

Introduction to Elementary Particles (TN2811)

Theory Lecture 6

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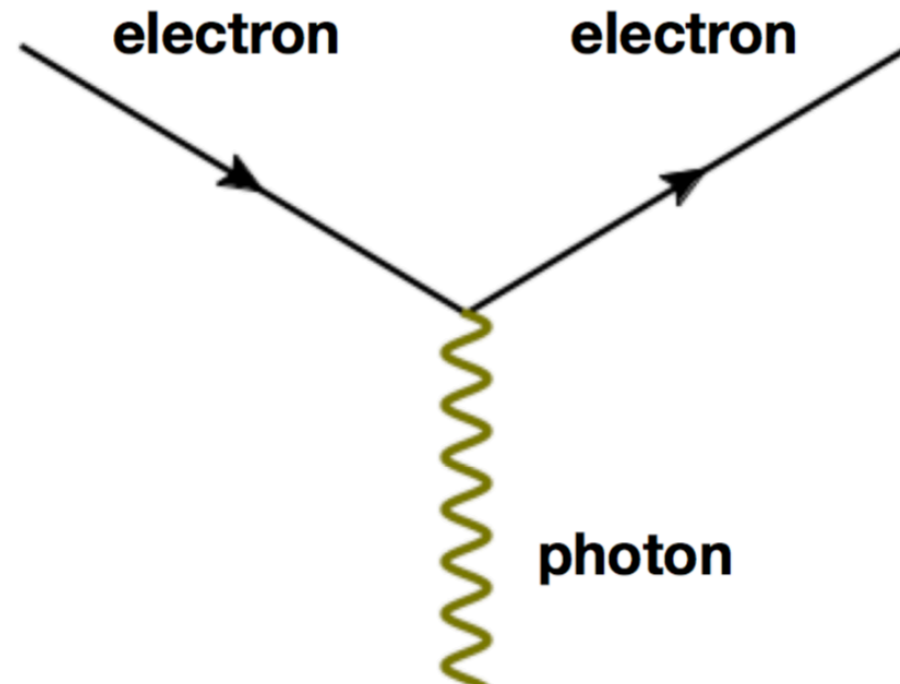


Today's lecture

- ☑ The **weak interaction** compared to the strong and EM forces
- ☑ The **weak boson W** : properties and implications
- ☑ Decays of **heavy hadrons**
- ☑ The **weak boson Z** : properties and implications

Quantum Electrodynamics (QED)

In QED there is a unique **interaction vertex**:



This fact implies the following **important properties** about the electromagnetic interaction:

- ☑ Electric charge is always conserved because the photon **does not carry electric charge**
- ☑ Being electrically neutral, the photon **cannot interact with itself**
- ☑ **Flavour** is conserved by QED interactions: automatic conservation of leptonic and baryonic numbers, as well as strangeness, charmness, and bottomness
- ☑ Since the photon is **exactly massless**, electromagnetism is a **long-range force**

Quantum Chromodynamics (QCD)

Let us summarise what we have learned about the **quantum theory of the strong interactions**: Quantum Chromodynamics

- ☑ **Flavour** is always **conserved** by strong interactions: automatic conservation of leptonic and baryonic numbers, as well as strangeness, charmness, and bottomness
- ☑ Gluons are **charged under color** so they can interact with themselves. They are however **electrically neutral** so they don't affect the electric charge in strongly interacting processes
- ☑ The **strength** of the strong force is not constant: it is more at low energies / large distances (leading to quark confinement into hadrons) but less at high energies / low distances (where it behaves like electromagnetism)
- ☑ While quarks have **fractional electric charge** and baryon number, only hadrons with **integer electric charge** and baryon number are physically allowed

Scattering reactions in QCD

Let's try to understand some **strong-interacting scattering processes** in terms of QCD

exercise

$$\pi^0 + p \rightarrow n + \pi^+$$

Write the corresponding Feynman diagram using **only quarks and gluons**

$$\pi^0 = (u \bar{u}) \qquad \pi^+ = (u \bar{d})$$

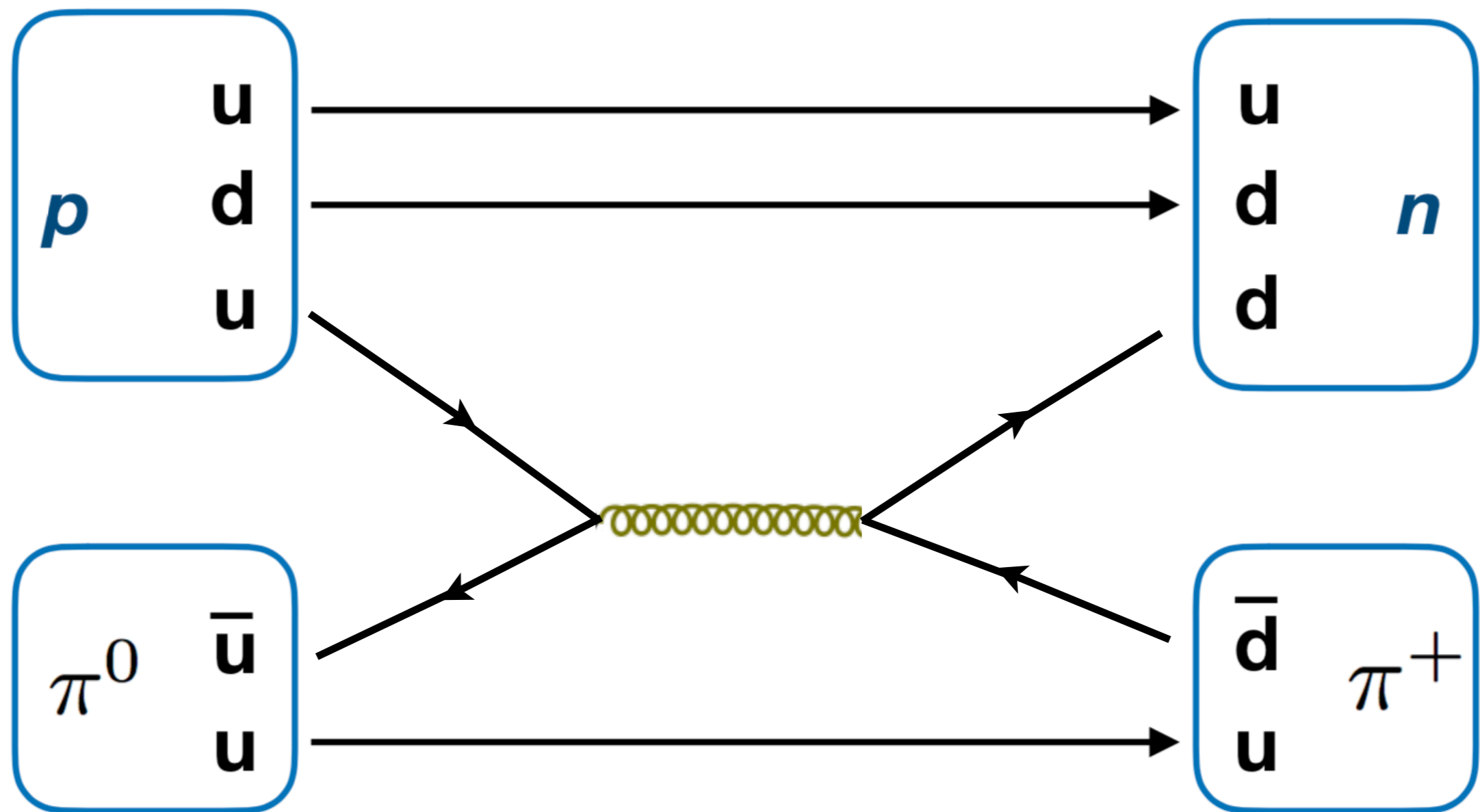
Note also how **Q, B, S, C, \dots** are conserved in this reaction

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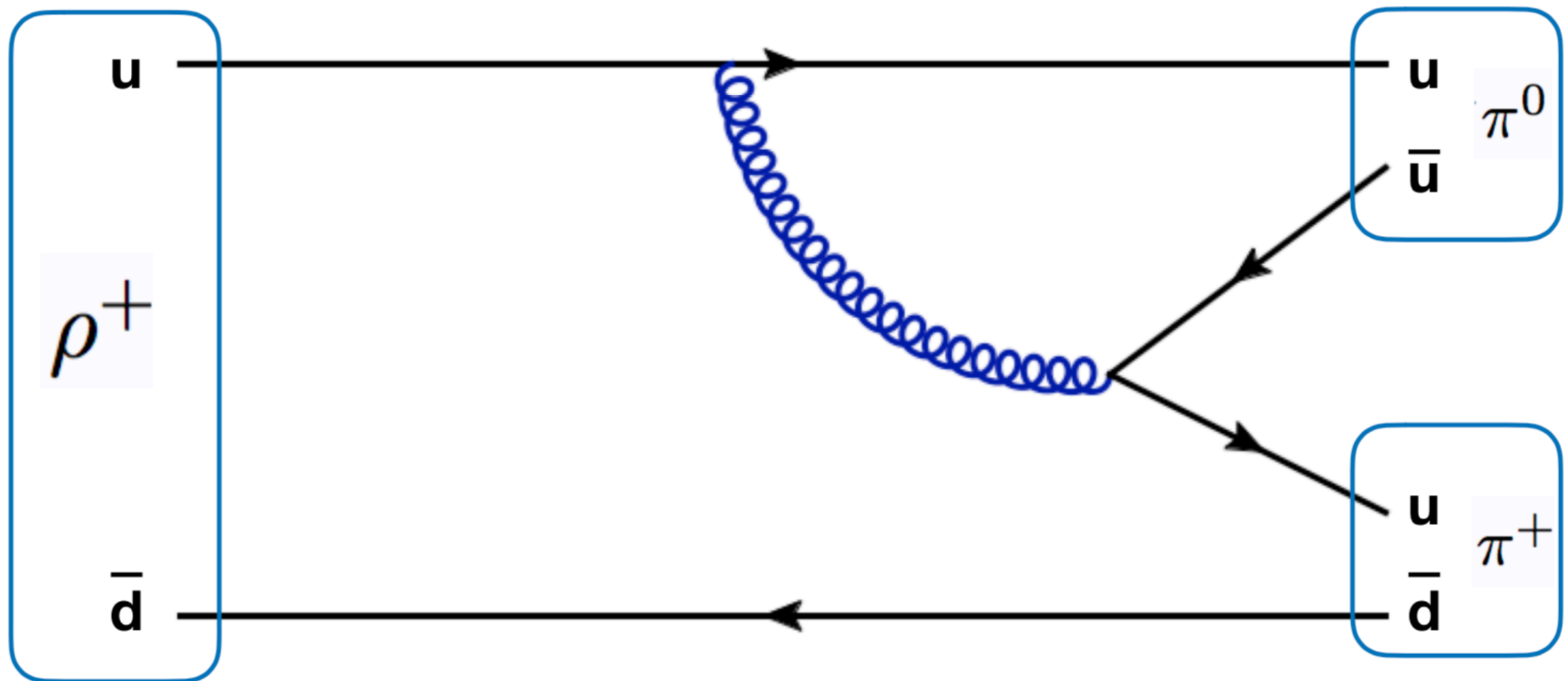
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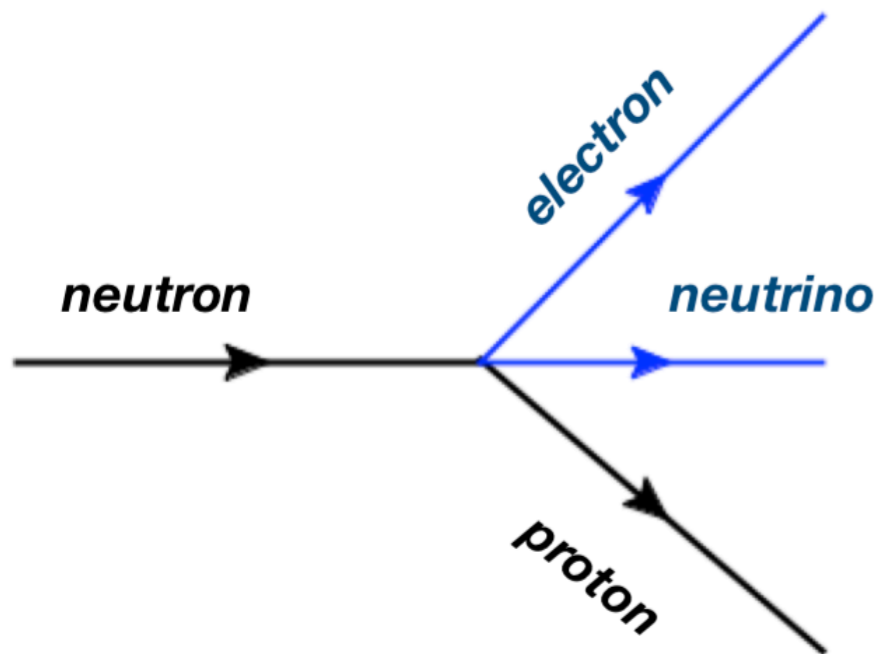
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- ☑ Make sure that all interaction vertices **conserve the corresponding quantum numbers**: for example, if gluons or photons are conserved, then **Q, B, S, C, b, \dots** should be conserved

The weak interaction

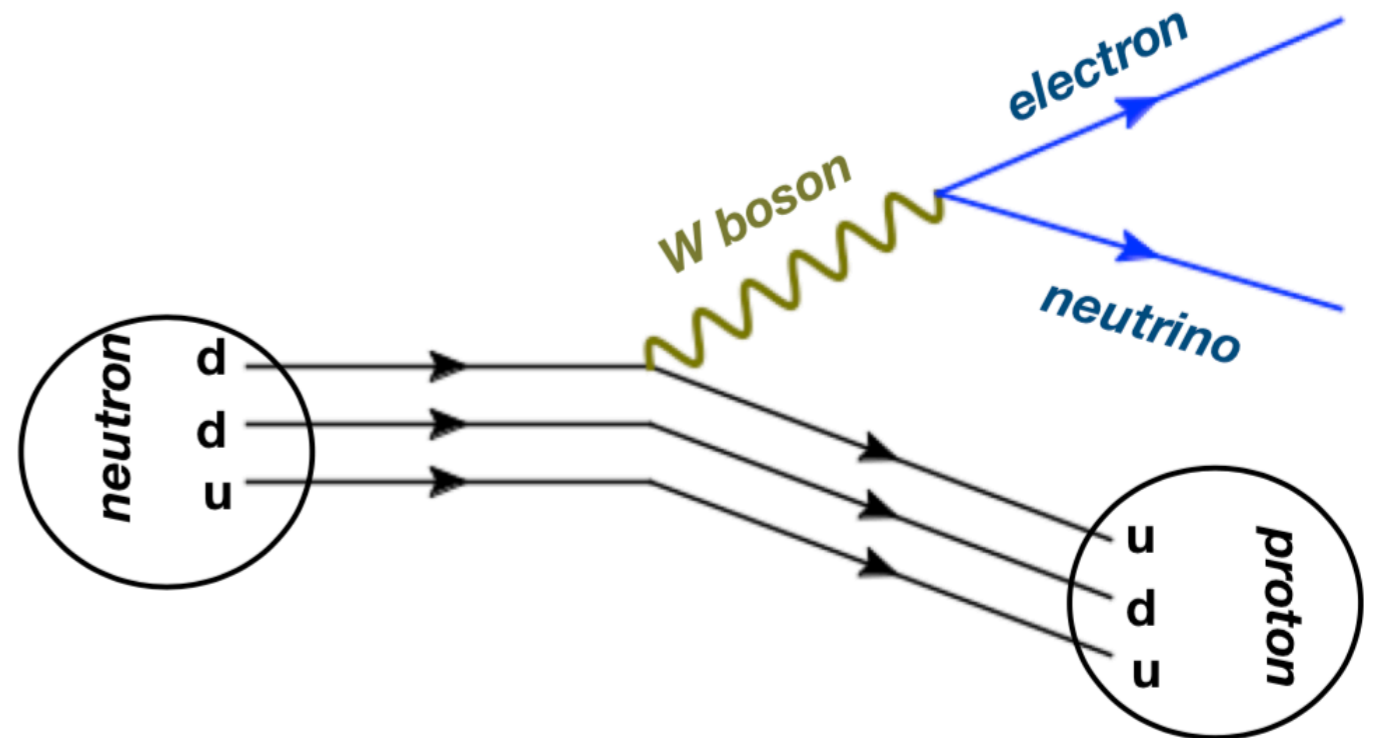
The weak nuclear force

- ✓ Fermi (30s) explained **beta-decay of nuclei** by a **four-body interaction** between neutrons, protons, electrons and neutrinos: the **weak nuclear interaction**
- ✓ Weak interaction also similar to electromagnetism, but with **massive vector bosons, the W and Z particles**. Due to **large masses** (80 and 91 GeV) their interactions are **point-like at low energies**

