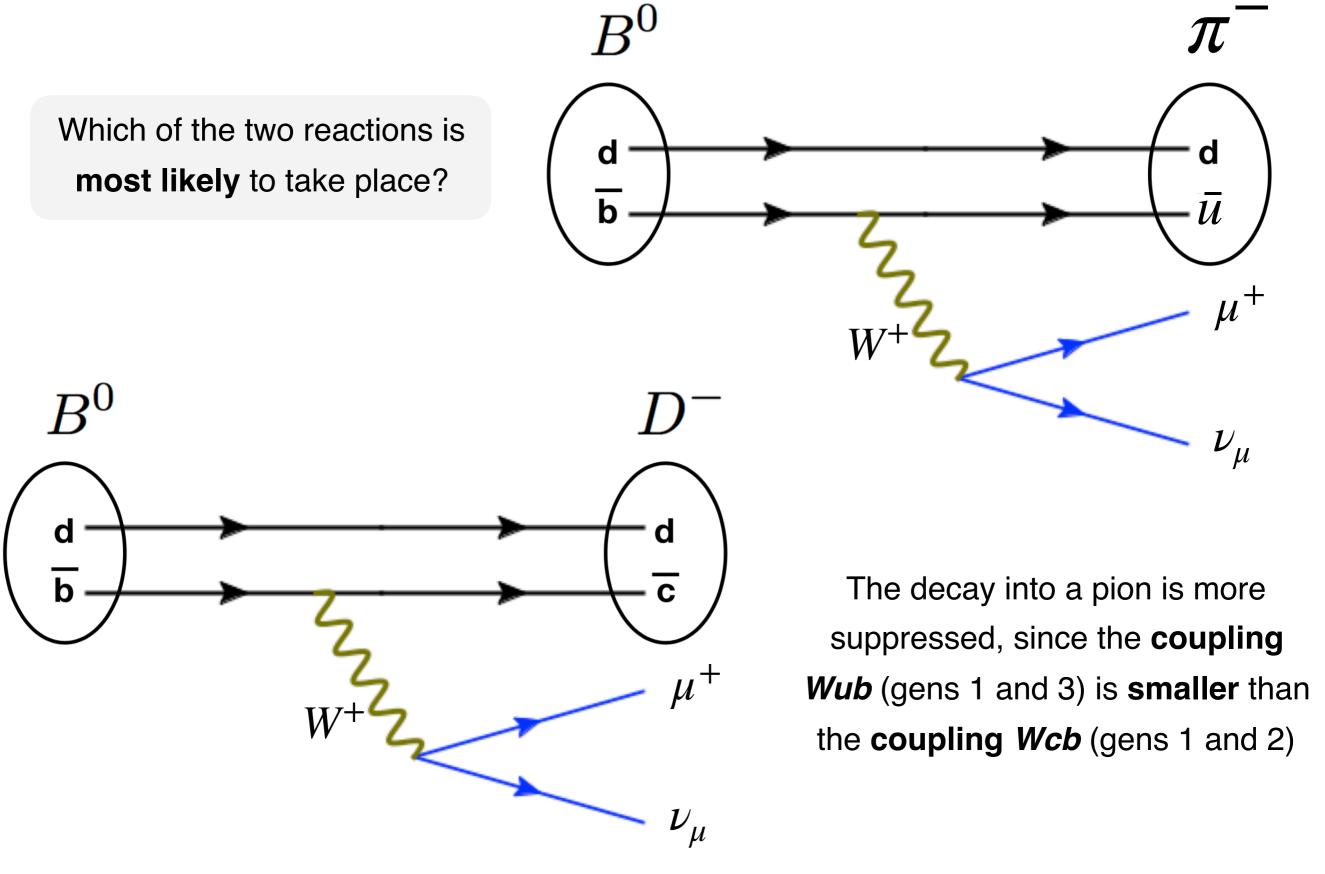
$$B^0 \to \pi^- + \mu^+ + \nu_\mu \qquad B^0 = (d\,\bar{b}) \qquad \pi^- = (d\bar{u})$$

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Note that some reaction processes might look very different from the outside, but their similarities become apparent at the Feynman diagram level

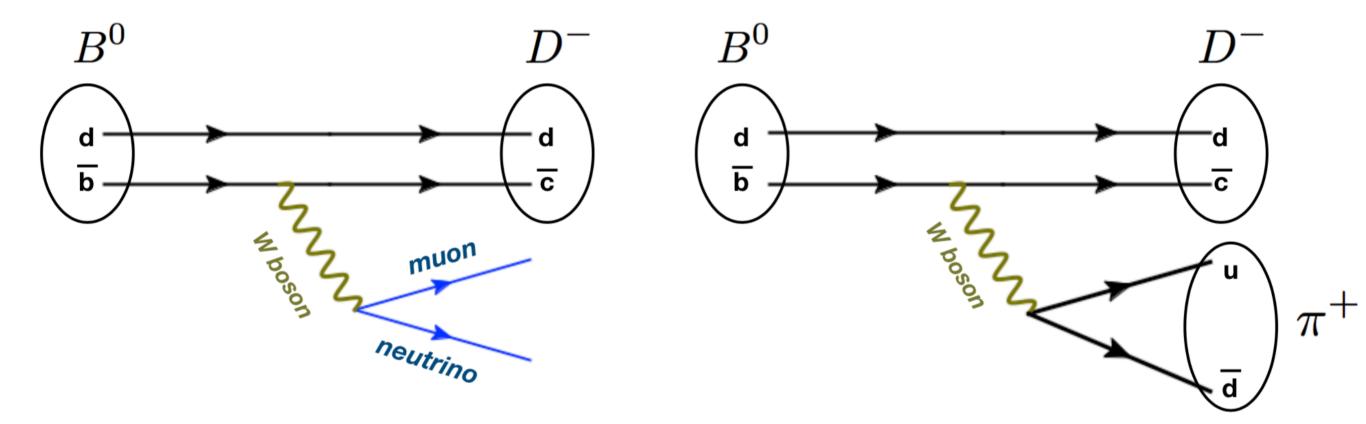
$$B^{0} \rightarrow D^{-} + \mu^{+} + \nu_{\mu}$$
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How do these two decay models relate to each other?