Fermi picture of the weak interaction



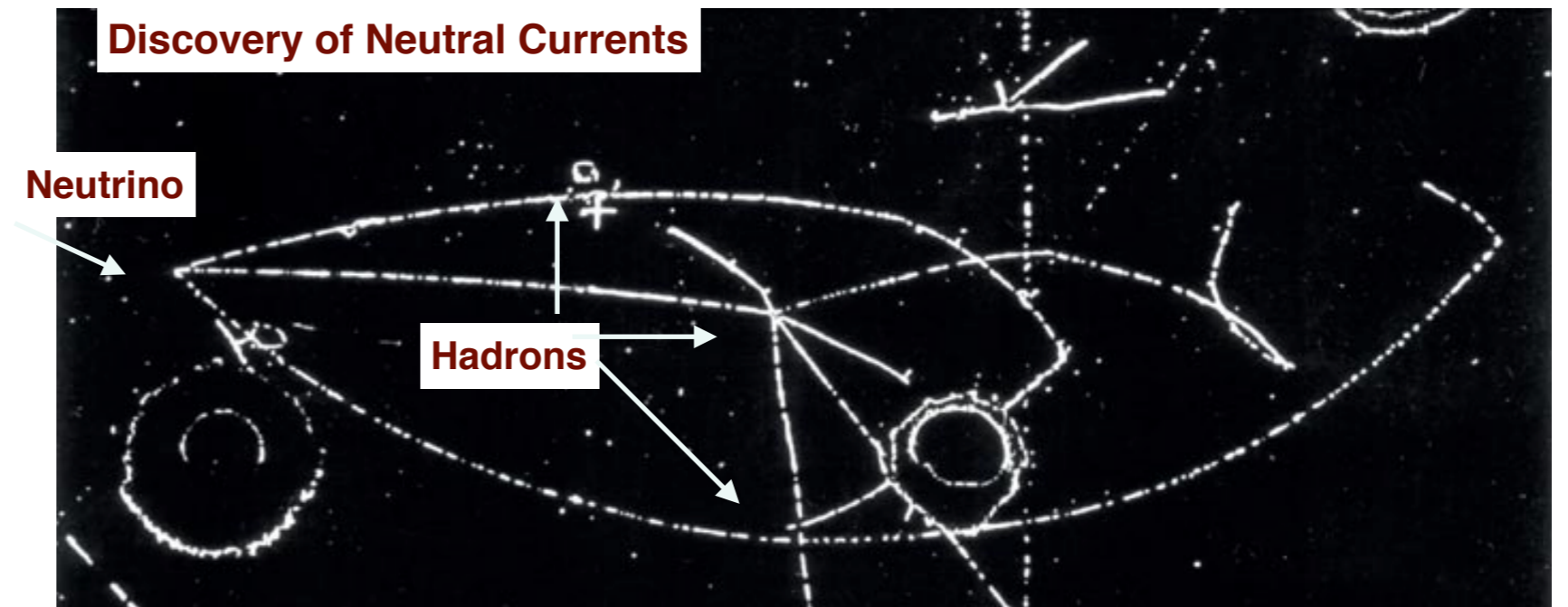
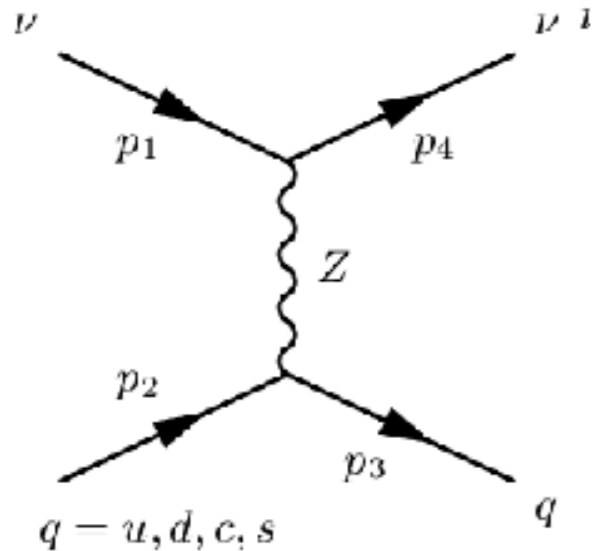
The weak interaction in the Standard Model



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- ✓ Evidence for **Neutral Currents** (73) followed by the **discovery of the W and Z bosons** at the CERN (83)

**Neutral currents in neutrino scattering:
indirect evidence for the Z boson**



Weak force vs electromagnetism

It is useful to enumerate the **properties of the weak interaction** by comparing them with those of the electromagnetic interactions

Electromagnetism

- ☑ A **single type of electric charge** exists: the only thing that varies is its sign and magnitude
- ☑ Electromagnetism is transmitted by **photons**, which are **massless** and **charge-neutral**
- ☑ The **strength of the electromagnetic interaction** is always small: electromagnetism looks the same at all energies/distances

Weak interactions

- ☑ All particles in the SM are carry a **weak charge**, and the specific values **depend on the matter particle**

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$$m_{W^\pm} = 80.385 \text{ GeV}$$

$$m_{Z^0} = 91.1876 \text{ GeV}$$

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- ☑ The strong interaction is transmitted by the **W** and **Z** bosons, which are **massive** and charged under the weak force
- ☑ The weak interaction is always weak and confined to small scales (large value of $m_{W,Z}$)

$$\text{range : } \Delta r \sim m^{-1} \begin{cases} \rightarrow \Delta r \simeq \infty \text{ (EM, QCD)} \\ \rightarrow \Delta r \simeq 10^{-18} \text{ m (weak)} \end{cases}$$

Weak reactions

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Let's illustrate this with two reactions mediated by the weak force

$$\overline{K}^0 \rightarrow \pi^+ + \pi^-$$

$$(s \bar{d}) \rightarrow (u \bar{d}) + (d \bar{u})$$

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exercise

$$D^+ \rightarrow \overline{K}^0 + e^+ + \nu_e$$

Compute the variation in strangeness in this reaction

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The weak boson W

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The weak interactions are mediated by three massive bosons: W^+ , W^- , Z^0

The main properties of the **W bosons** are:

- ☑ As opposed to the **massless** gluons and photons, the W boson is **very massive**, around 80 times the proton mass

$$m_\gamma = 0$$

$$m_g = 0$$

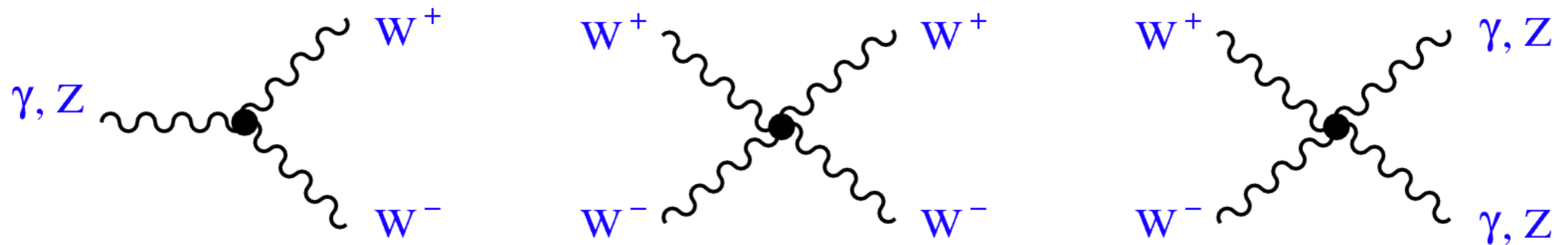
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Note how all these **interaction vertices** satisfy electric charge conservation

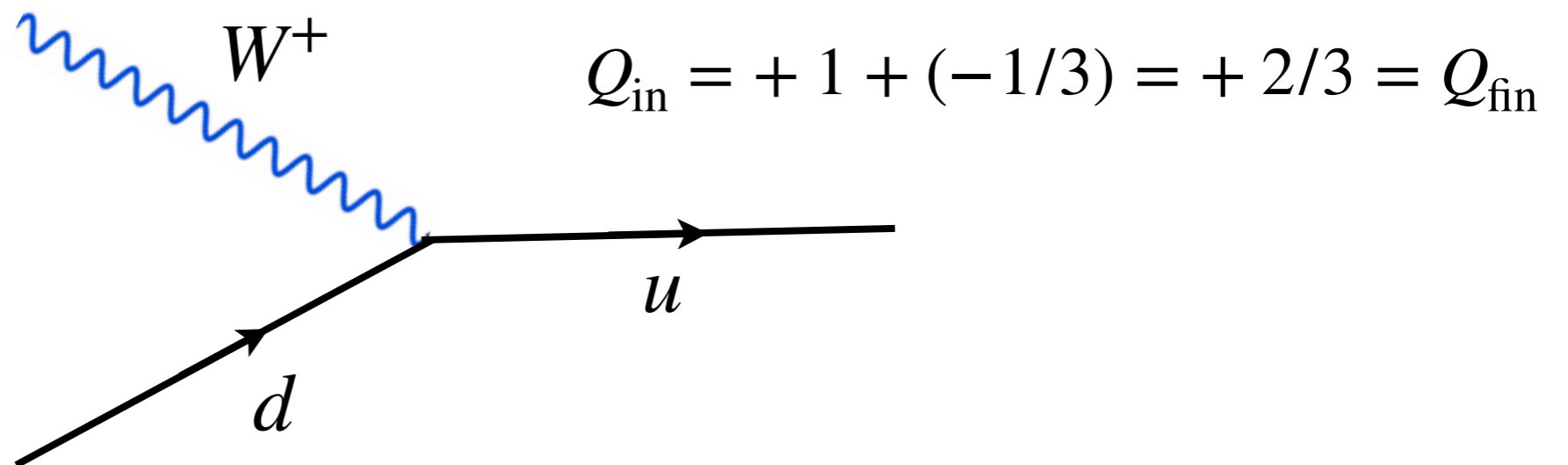
$$Q_{\text{in}} = +1 + (-1) = 0 = Q_{\text{fin}}$$

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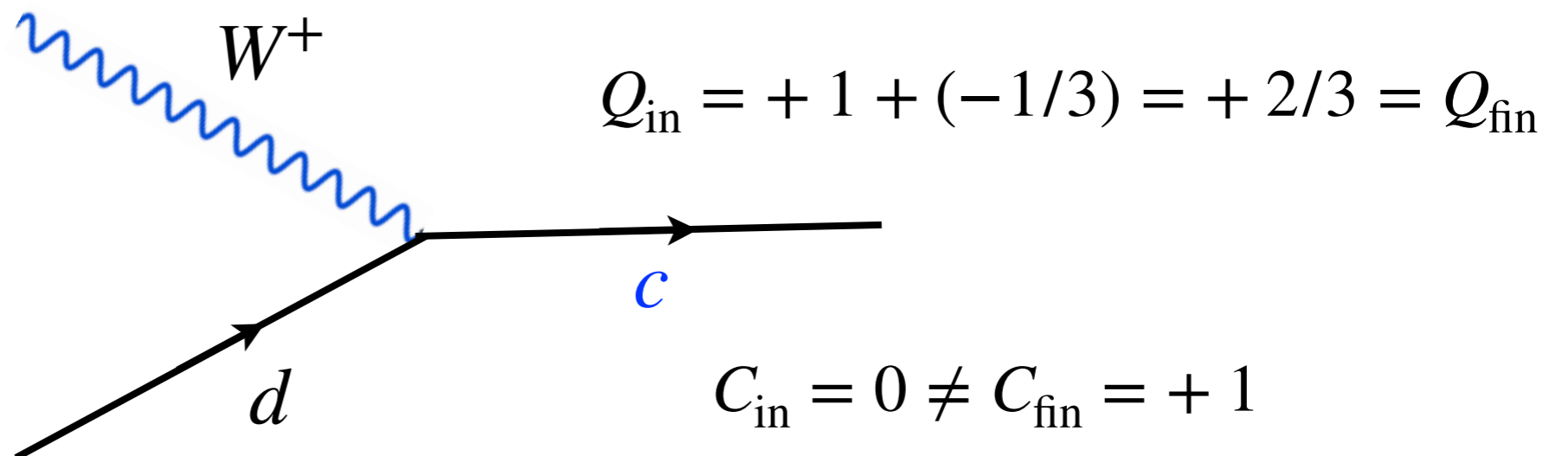


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- ☑ In weak interaction processes **mediated by the W boson**, the flavour quantum numbers (strangeness, charmness, bottomness) are **not conserved** quantities

The weak boson W

Taking into account these properties, some of the physically allowed reactions involving **quarks** and **W bosons** will be:

$$\begin{aligned} u + W^- &\rightarrow d, & u + W^- &\rightarrow s, & d + W^+ &\rightarrow u, & s + W^+ &\rightarrow u, \\ \bar{u} + W^+ &\rightarrow \bar{d}, & \bar{u} + W^+ &\rightarrow \bar{s}, & \bar{d} + W^- &\rightarrow \bar{u}, & \bar{s} + W^- &\rightarrow \bar{u}, \\ W^+ &\rightarrow u + \bar{d}, & W^+ &\rightarrow u + \bar{s}, & W^- &\rightarrow d + \bar{u}, & W^- &\rightarrow s + \bar{u}, \end{aligned}$$

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- ☑ You can always **replace** a given quark by the corresponding quark of a **different generation**: for example a down antiquark by a strange antiquark
- ☑ If a given reaction is allowed, the corresponding reaction involving the **antiparticles** is also physically allowed

$$\bar{u} + W^+ \rightarrow \bar{s} \quad \Rightarrow \quad u + W^- \rightarrow s$$

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Taking into account these properties, some of the physically allowed reactions involving **leptons** and **W bosons** will be:

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$$e^+ + W^- \rightarrow \bar{\nu}_e \quad \Rightarrow \quad \tau^+ + W^- \rightarrow \bar{\nu}_\tau$$

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- ☑ You can always **replace** the two leptons of a given generation for the corresponding two leptons of **another generation**
- ☑ The **individual leptonic quantum numbers** are always conserved in weak reactions

exercise

The weak boson W

Draw the Feynman diagram for the following process

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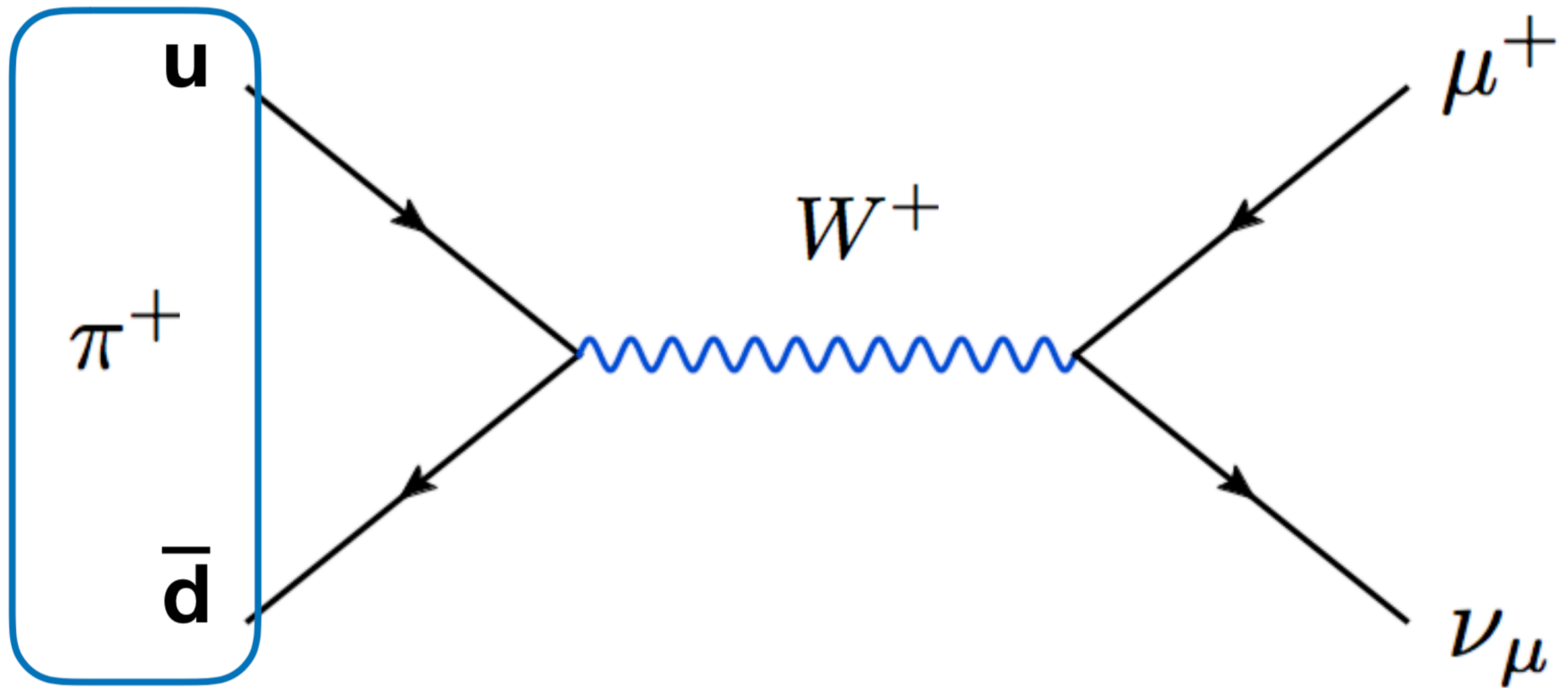
- We have a neutrino in the final state: the **weak interaction** must be involved
- Quarks and leptons only interact indirectly via either photons or W, Z bosons
- Since the electric charge is $Q=+-1$, then a positively charged **W boson** is involved
- We know what **vertices are allowed** involving quarks or leptons and a W boson