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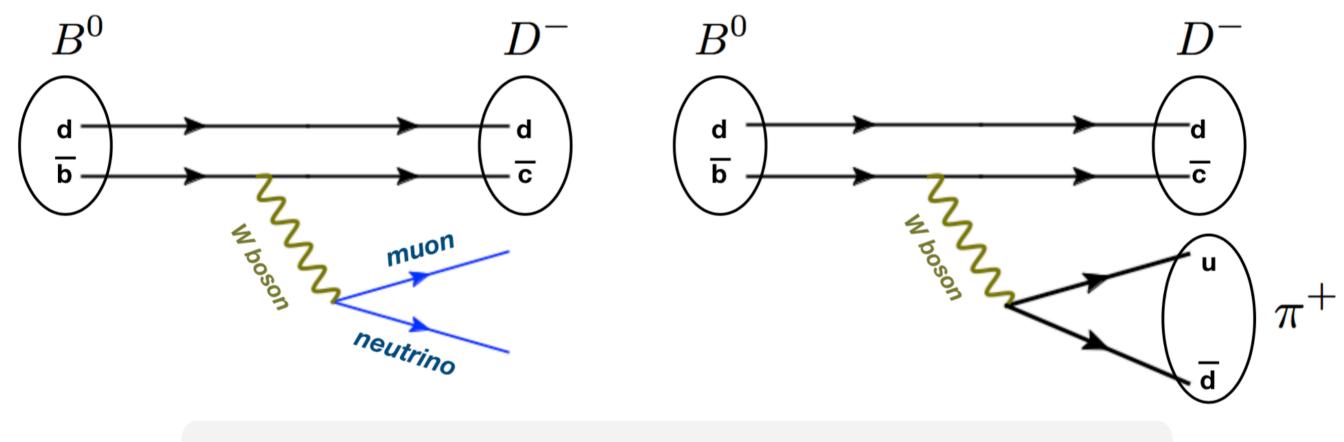
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$$B^0 \rightarrow D^- + \mu^+ + \nu_\mu$$
$$B^0 \rightarrow D^- + \pi^+$$

How do these two decay models relate to each other?



These two processes have a very **similar probability** to happen!

The weak interactions are mediated by three massive bosons: W+, W+, Z⁰

The main properties of the *Z* **bosons** are:

✓ As opposed to the massless gluons and photons, the Z boson is very massive, around 91 times the proton mass (similar to W boson)

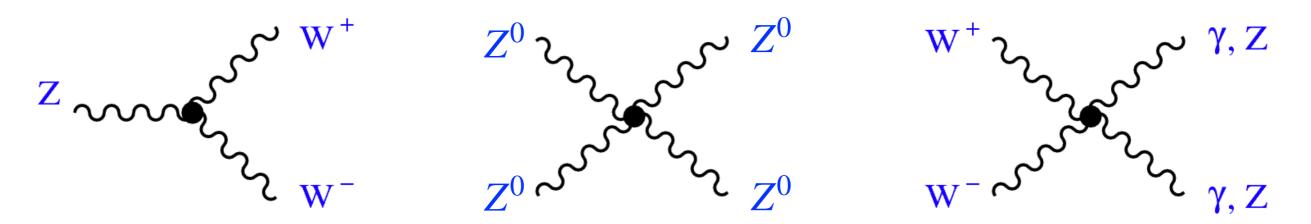
$$m_{\gamma} = 0$$

 $m_g = 0$
 $m_{W^{\pm}} = 80.385 \,\text{GeV}$
 $m_{Z^0} = 91.1876 \,\text{GeV}$

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- When interacting with quarks, the Z boson does not change the quark flavour
- In weak interaction processes mediated by the Z boson, the flavour quantum numbers (strangeness, charmness, botomness) are always conserved quantities

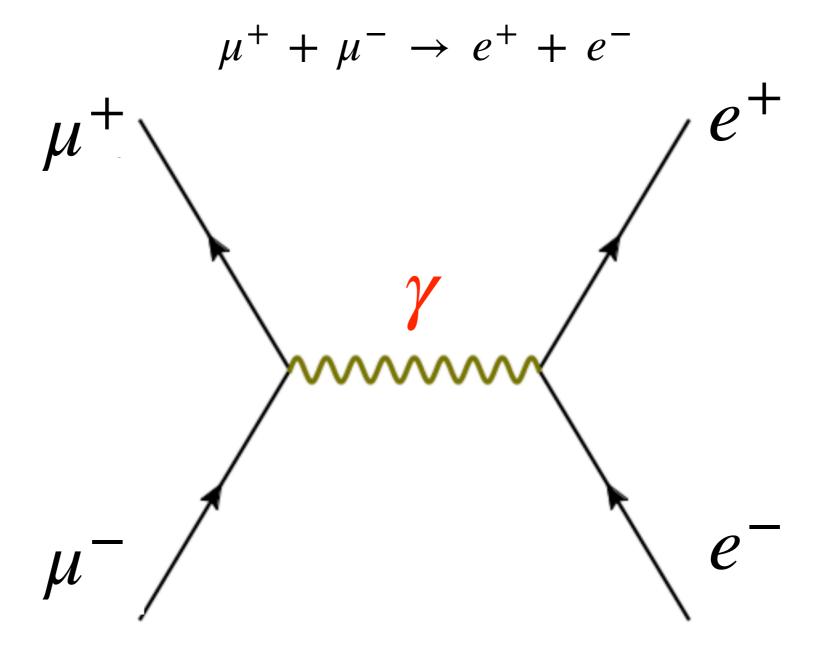
In terms of its interactions, the weak boson Z is a kind of ``*heavy photon*"

In diagrams involving quarks and charged leptons, and where the photon mediates the interaction, one can **replace the photon by a** *Z* **boson**

$$\mu^+ + \mu^- \rightarrow e^+ + e^-$$

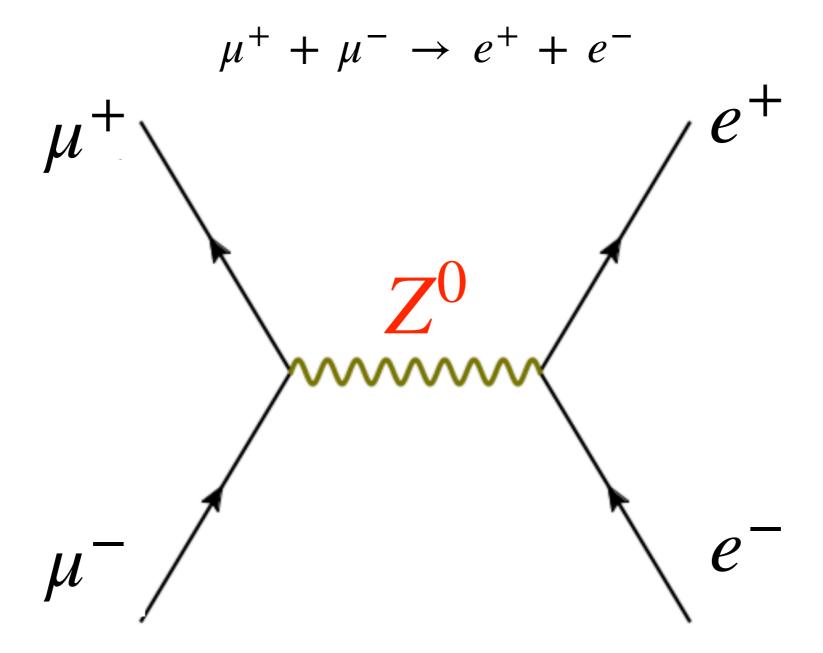
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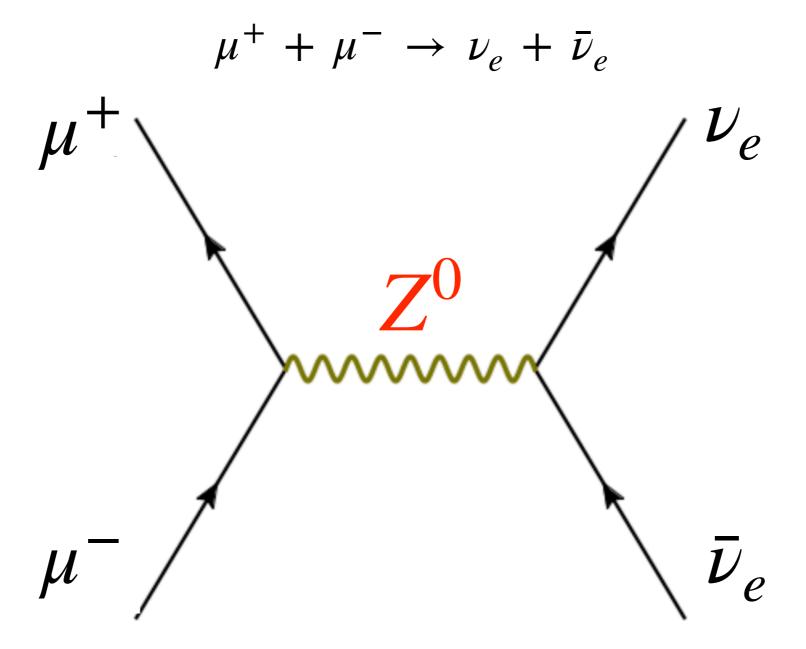
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In terms of its interactions, the weak boson Z is a kind of ``heavy photon"