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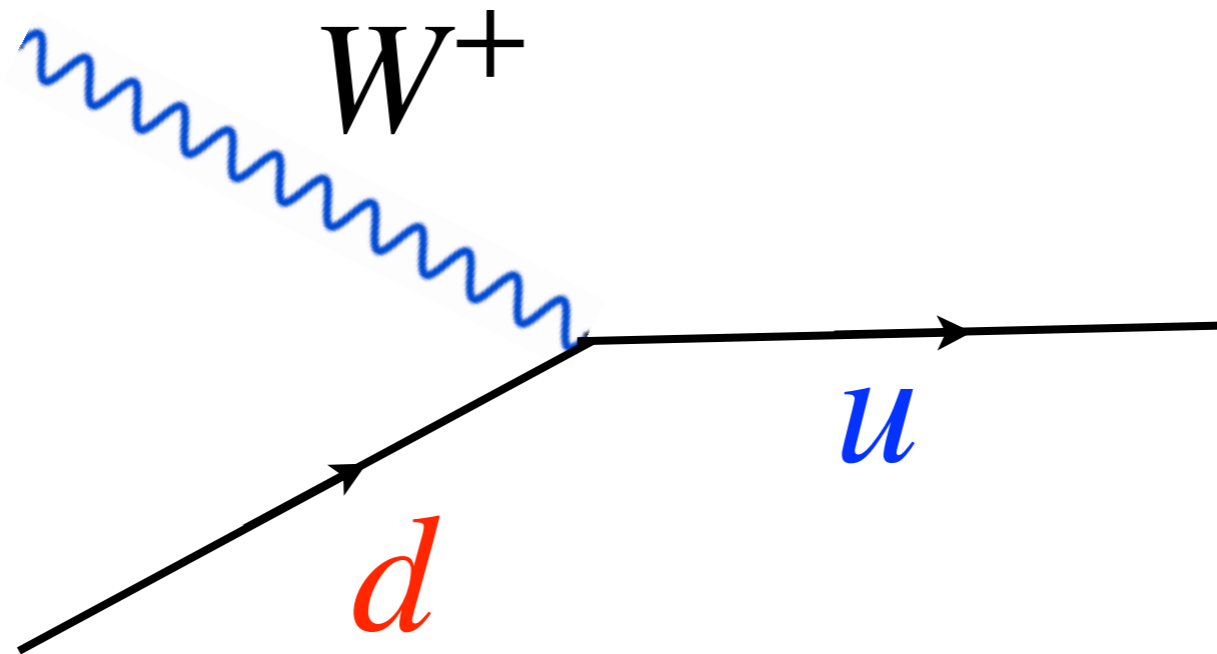


You can check that all relevant quantum numbers are **conserved**: L, B, Q, \dots

Heavy hadron decays

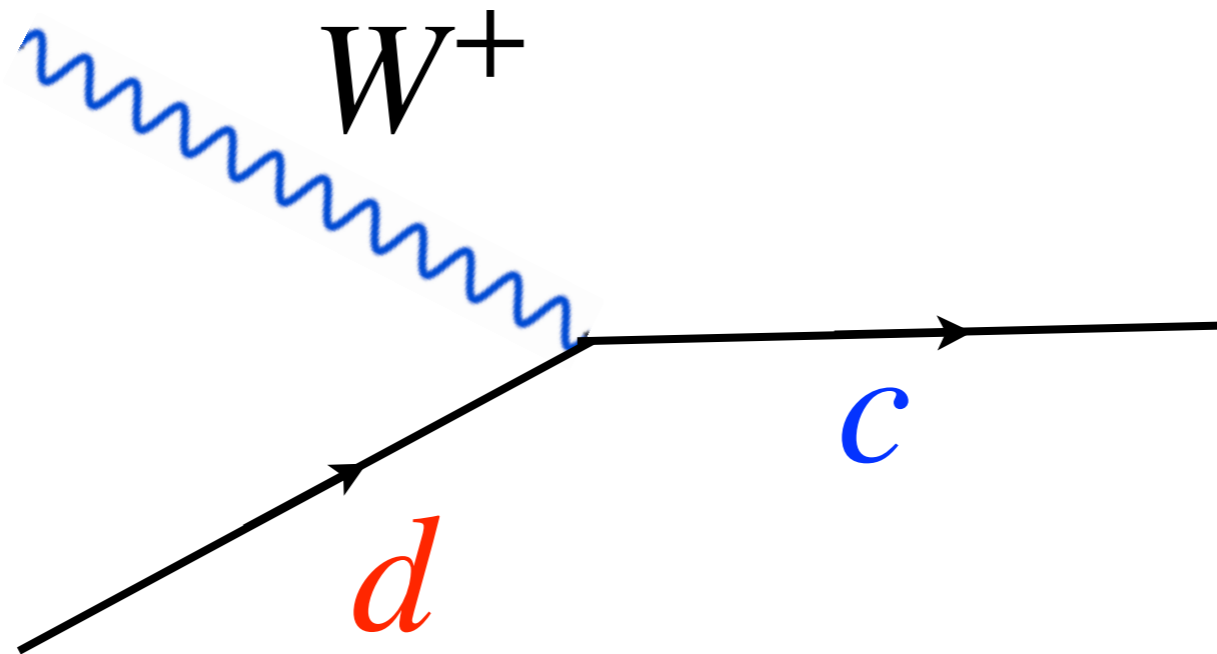
Weak coupling between generations

We have seen that in processes mediated by the weak gauge boson W the **flavour** of the quarks will **change**



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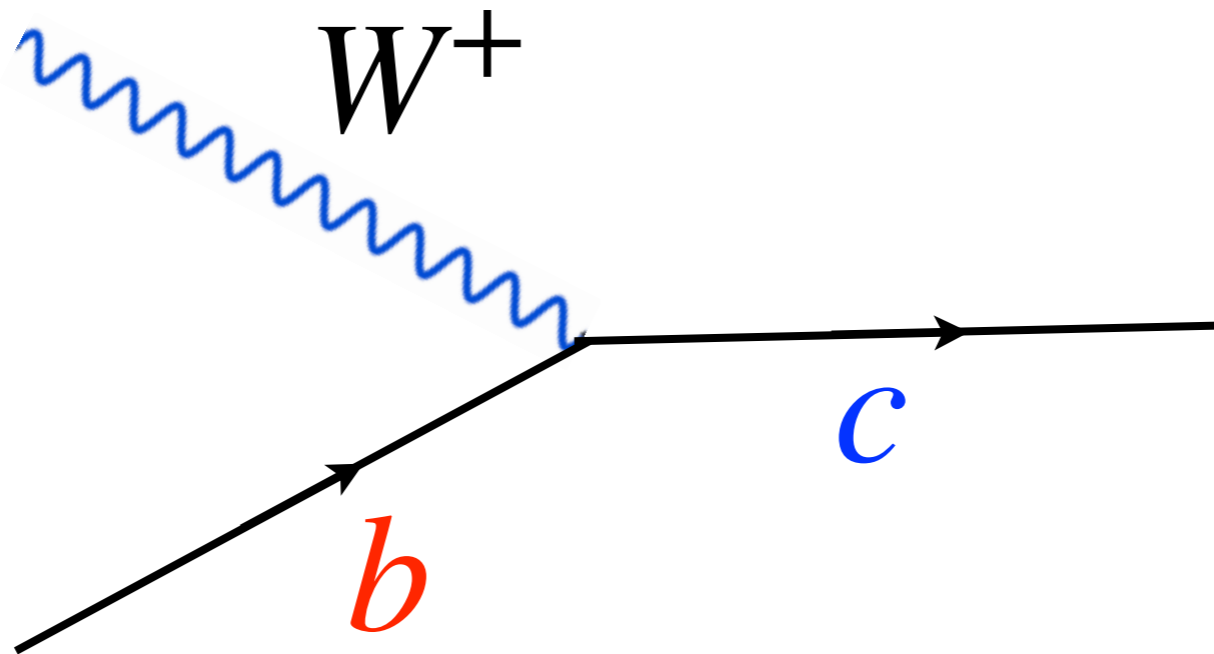
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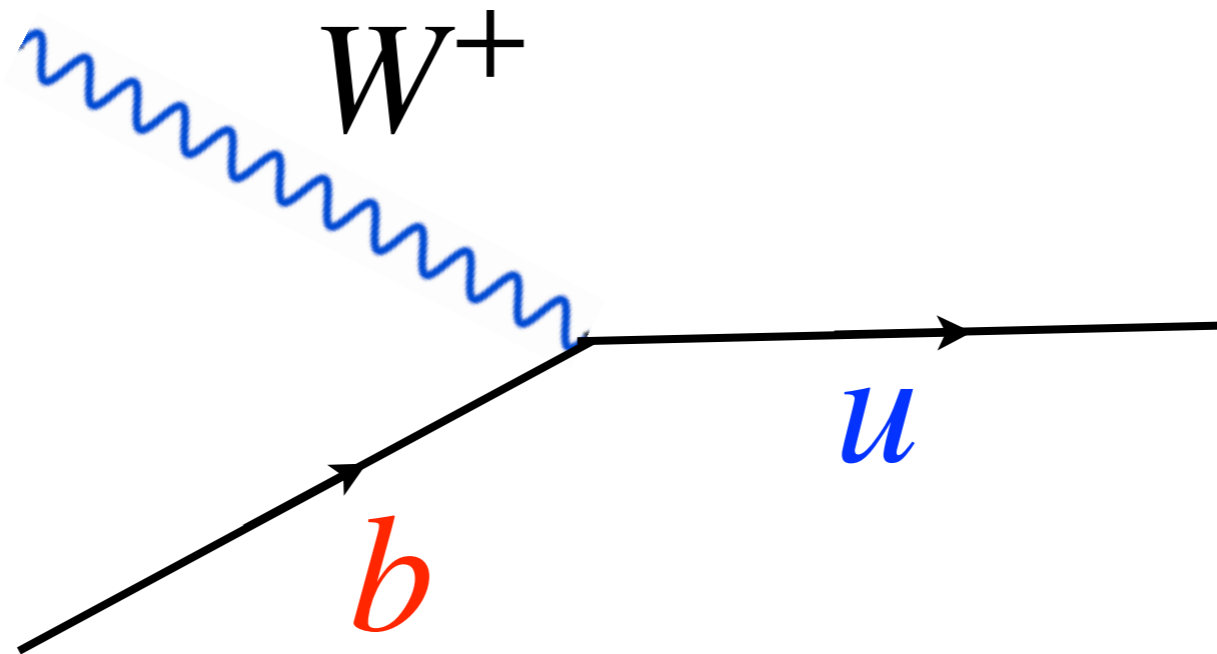
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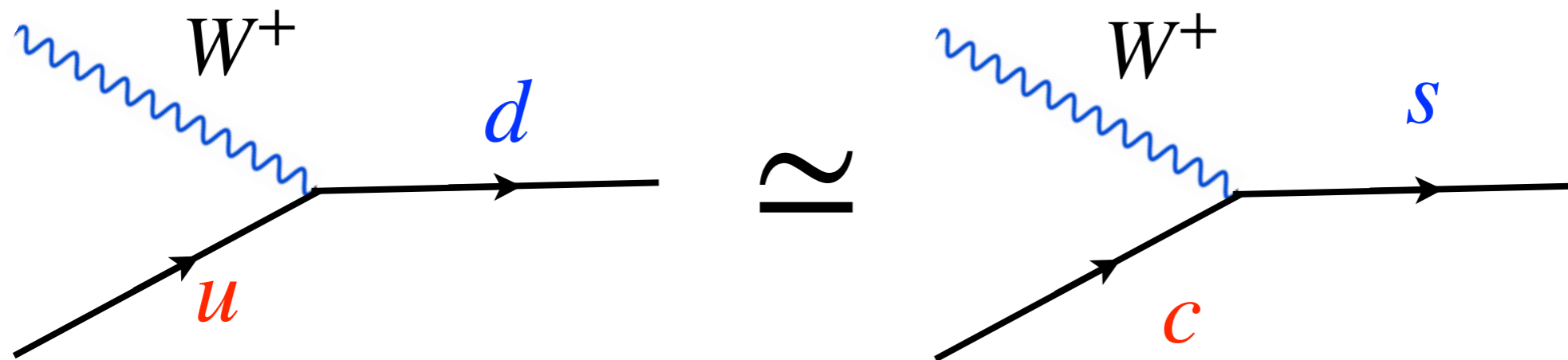


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The weak interactions mediates **transitions** between **quarks of different generations**

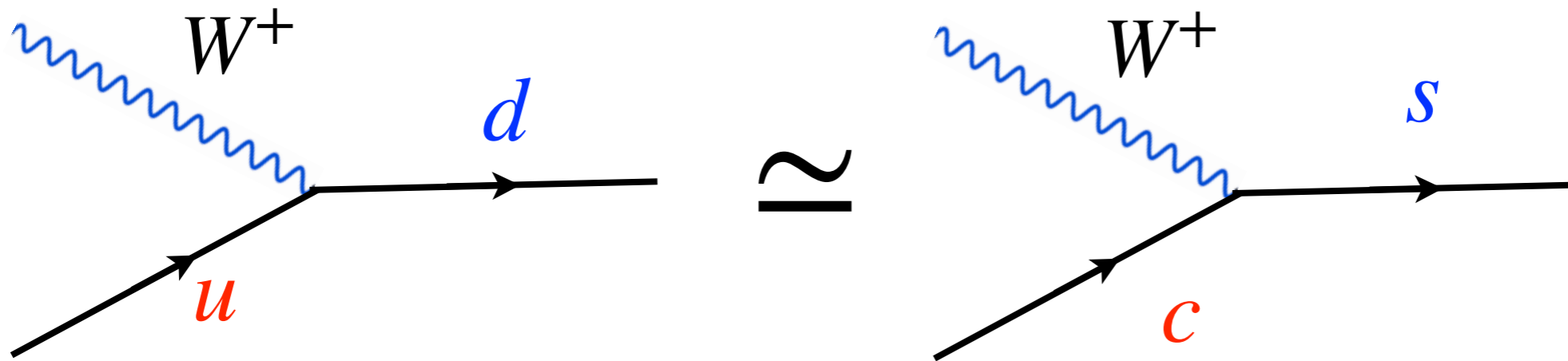
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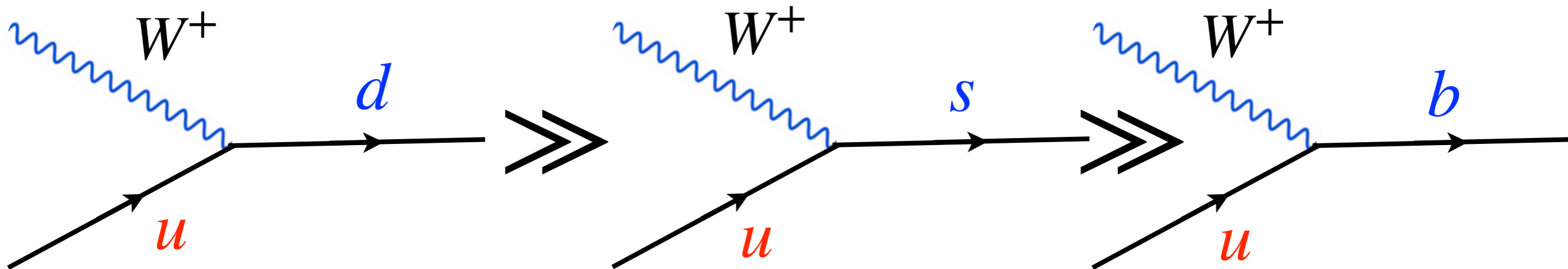