The *Z* boson also mediates processes involving **neutrinos**



We can now summarise the weak interaction vertices involving the Z boson

with quarks

$$\begin{split} u &+ \bar{u} \to Z^0, \quad d + \bar{d} \to Z^0, \quad s + \bar{s} \to Z^0, \dots \\ u &+ Z^0 \to u, \quad d + Z^0 \to d, \quad s + Z^0 \to s, \dots \\ Z^0 \to u + \bar{u}, \quad Z^0 \to d + \bar{d}, \quad Z^0 \to s + \bar{s}, \dots \end{split}$$

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with leptons

$$\begin{split} e^{+} + e^{-} &\to Z^{0}, \quad \mu^{+} + \mu^{-} \to Z^{0}, \quad \nu_{e} + \bar{\nu}_{e} \to Z^{0}, \dots \\ e^{-} + Z^{0} \to e^{-}, \quad \nu_{e} + Z^{0} \to \nu_{e}, \quad \tau^{+} + Z^{0} \to \tau^{+}, \dots \\ Z^{0} \to e^{-} + e^{+}, \quad Z^{0} \to \tau^{+} + \tau^{-}, \quad Z^{0} \to \nu_{\mu} + \bar{\nu}_{\mu}, \dots \end{split}$$

Any allowed reaction when particles are interchanged by antiparticles is also allowed

Let us summarise what we have learned about the weak interactions

Flavour is **not necessarily conserved** by the weak interactions: strangeness, charmness, and bottomness can vary in reactions mediated by the **W bosons** (but not by the **Z** boson)

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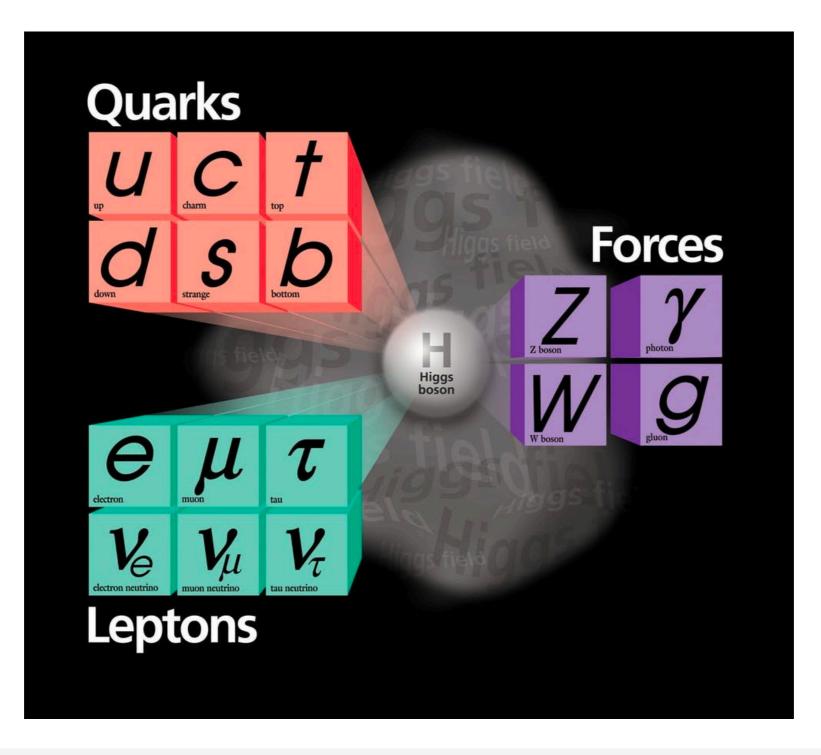
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From the point of view of the interactions with leptons and charged quarks, the Z boson behaves as it it was a heavy photon

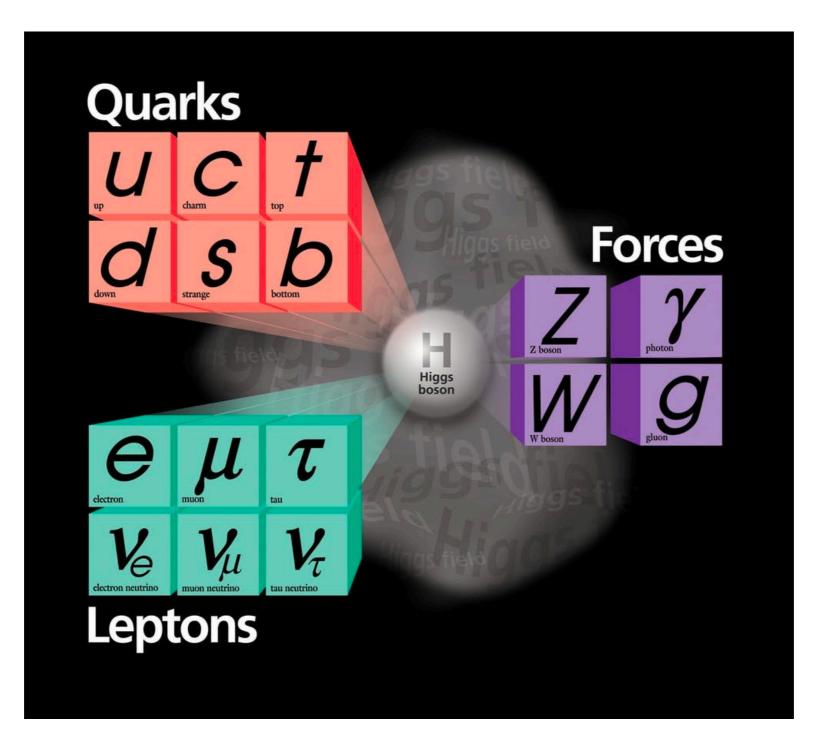
The Standard Model of particle physics



We are by know familiar with the different types of **matter particles** (leptons and quarks) and their interactions, mediated by the **force carrier particles**

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The Standard Model of particle physics



The only missing ingredient to complete the Standard Model is the Higgs boson



What are the defining properties of the Higgs boson?

It has spin zero: a scalar particle (hence the name boson)



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 \mathbf{V} It is also responsible for the mass of the \mathbf{W} and \mathbf{Z} bosons

Without the Higgs, elementary particles would be **massless** and the Universe as we know it would be **impossible**

M The symmetries of the weak interaction require that elementary particles are **massless**

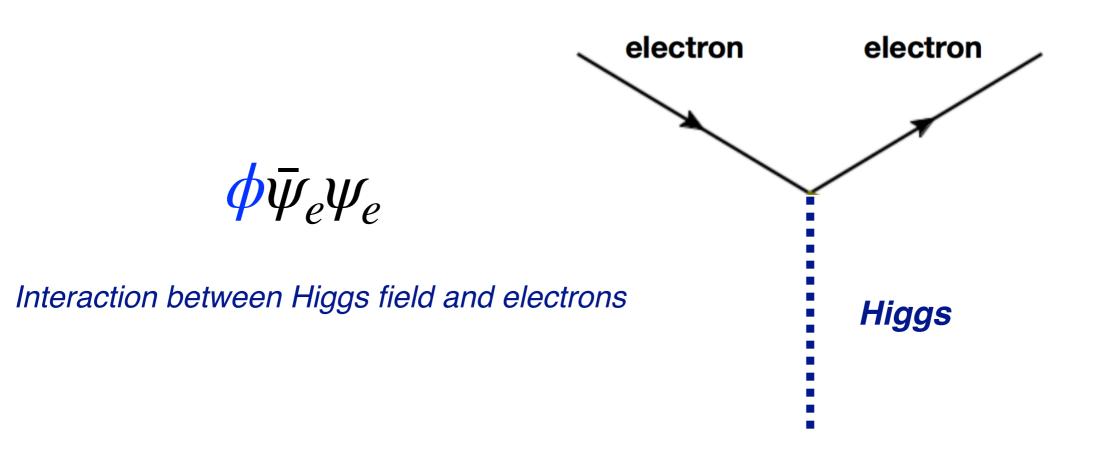
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We can use the important concept of **spontaneous symmetry breaking**

In Let us start with a theory of massless particles, and add an extra scalar field (without spin) that interacts with all other particles and has its own potential



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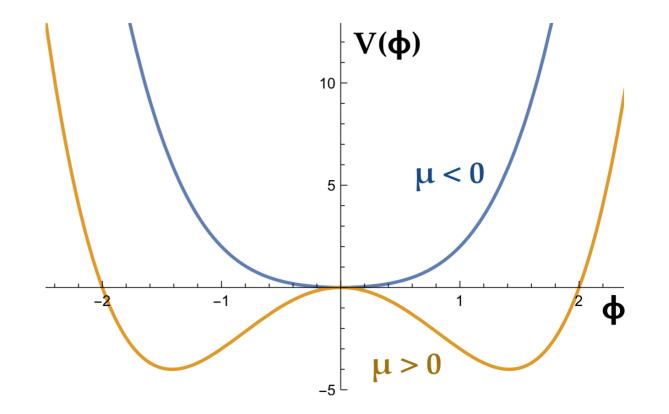
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 $V(\phi) = -\mu \phi^2 + \lambda \phi^4$

Interaction of Higgs field with itself



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What determines the ground state (state with minimum energy) for a system with potential energy given by $V(\phi)$?

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The ground state of the system corresponds to the minimum of the potential First let us consider the case for which $\mu < 0$ (we always have $\lambda > 0$)

$$\frac{d}{d\phi}V(\phi) = 0 = 2\left|\mu\right|\phi + 4\lambda\phi^3$$

Modular This equation can only be satisfied if $\phi=0$: the ground state of the theory is the one where the field vanishes (so there is no Higgs field)

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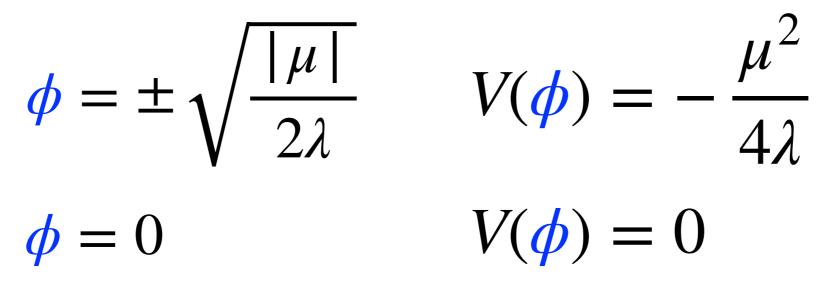
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$$\phi = \pm \sqrt{\frac{|\mu|}{2\lambda}}$$

Electroweak symmetry breaking $V(\phi) = - |\mu| \phi^2 + \lambda \phi^4$

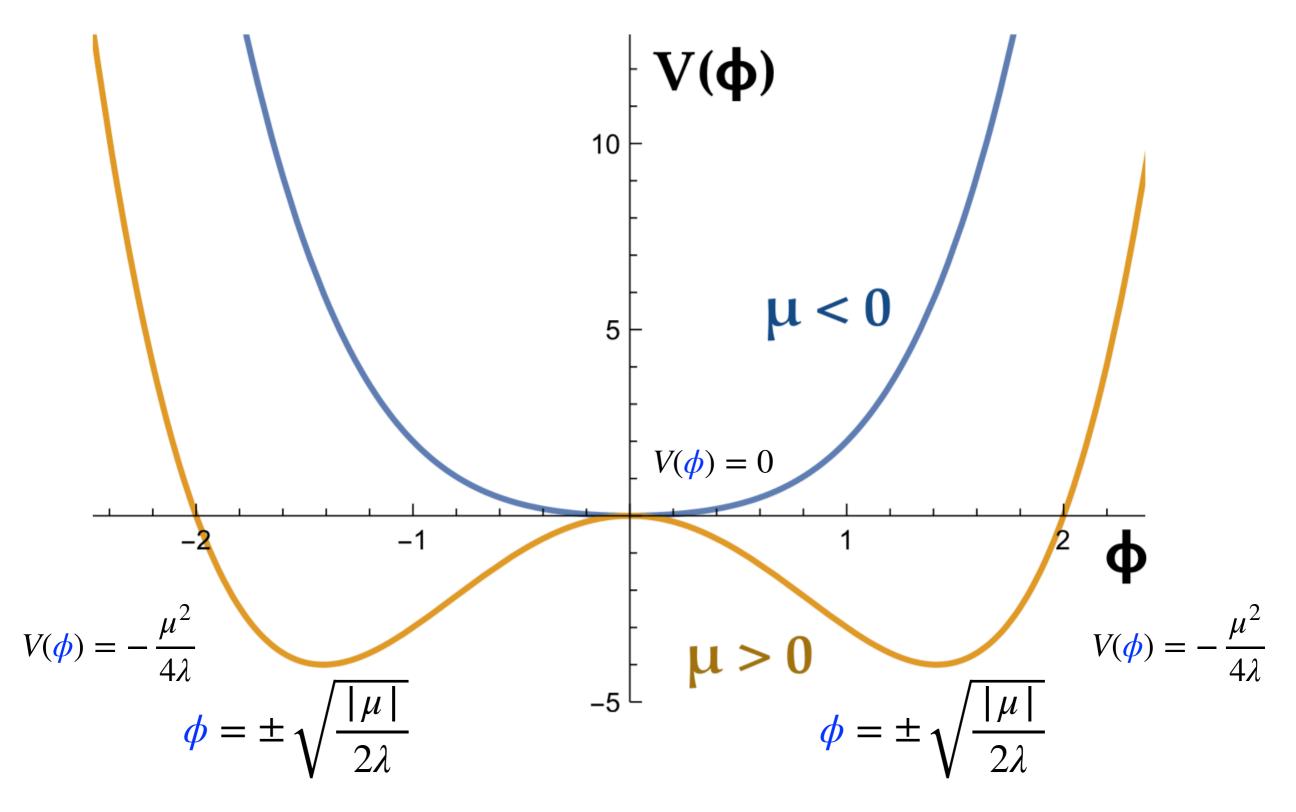
Which of these three solutions has the lowest potential energy?