Weak coupling between generations

The **strength of the weak coupling** is similar between **quarks of the same generation**



The **strength of the weak coupling** is smaller between **quarks of different generation**



Weak coupling between **gens 1 and 2** bigger than between **gens 1 and 3**

Drawing Feynman diagrams

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Heavy hadron decays

exercise

This **hierarchy of the weak couplings** between quark generations is particularly important in order to understand the decays of **hadrons** that contain **heavy quarks**

$$B^0 \rightarrow D^- + \mu^+ + \nu_\mu \quad B^0 = (d\bar{b}) \quad D^- = (d\bar{c})$$

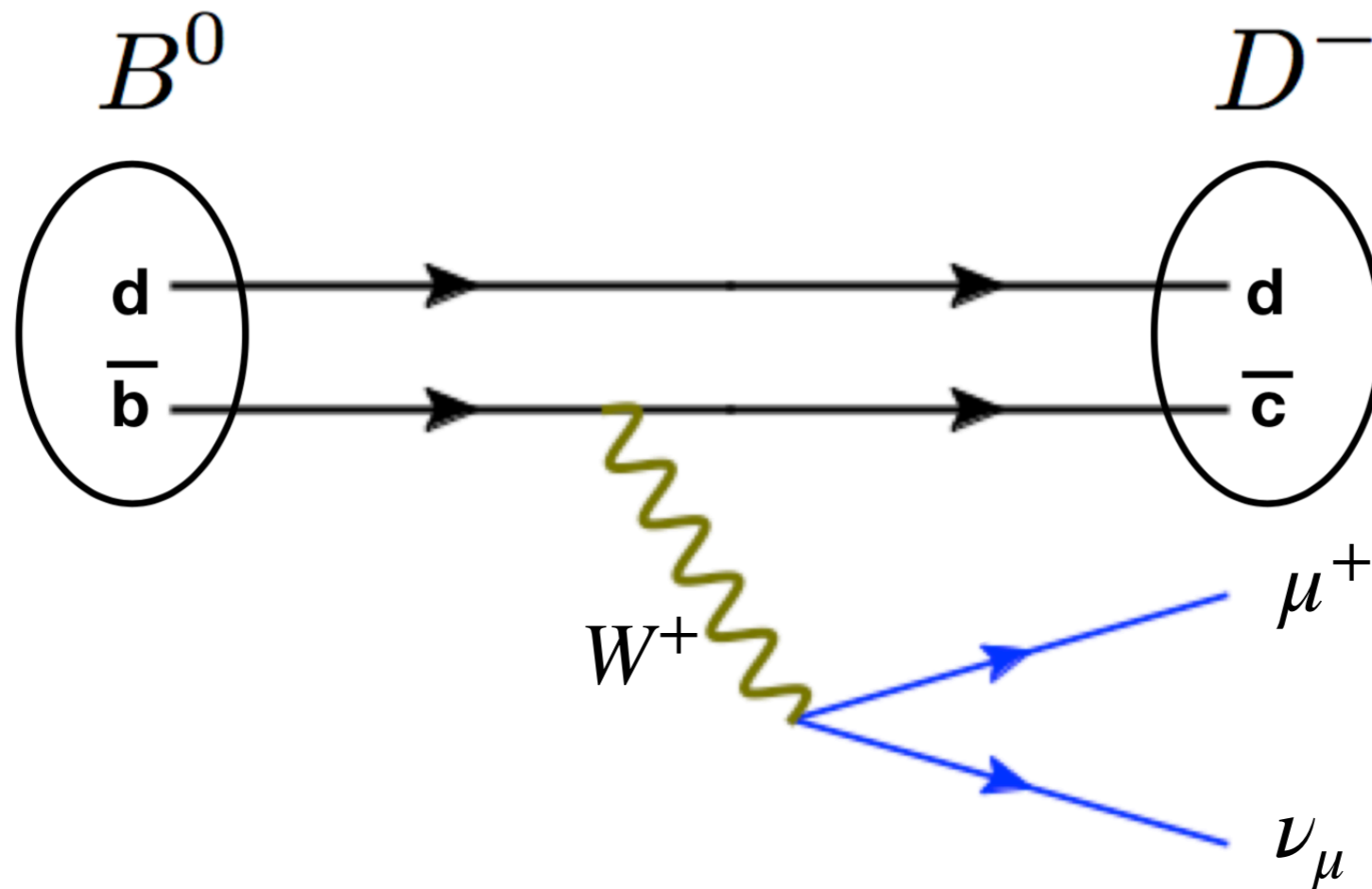
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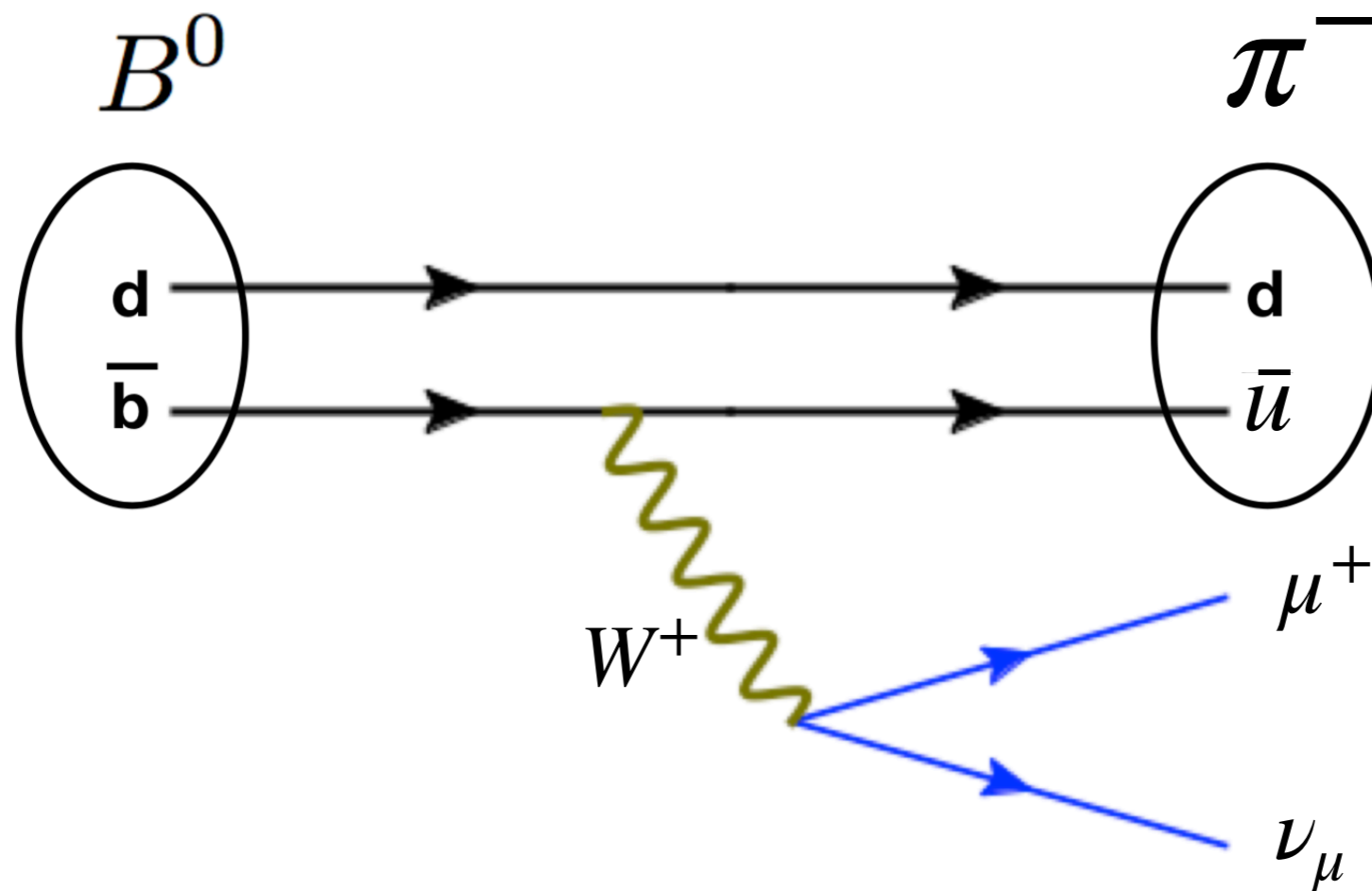
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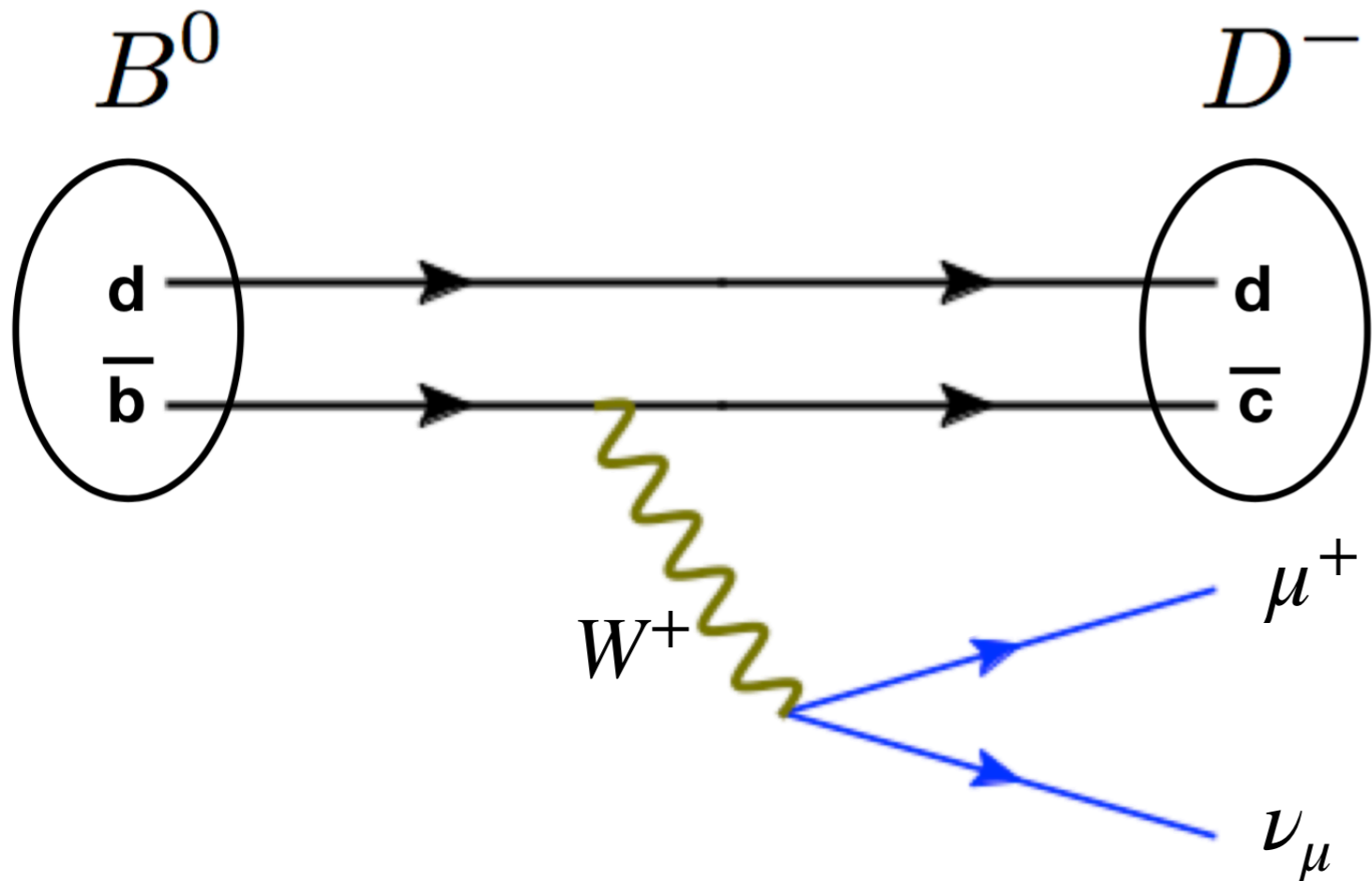
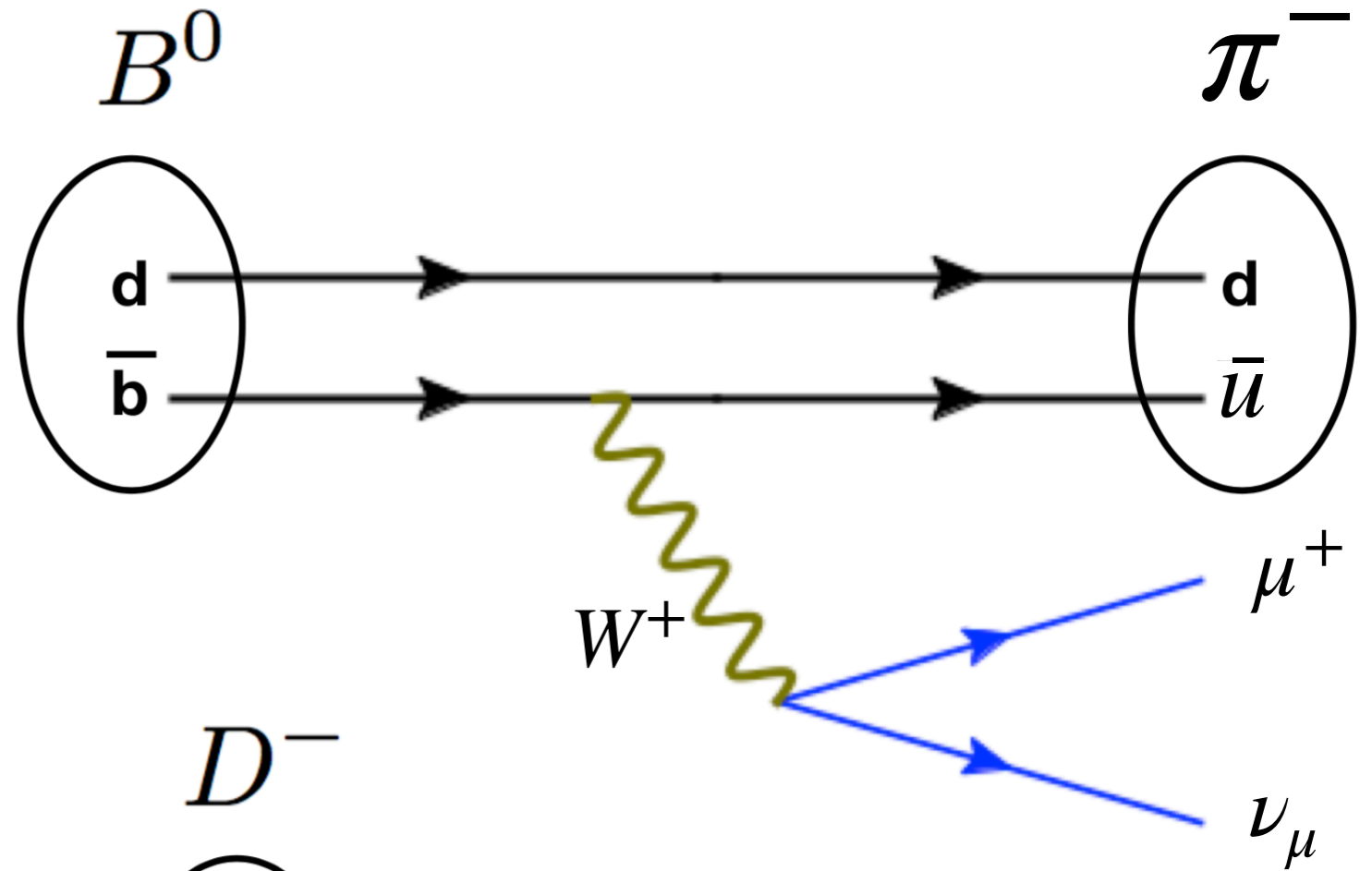
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what is the corresponding Feynman diagram?