The lowest energy configuration (ground state of the theory) is one where the **Higgs field is different from zero!**

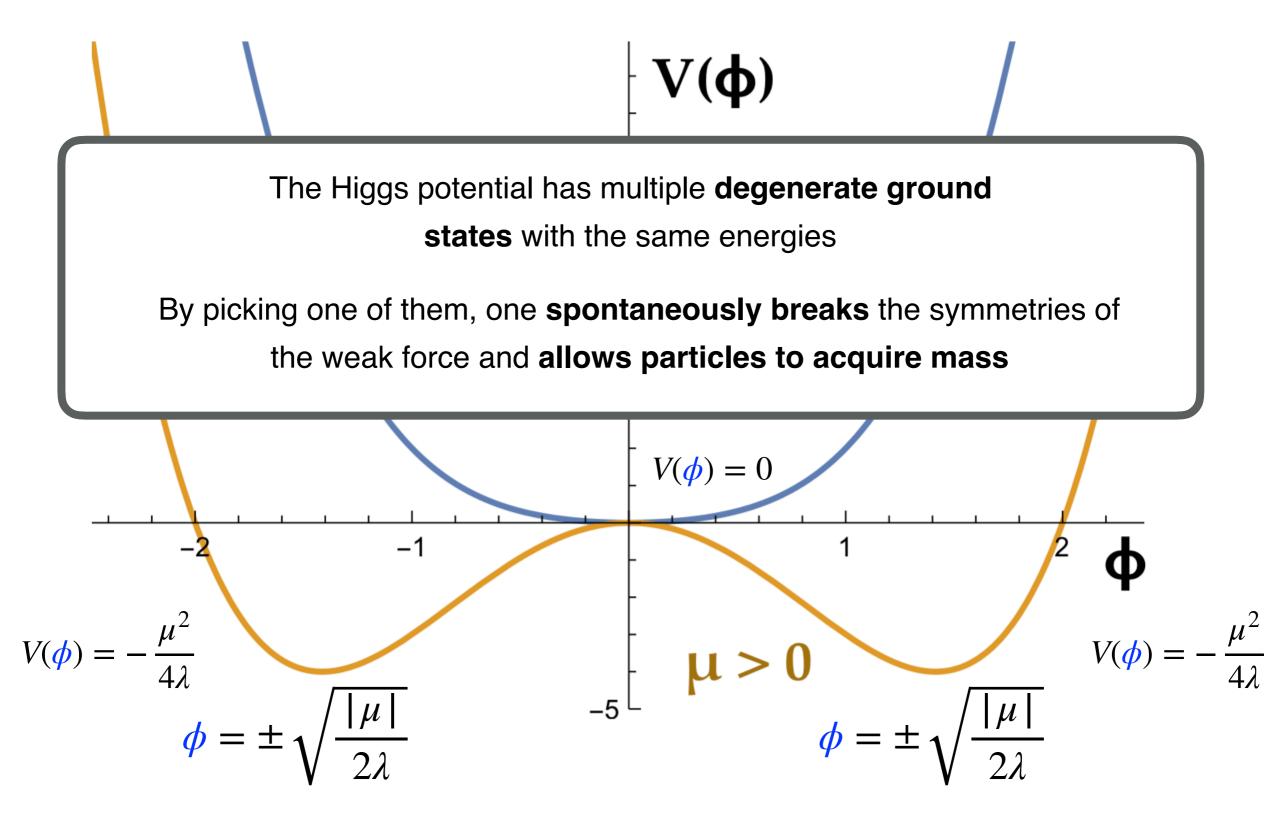
The Higgs field permeates all space and **elementary particles** acquire their mass by interacting with it

Higgs mechanism I



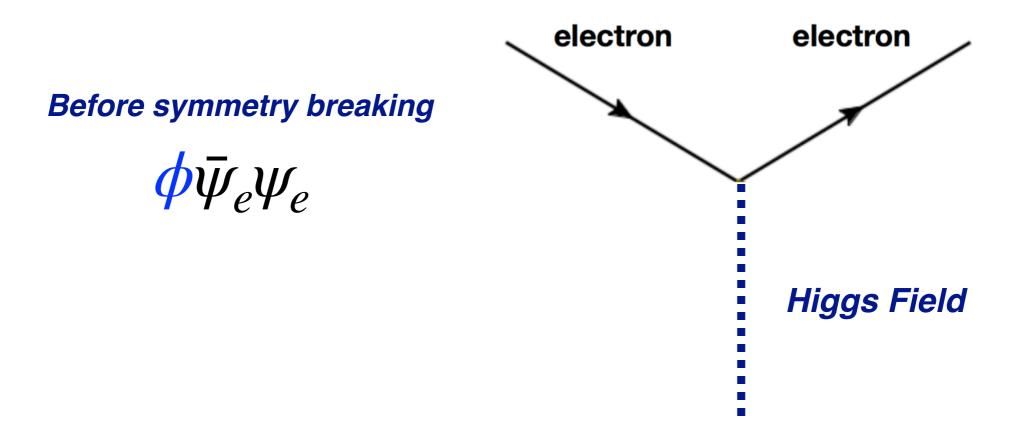
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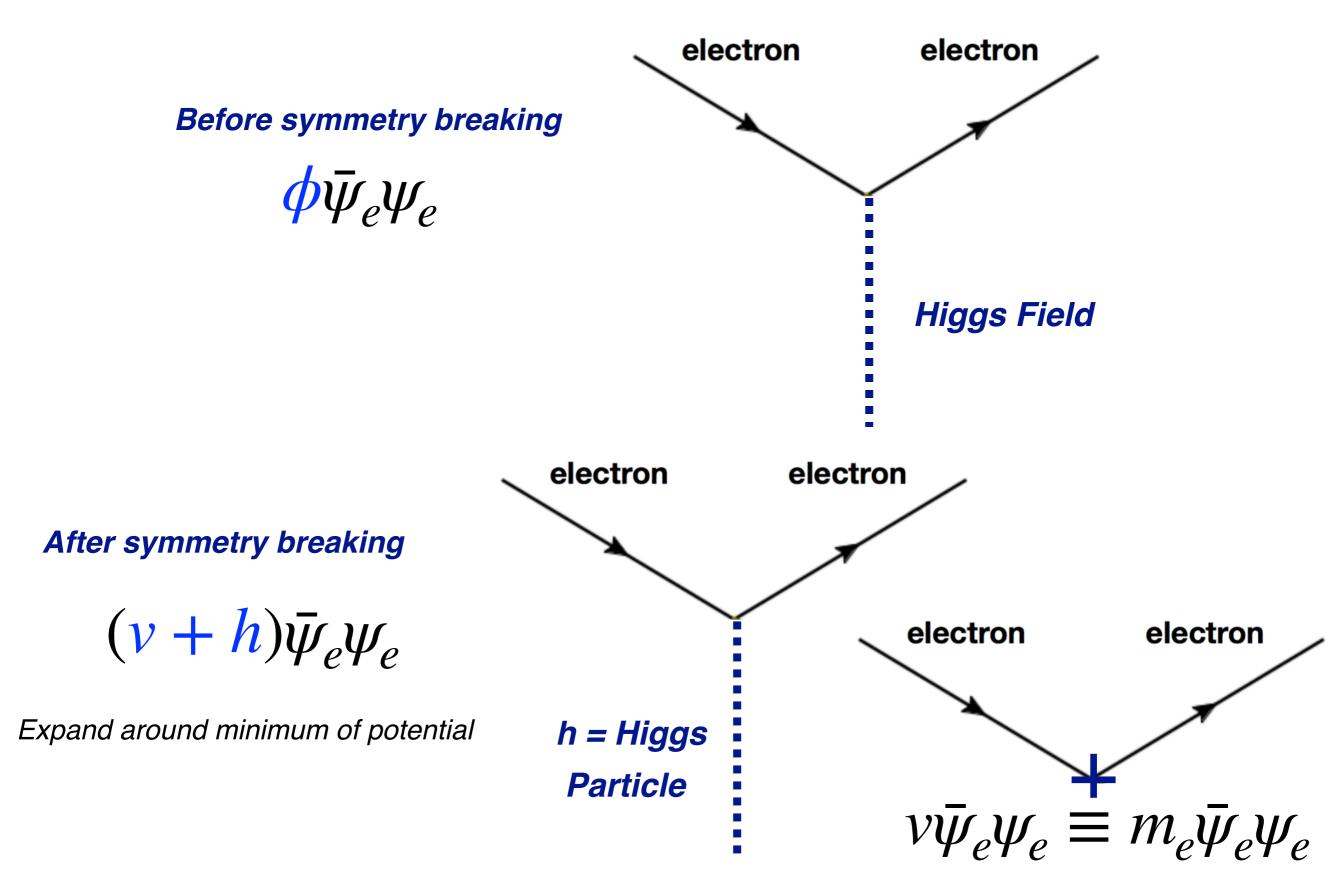


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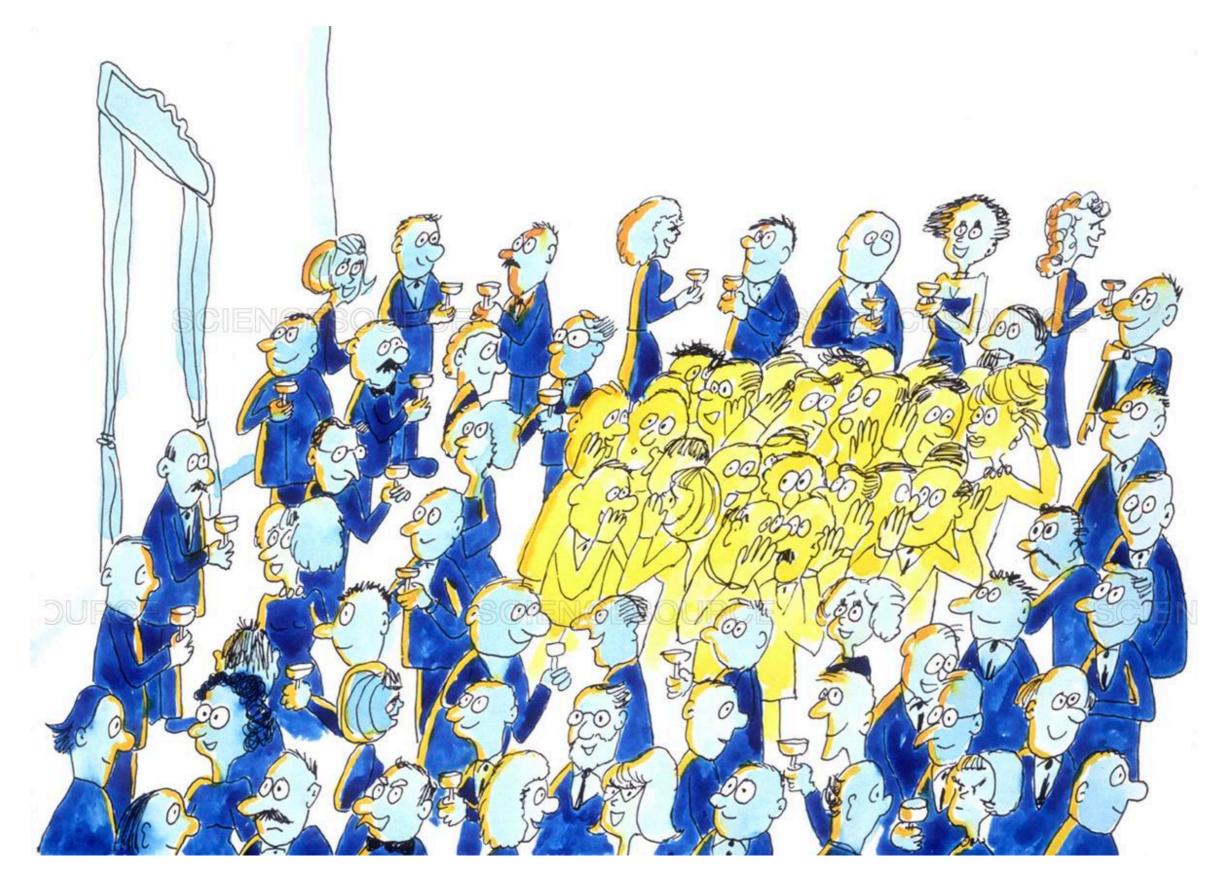
Higgs mechanism II



Higgs mechanism II



Higgs mechanism III



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Higgs boson recap I



Higgs boson recap II



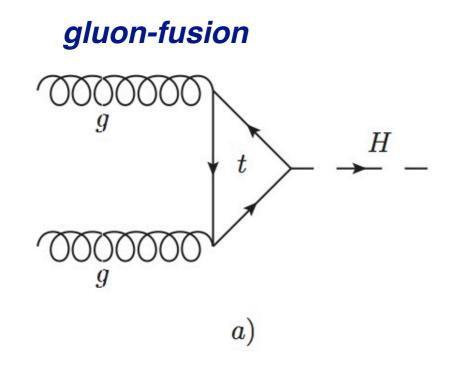
PhD Comics: https://www.youtube.com/watch?v=lqAWqwh3Etw