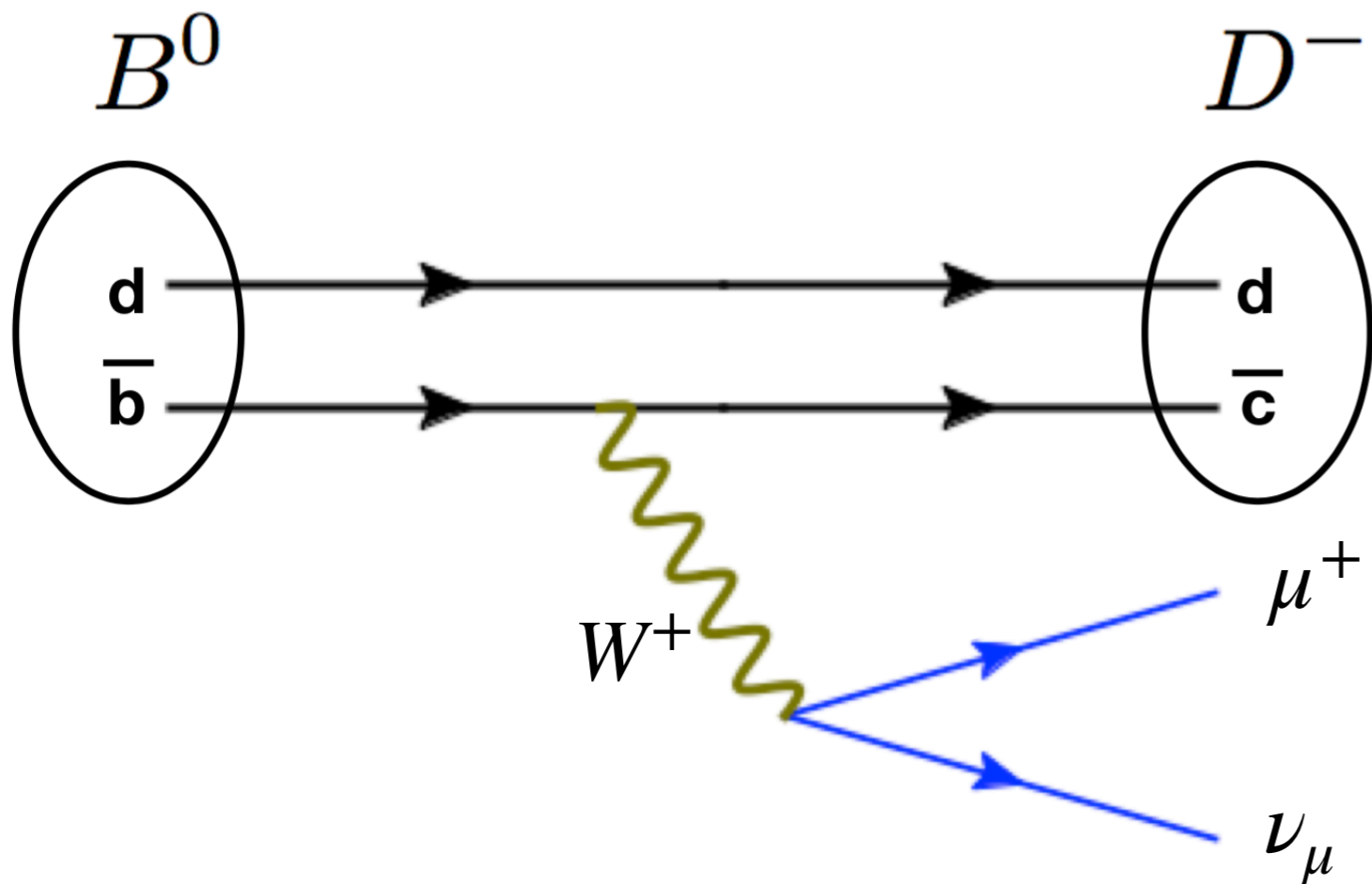
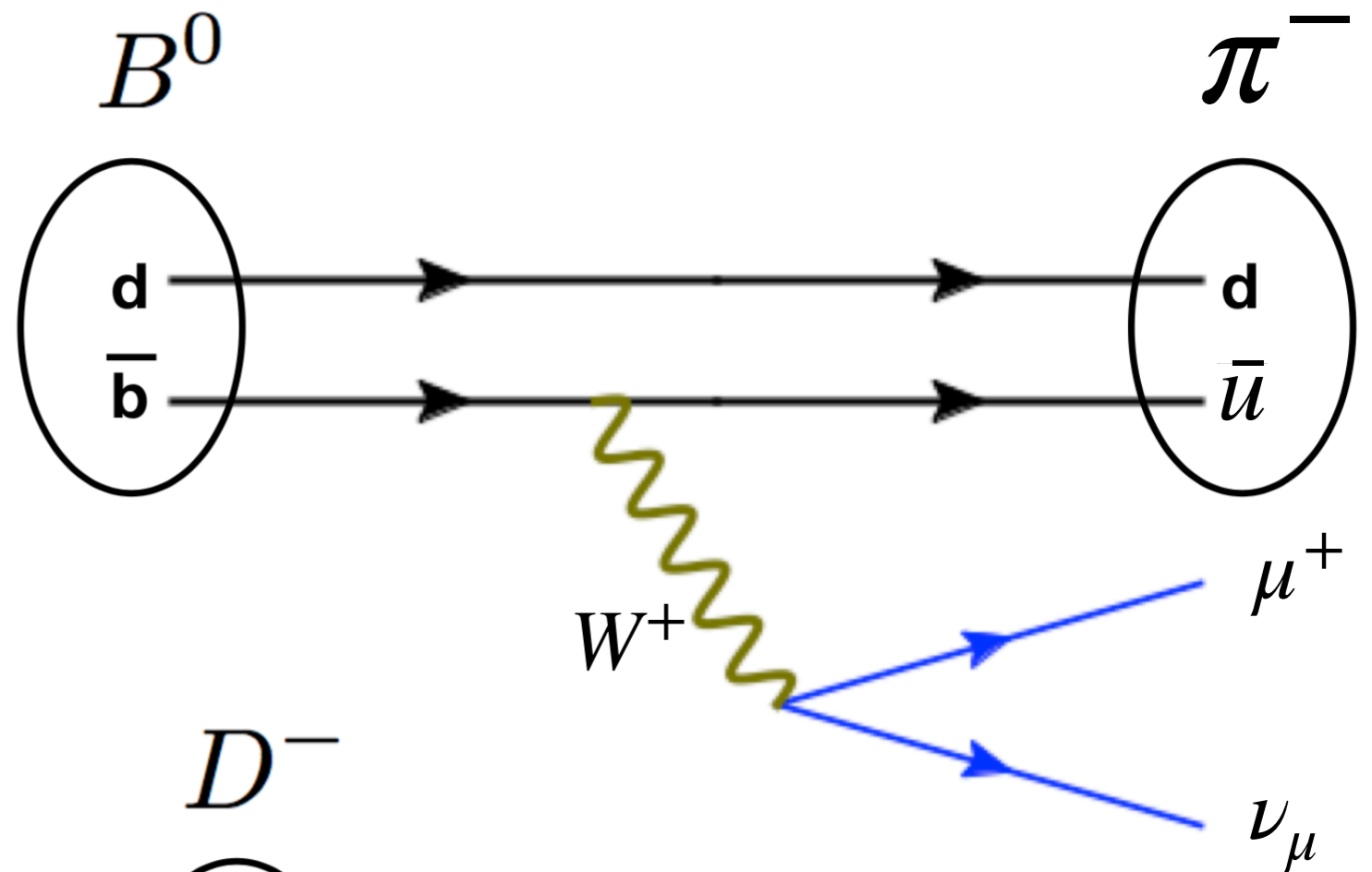
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Which of the two reactions is **most likely** to take place?



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The decay into a pion is more suppressed, since the **coupling W_{ub}** (gens 1 and 3) is **smaller** than the **coupling W_{cb}** (gens 1 and 2)

exercise

Heavy hadron decays

Draw the Feynman diagram associated to this **heavy hadron decay**

$$D^0 \rightarrow \pi^- + K^- + \pi^+ \quad \pi^+ = (u \bar{s})$$

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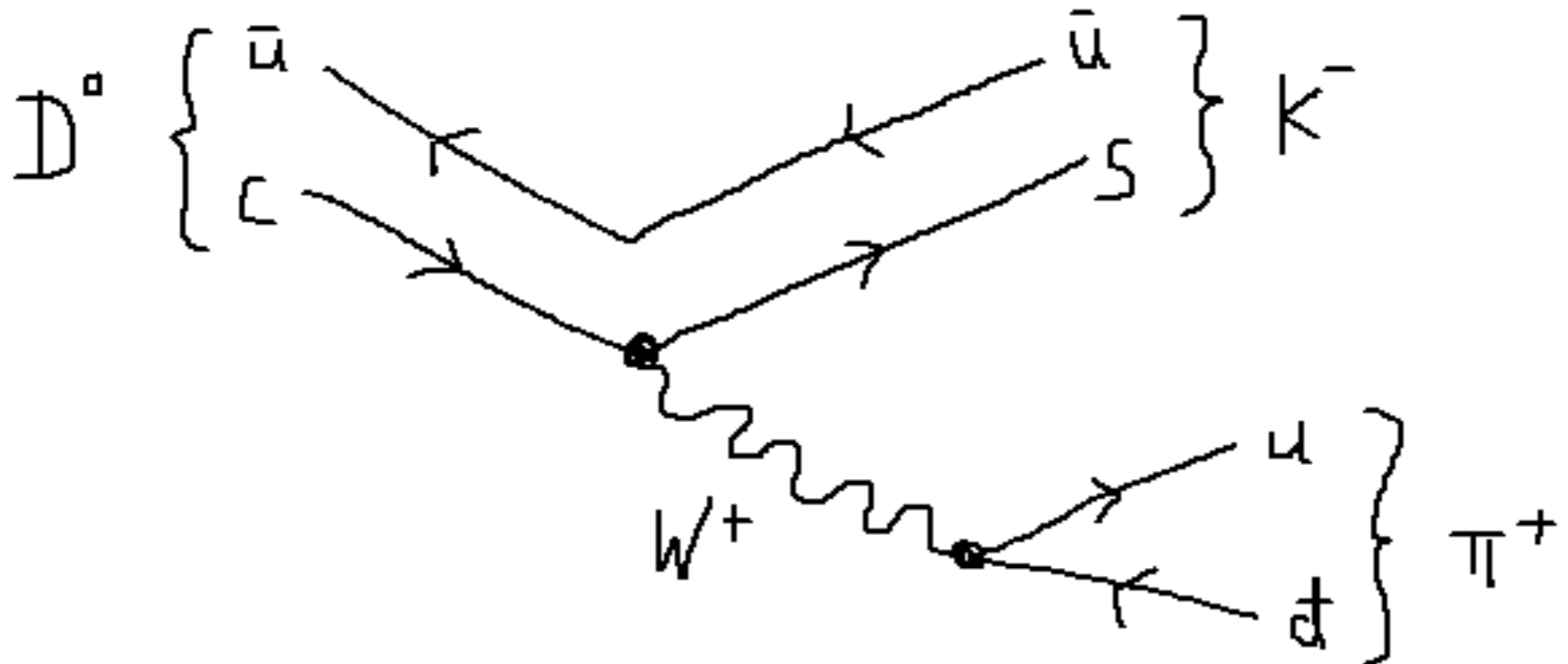
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How do these two decay models relate to each other?

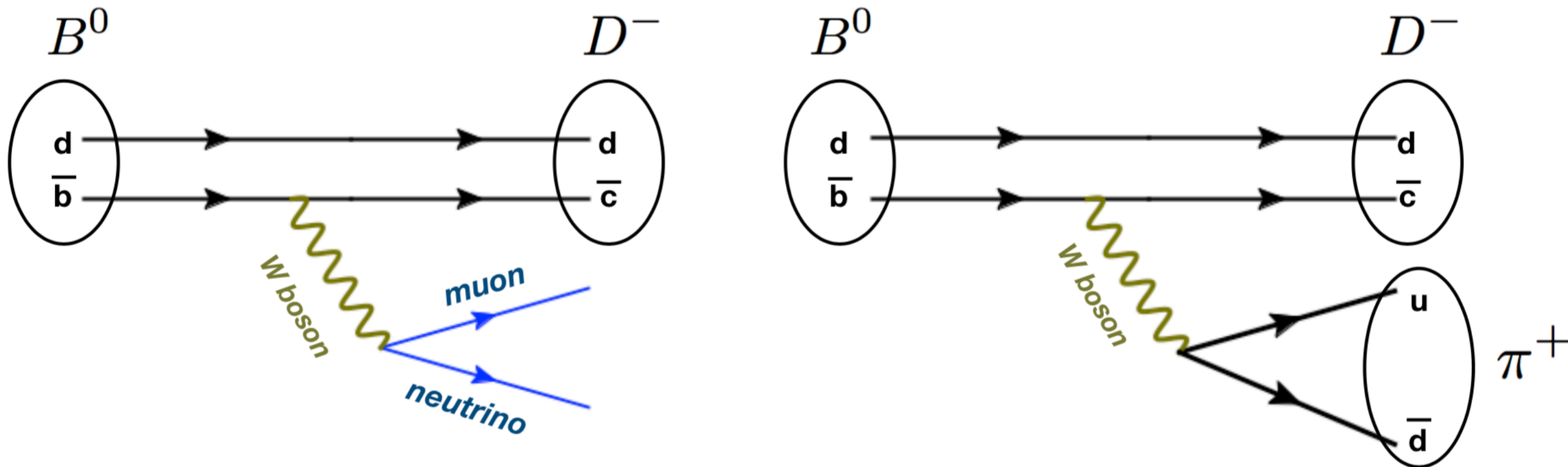
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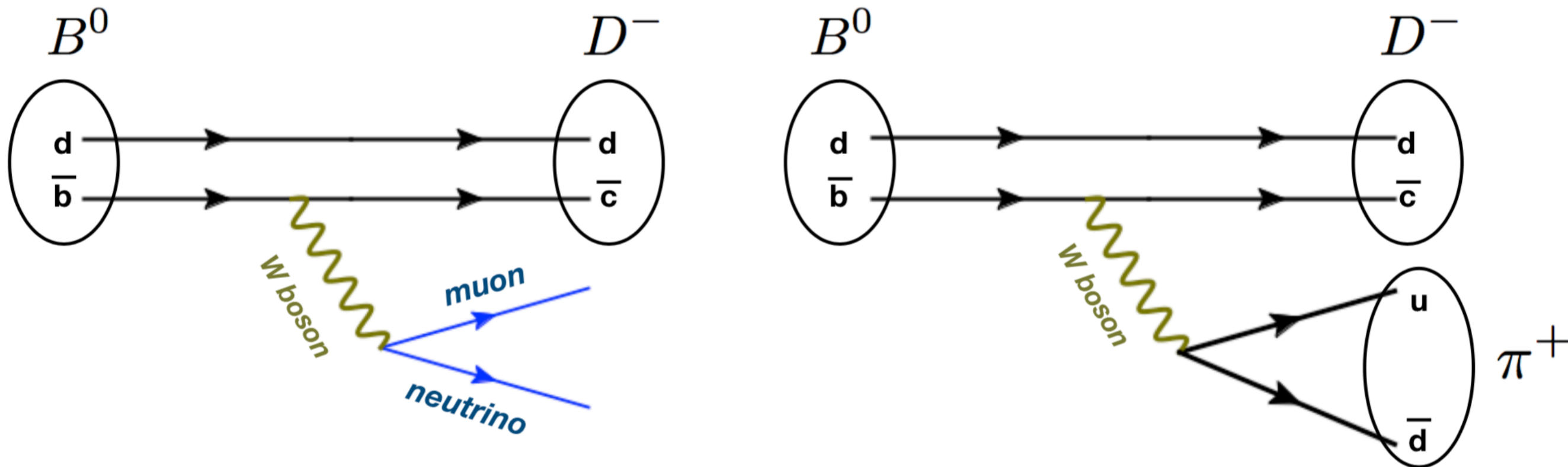
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The main properties of the **Z bosons** are:

- ☑ As opposed to the **massless** gluons and photons, the **Z** boson is **very massive**, around 91 times the proton mass (similar to W boson)

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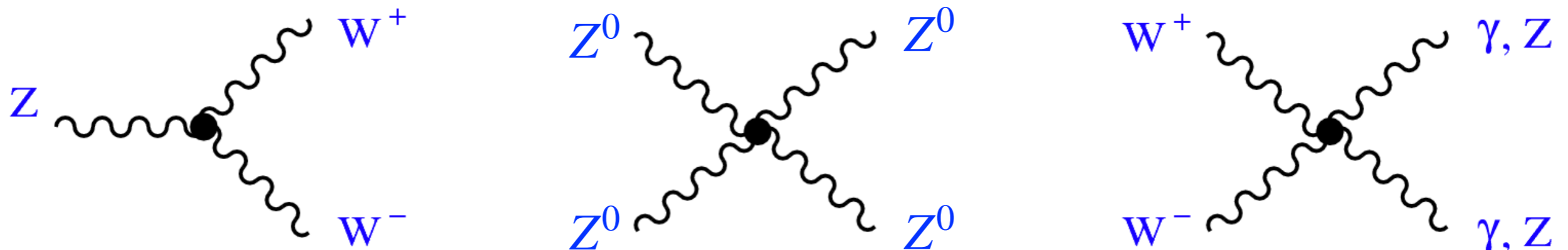
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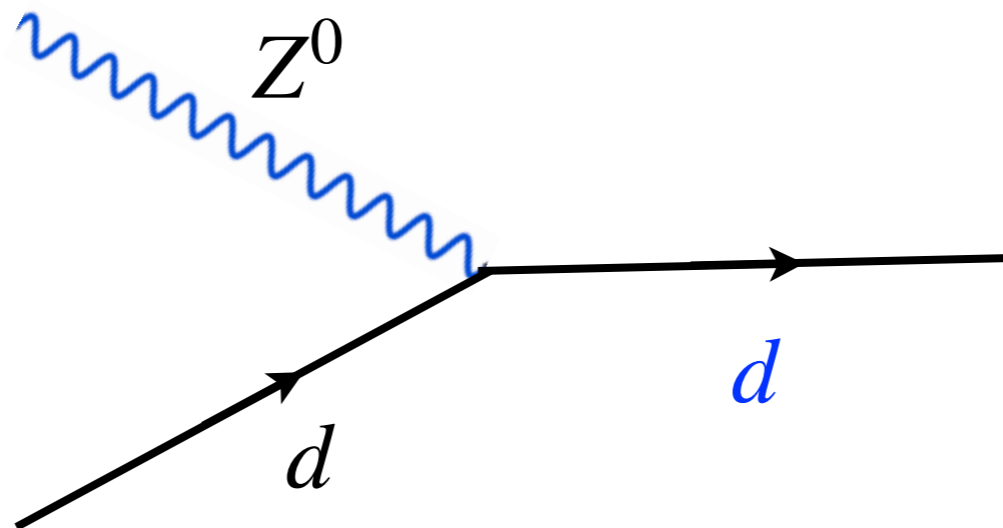


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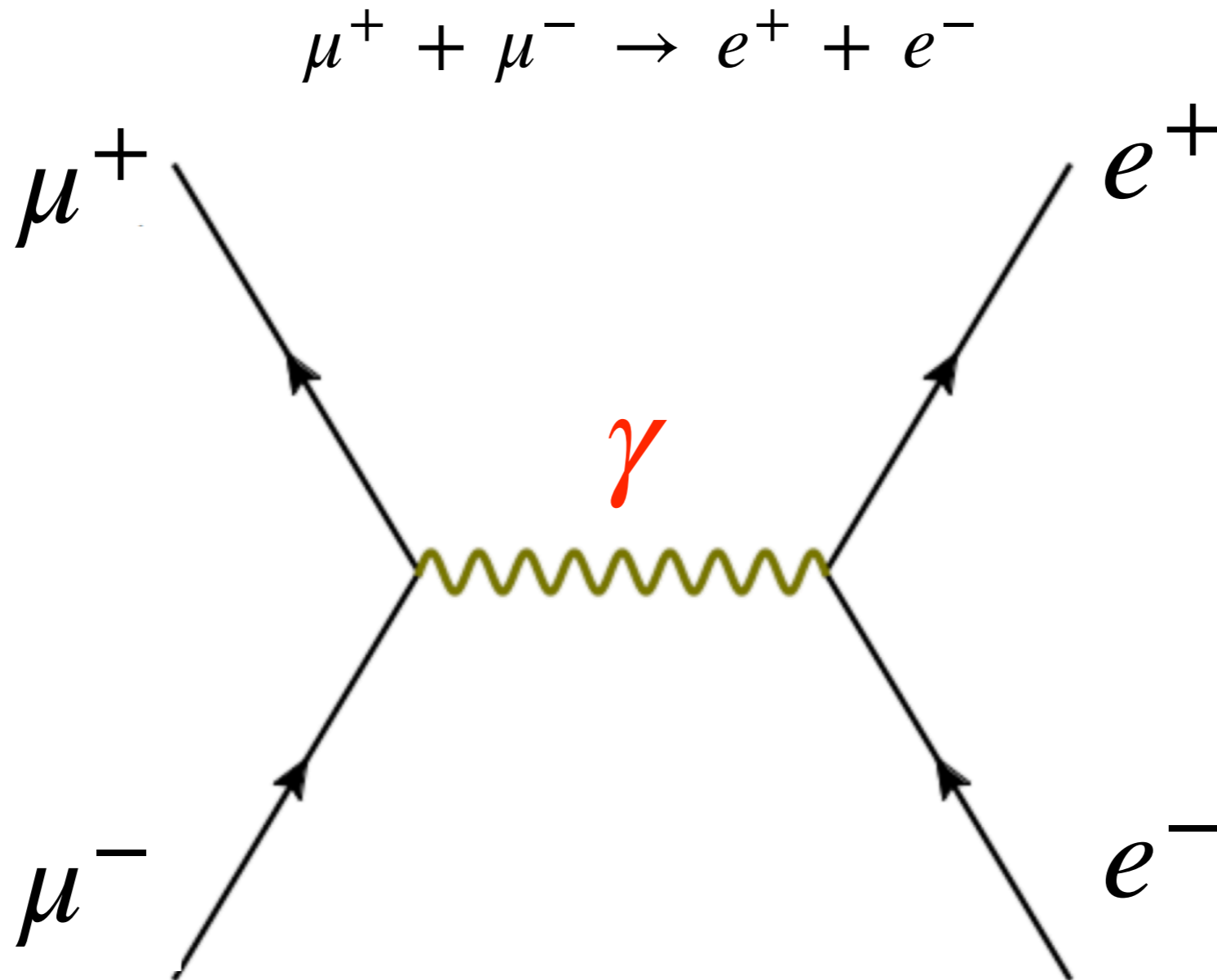
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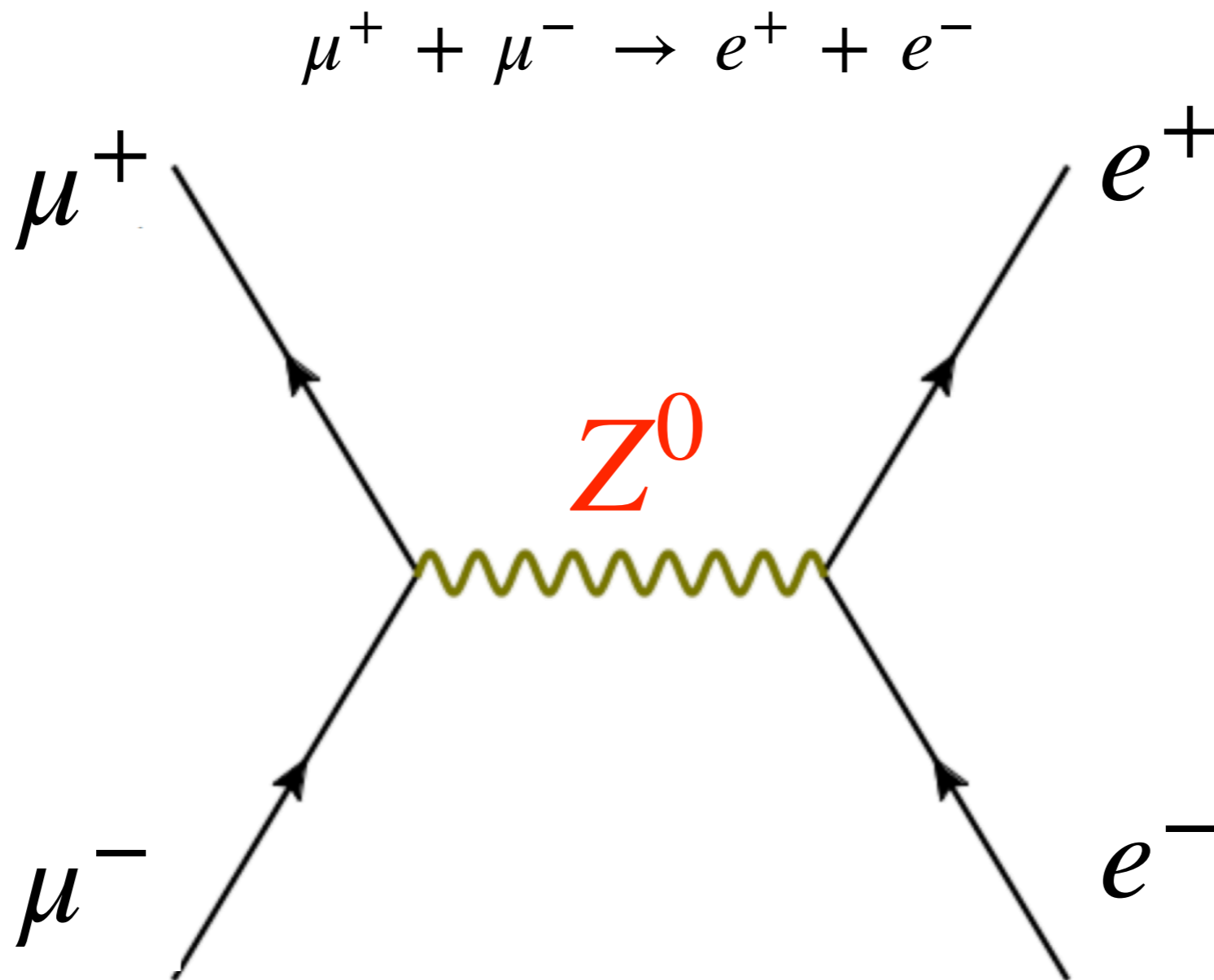
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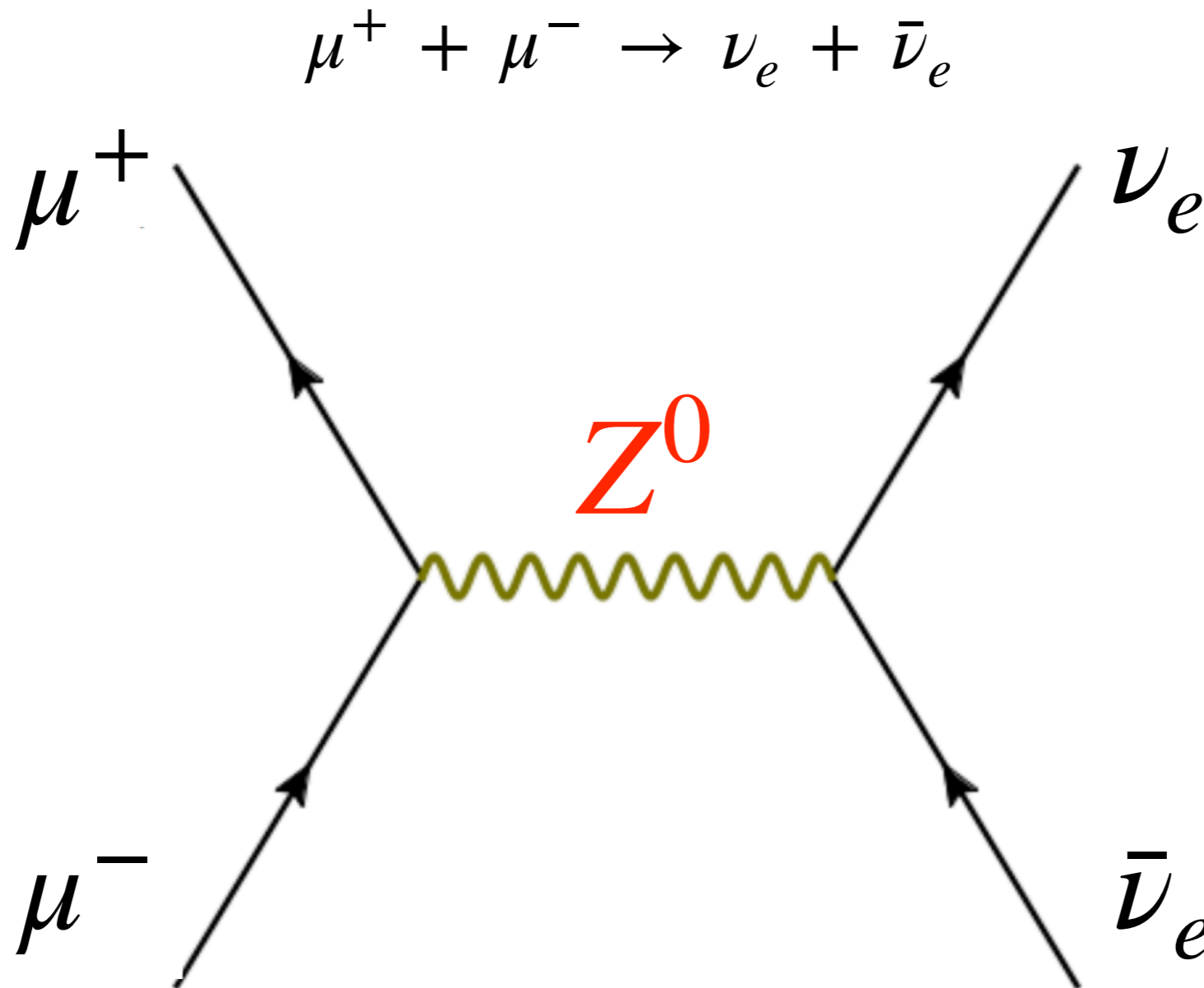
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The Z boson also mediates processes involving **neutrinos**



The weak boson Z

We can now summarise the **weak interaction vertices** involving the Z boson

with quarks

$$u + \bar{u} \rightarrow Z^0, \quad d + \bar{d} \rightarrow Z^0, \quad s + \bar{s} \rightarrow Z^0, \dots$$

$$u + Z^0 \rightarrow u, \quad d + Z^0 \rightarrow d, \quad s + Z^0 \rightarrow s, \dots$$

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with leptons

$$e^+ + e^- \rightarrow Z^0, \quad \mu^+ + \mu^- \rightarrow Z^0, \quad \nu_e + \bar{\nu}_e \rightarrow Z^0, \dots$$

$$e^- + Z^0 \rightarrow e^-, \quad \nu_e + Z^0 \rightarrow \nu_e, \quad \tau^+ + Z^0 \rightarrow \tau^+, \dots$$

$$Z^0 \rightarrow e^- + e^+, \quad Z^0 \rightarrow \tau^+ + \tau^-, \quad Z^0 \rightarrow \nu_\mu + \bar{\nu}_\mu, \dots$$

Any allowed reaction when **particles are interchanged by antiparticles** is also **allowed**

The weak interactions

Let us summarise what we have learned about the **weak interactions**

- ☑ **Flavour is not necessarily conserved** by the weak interactions: strangeness, charmness, and bottomness can vary in reactions mediated by the **W bosons** (but not by the Z boson)

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- ☑ From the point of view of the interactions with **leptons** and **charged quarks**, the Z boson behaves as if it was a **heavy photon**

The weak boson W

Taking into account these properties, some of the physically allowed reactions involving **quarks** and **W bosons** will be:

$$\begin{aligned} u + W^- &\rightarrow d, & u + W^- &\rightarrow s, & d + W^+ &\rightarrow u, & s + W^+ &\rightarrow u, \\ \bar{u} + W^+ &\rightarrow \bar{d}, & \bar{u} + W^+ &\rightarrow \bar{s}, & \bar{d} + W^- &\rightarrow \bar{u}, & \bar{s} + W^- &\rightarrow \bar{u}, \\ W^+ &\rightarrow u + \bar{d}, & W^+ &\rightarrow u + \bar{s}, & W^- &\rightarrow d + \bar{u}, & W^- &\rightarrow s + \bar{u}, \end{aligned}$$