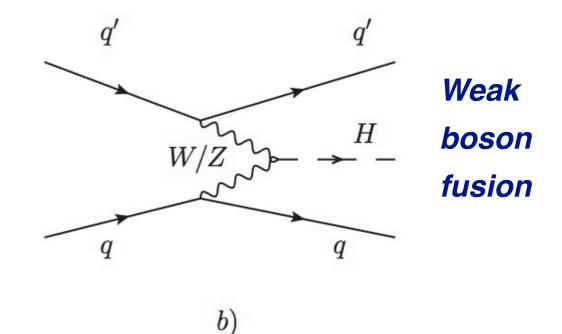
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Higgs production and collider phenomenology

At proton-proton colliders such as the LHC, multiple ways to produce Higgs bosons

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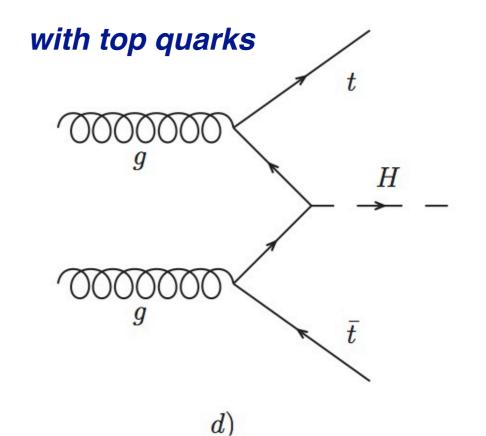




W/Z associated W/Z q W/Z^* H \bar{q} W/Z^* H

c)

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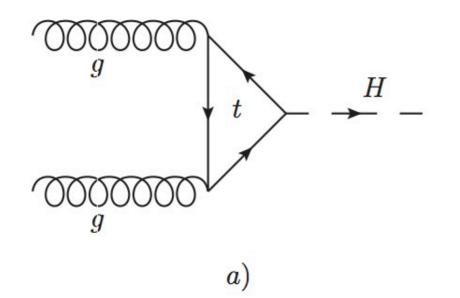


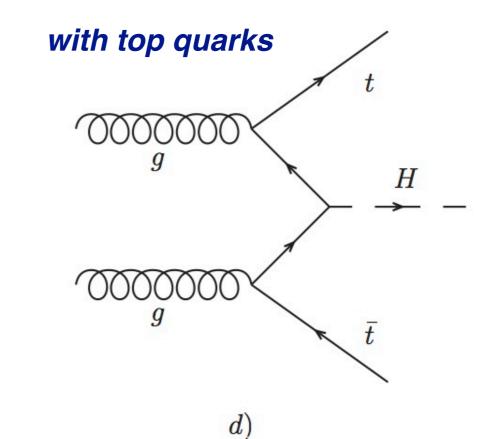
Which processes are **more likely** to happen? Strength of Higgs boson coupling

to a particle is **proportional to the particle mass**

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gluon-fusion



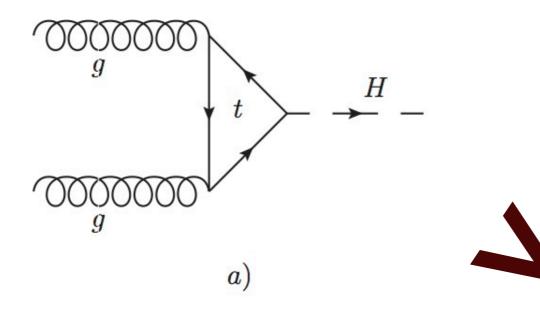


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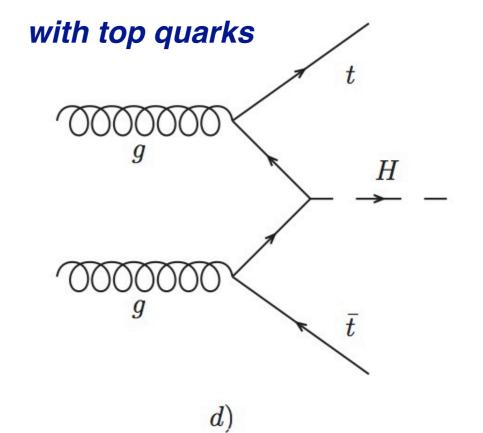
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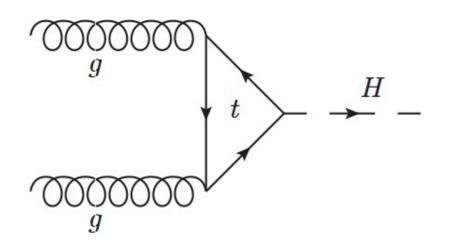
Same coupling between Higgs and top quarks ... But in one case one needs to produce **in addition a top quark pair** which requires a lot of extra energy