- ☑ **Electric charge** is always conserved
- ☑ You can always **replace** a given quark by the corresponding quark of a **different generation**: for example a down antiquark by a strange antiquark
- ☑ If a given reaction is allowed, the corresponding reaction involving the **antiparticles** is also physically allowed

$$\bar{u} + W^+ \rightarrow \bar{s} \quad \Rightarrow \quad u + W^- \rightarrow s$$

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Taking into account these properties, some of the physically allowed reactions involving **leptons** and **W bosons** will be:

$$e^+ + W^- \rightarrow \bar{\nu}_e, \quad e^- + W^+ \rightarrow \nu_e, \quad \nu_e + W^+ \rightarrow e^-, \quad \bar{\nu}_e + W^+ \rightarrow e^+ \\ W^+ \rightarrow e^+ + \nu_e, \quad W^- \rightarrow e^- + \bar{\nu}_e, \quad e^+ + \nu_e \rightarrow W^+, \quad e^- + \bar{\nu}_e \rightarrow W^-$$

- ☑ **Electric charge** is always conserved
- ☑ Each interaction vertex involves a **charged** and a **neutral lepton** that belong to the **same lepton generation**
- ☑ You can always **replace** the two leptons of a given generation for the corresponding two leptons of **another generation**
- ☑ The **individual leptonic quantum numbers** are always conserved in weak reactions

exercise

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Draw the Feynman diagram for the following process

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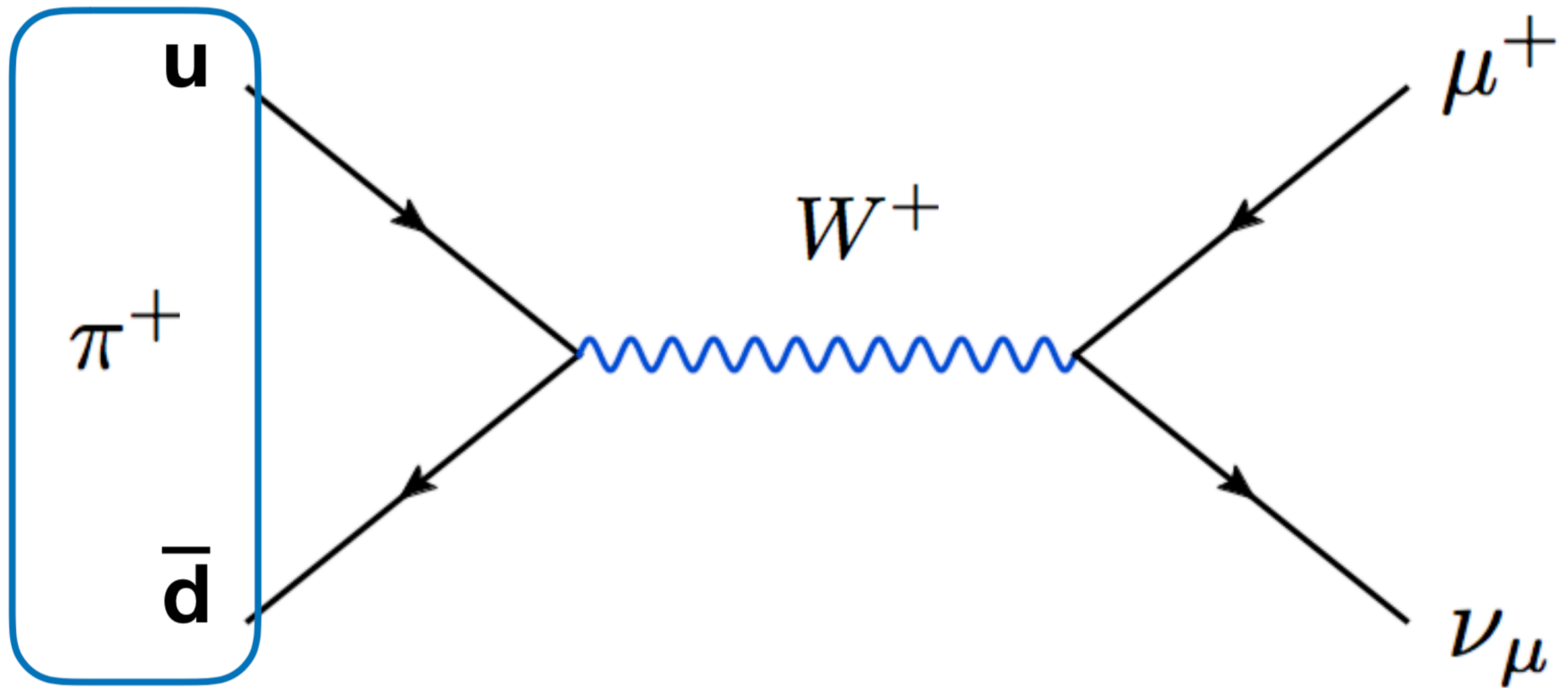
- We have a neutrino in the final state: the **weak interaction** must be involved
- Quarks and leptons only interact indirectly via either photons or W, Z bosons
- Since the electric charge is $Q=+-1$, then a positively charged **W boson** is involved
- We know what **vertices are allowed** involving quarks or leptons and a W boson

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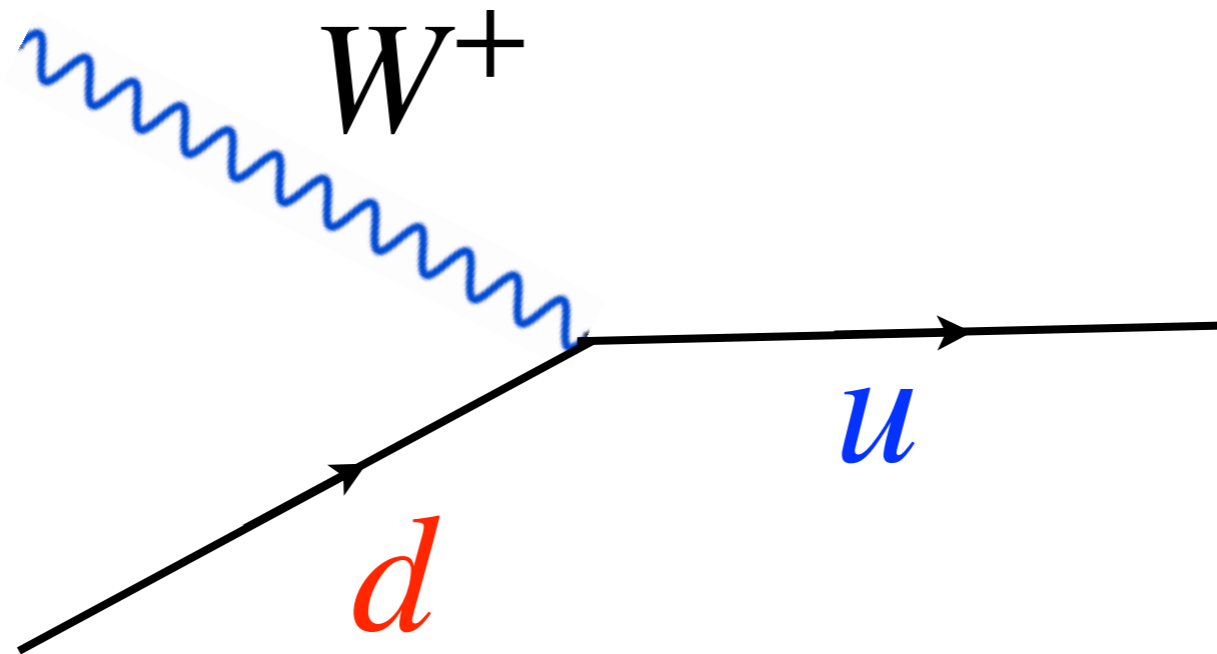


You can check that all relevant quantum numbers are **conserved**: L, B, Q, \dots

Heavy hadron decays

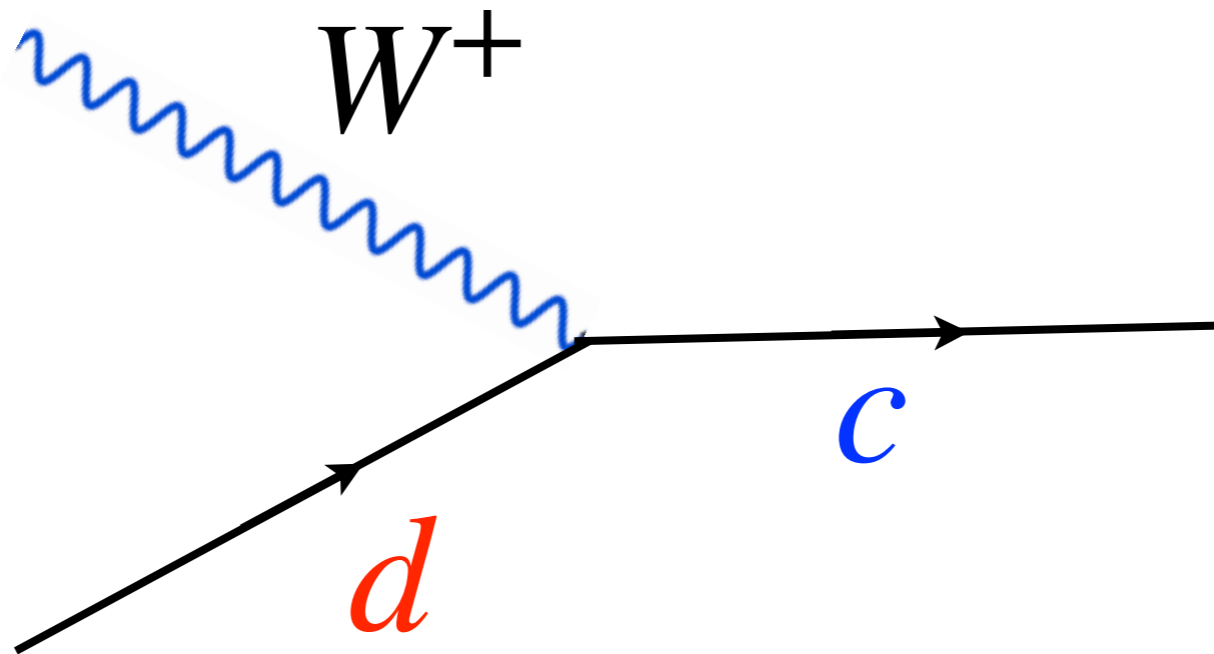
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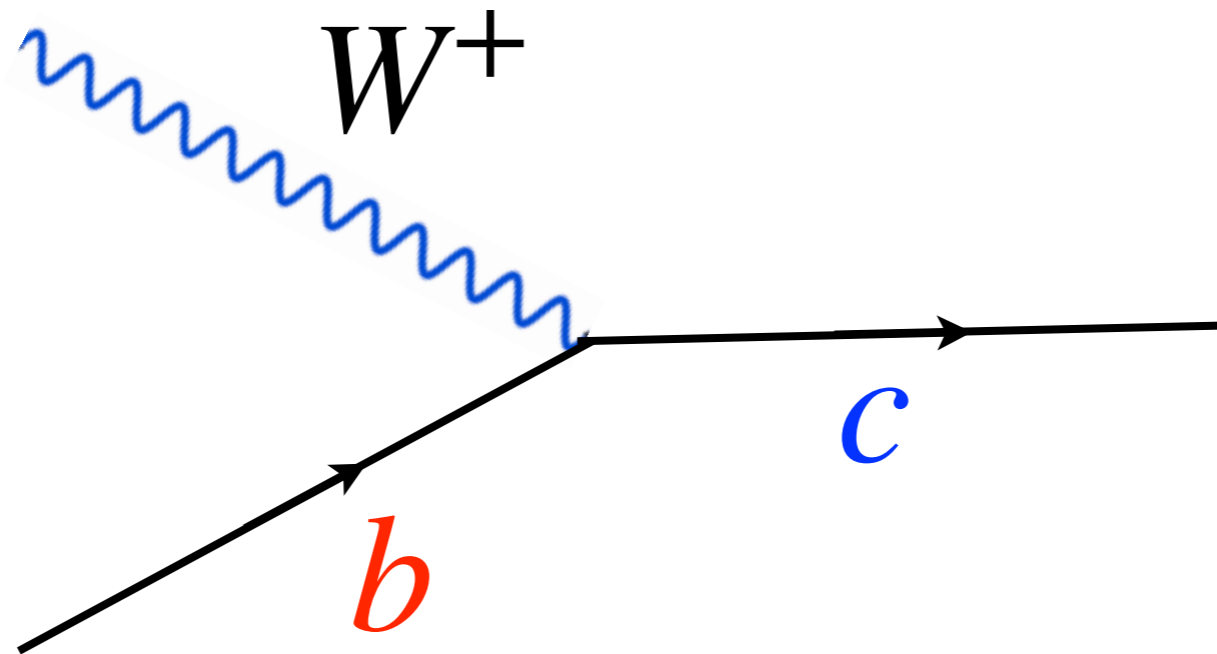
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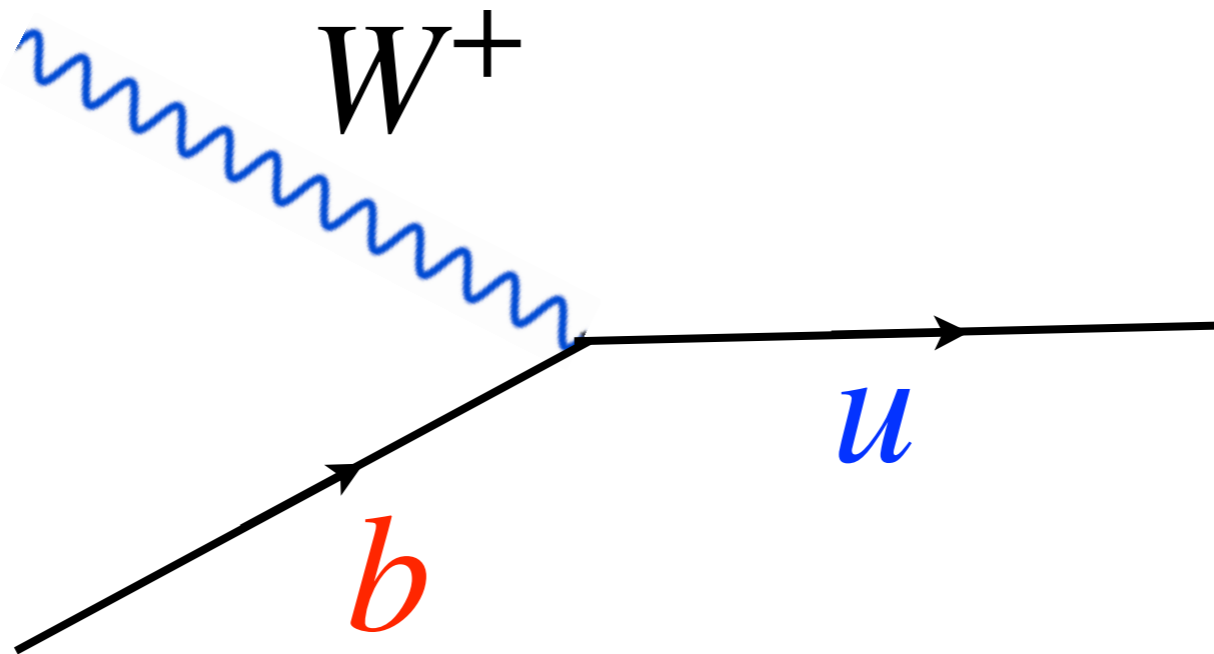
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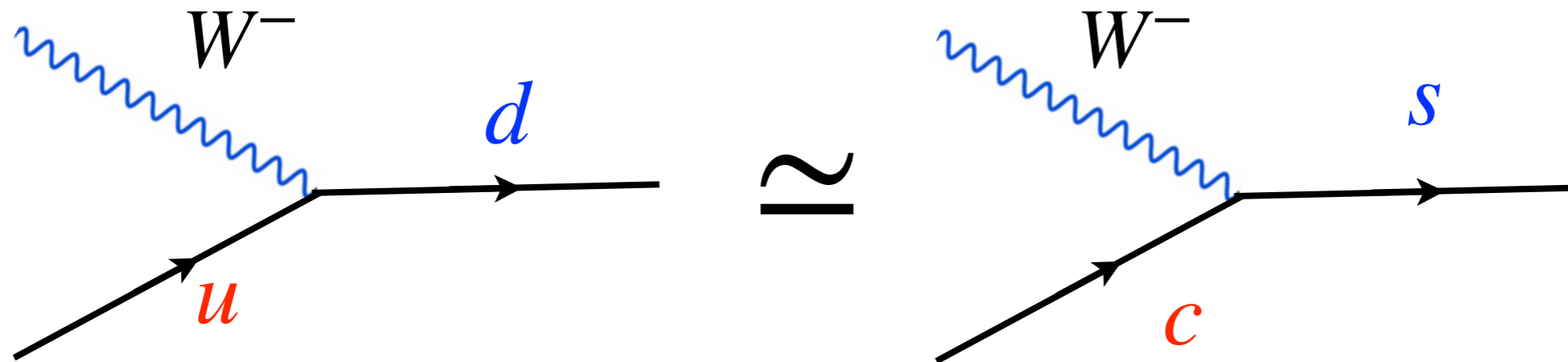