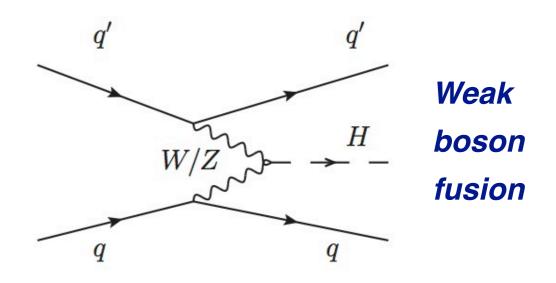


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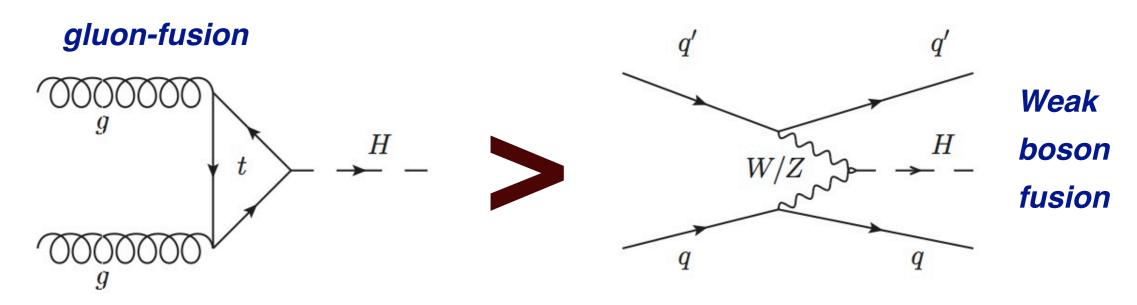
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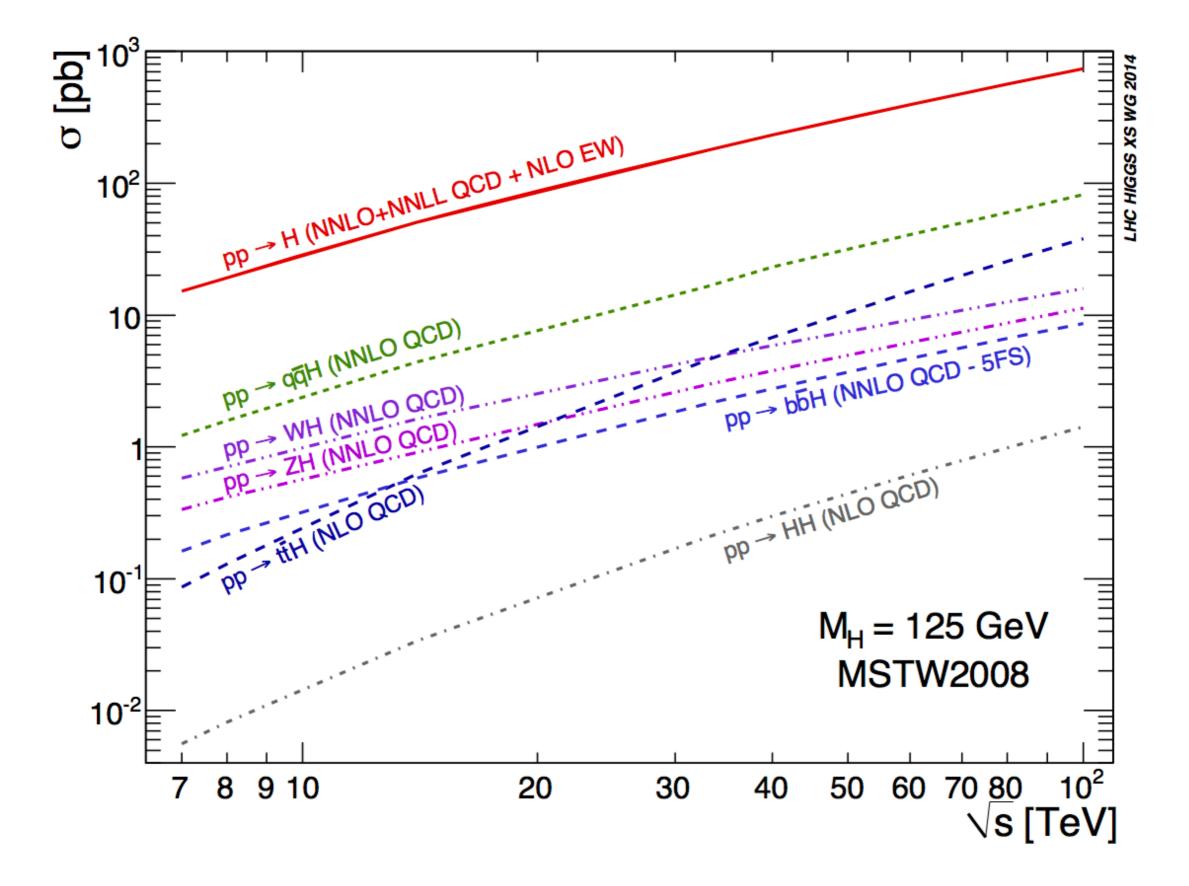




Which processes are **more likely** to happen? Strength of Higgs boson coupling to a particle is **proportional to the particle mass**



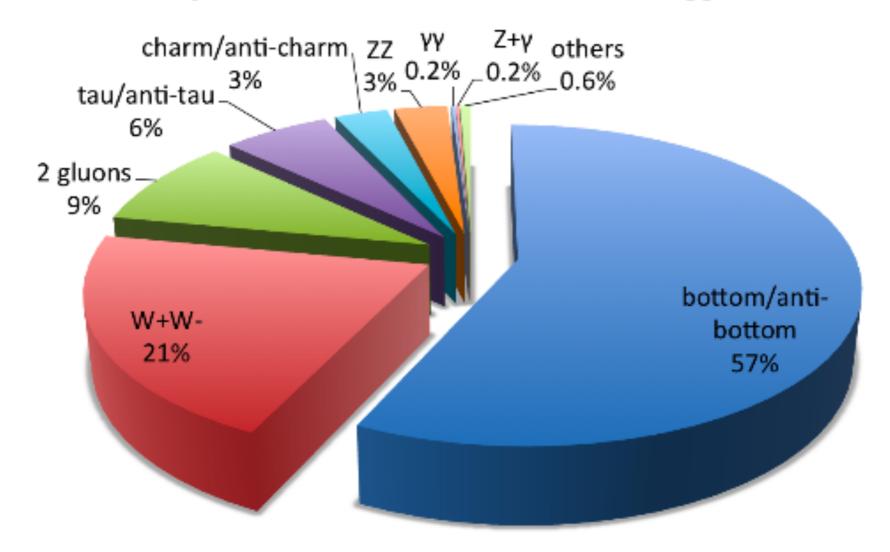
The **top quark mass**, 173 GeV, is **larger than the weak boson masses**, 80 GeV and 91 GeV, therefore the Higgs coupling to tops is larger and the gluon-fusion process is more likely to happen



Higgs boson decays

Once produced, the Higgs boson decays almost instantaneously

Decays of a 125 GeV Standard-Model Higgs boson



The define a **branching ratio BR** as the likelihood that a particle **decays to a given final state**, normalised to all possible final states

Higgs boson decays

Once produced, the Higgs boson decays almost instantaneously

$$BR(h \rightarrow b\bar{b}) = 0.57$$

$$BR(h \to W^+W^-) = 0.21$$

$$BR(h \to \tau^+ \tau^-) = 0.21$$

$$BR(h \rightarrow \gamma \gamma) = 0.003$$

$$BR(h \rightarrow ZZ) = 0.03$$

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$$BR(h \rightarrow b\bar{b}) = 0.57$$

$$BR(h \to W^+W^-) = 0.21$$

$$BR(h \to \tau^+ \tau^-) = 0.21$$

$$BR(h \rightarrow \gamma \gamma) = 0.003$$

$$BR(h \to ZZ) = 0.03$$

The Higgs tends to decay more into particles to which **it couples more strongly** (so with higher mass), but there is also a suppression factor if the decay products **have similar or bigger mass** than the Higgs

From cross-sections to event rates

The **interaction cross-section σ** measures how likely a given scattering reaction is to take place. It is a kind of **effective collision area** and the units are cm⁻²

The number of Higgs bosons produced at the LHC will be

$$N_h = \mathscr{L}_{\text{int}} \times \sigma(pp \to h + X) \times BR(h \to Y)$$

where the **integrated luminosity** measures how many protons are available for scattering in a given period of time

For elementary particles, the **barn** is a more suitable unit for cross-sections

$$1 b = 10^{-24} cm^2$$

 $1 pb = 10^{-36} cm^2$ (picobarn)
 $1 fb = 10^{-39} cm^2$ (femtobarn)

Counting Higgs bosons

exercise Up to 2018, the LHC has accumulated *L* = 150 fb of luminosity

> Compute the number of Higgs bosons produced in *i*) gluon fusion and *ii*) associated production with a W, and in each case in the *i*) *diphoton* and *ii*) *bottom-antibottom* final states