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The weak interactions mediates **transitions** between **quarks of different generations**

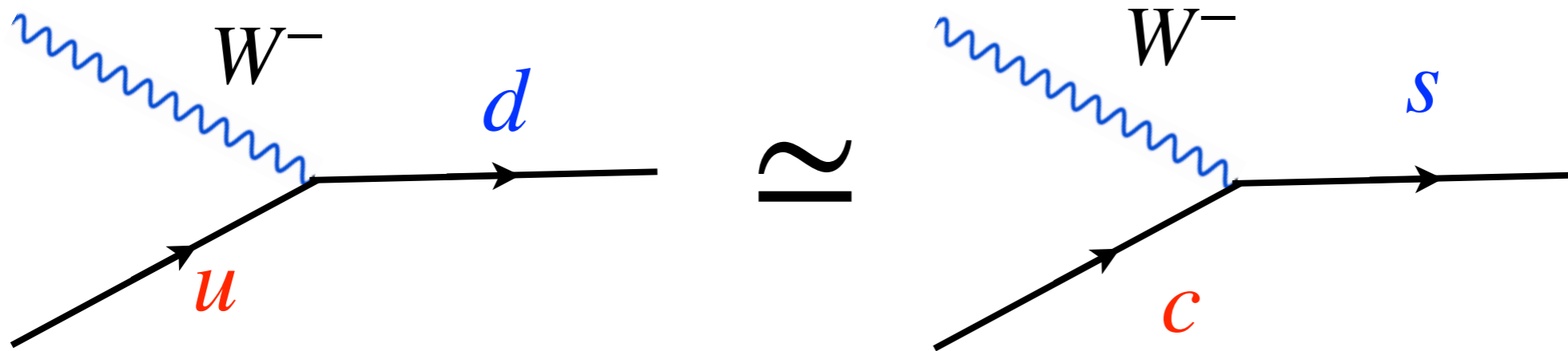
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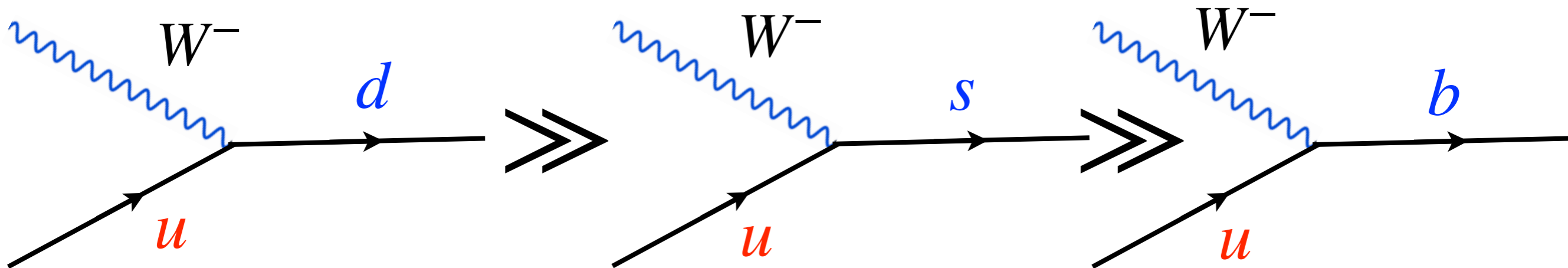


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Weak coupling between **gens 1 and 2** bigger than between **gens 1 and 3**

Drawing Feynman diagrams

- ☑ If the scattering reaction involves composite particles (hadrons) first of all determine their **quark decomposition** making sure all quantum numbers add up consistently
- ☑ Then put at the **left** of the diagram the **initial-state particles** and at the **right** of the diagram the **final-state** particles
- ☑ Attempt to connect the initial and final state particles among them. Note that some particles will not interact and will be just **spectators** in the reaction
- ☑ Make sure that all interaction vertices **conserve the corresponding quantum numbers**: for example, if gluons or photons are conserved, then **Q, B, S, C, b, \dots** should be conserved

Heavy hadron decays

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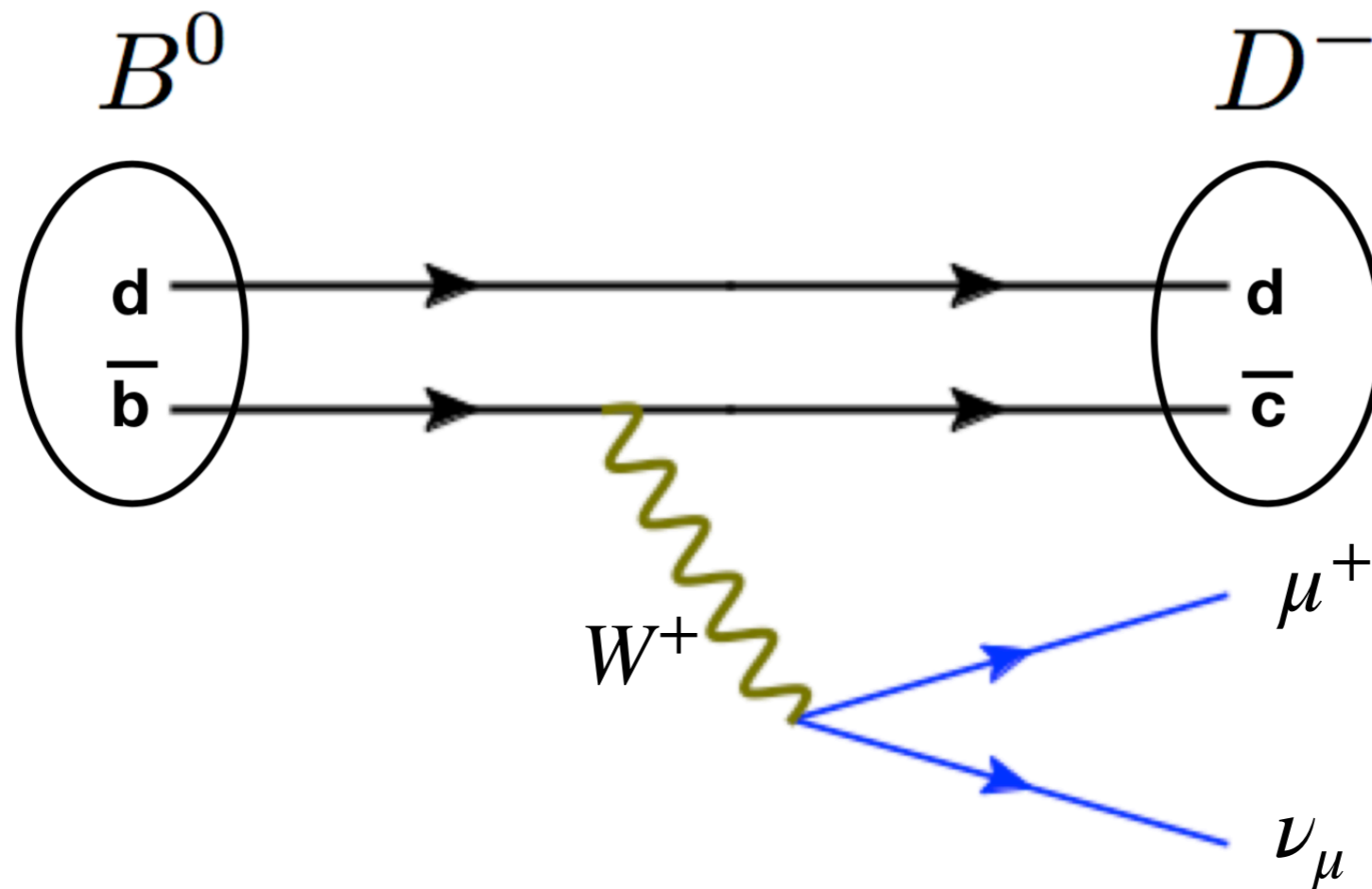
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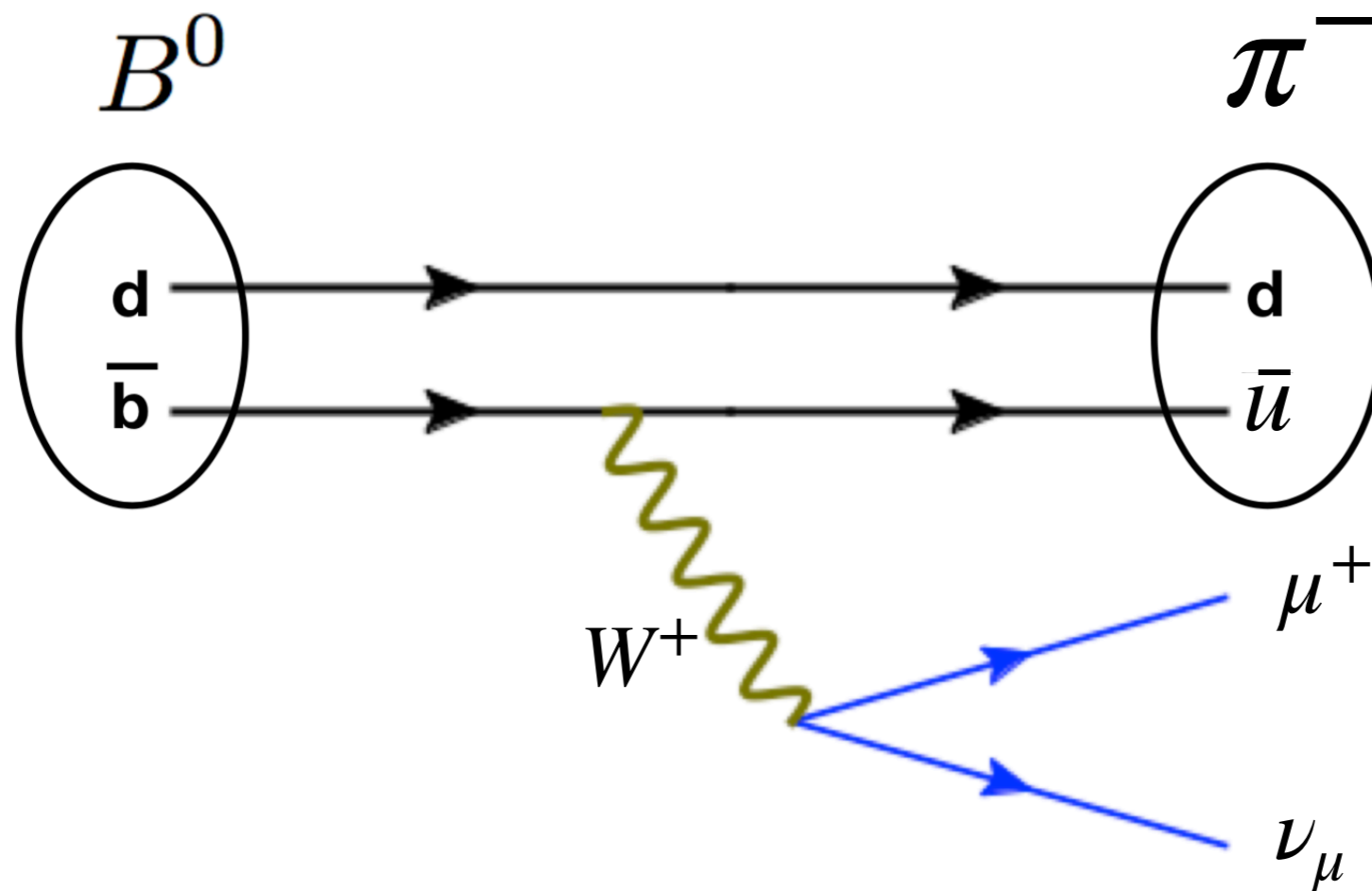
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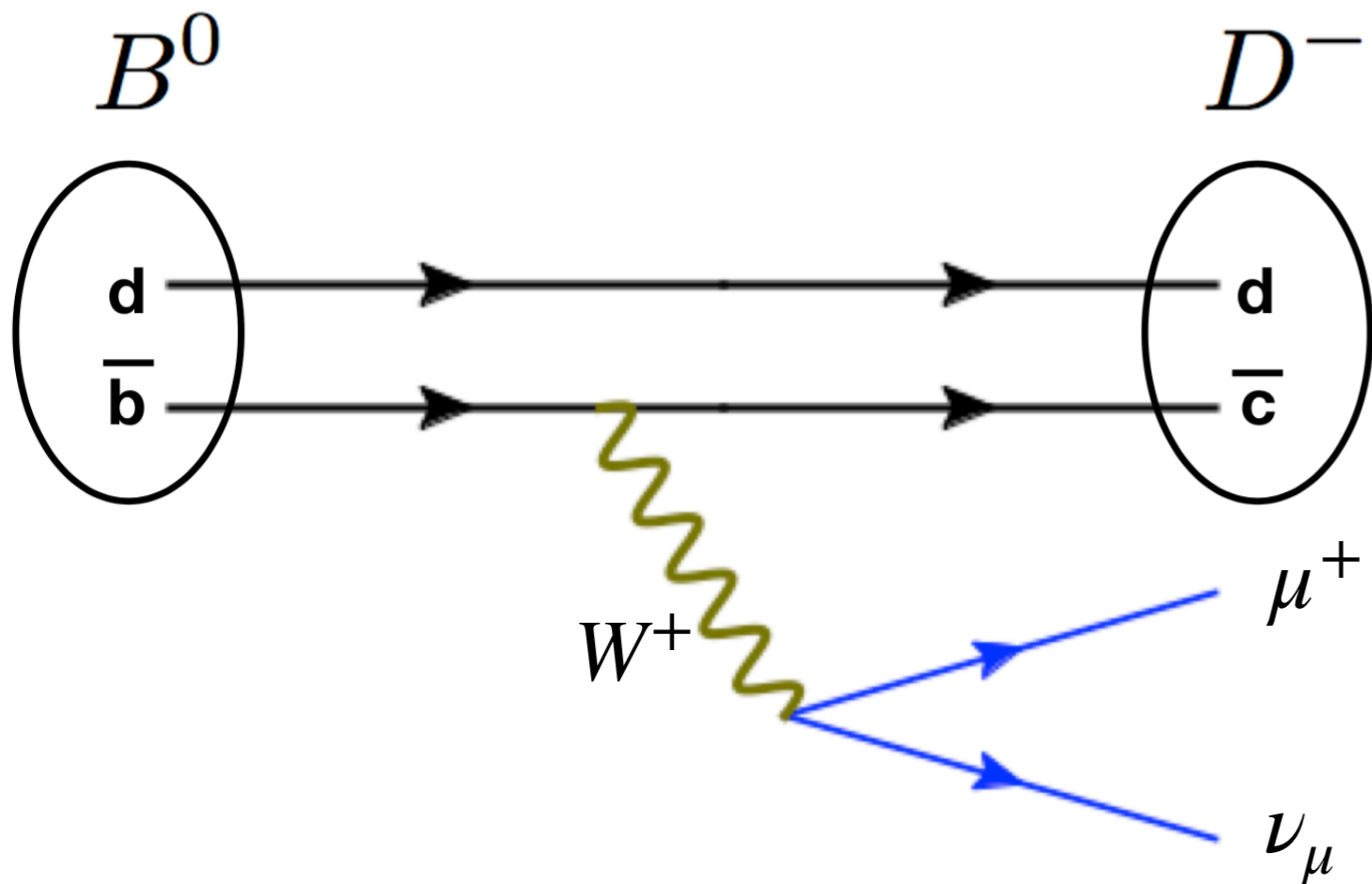
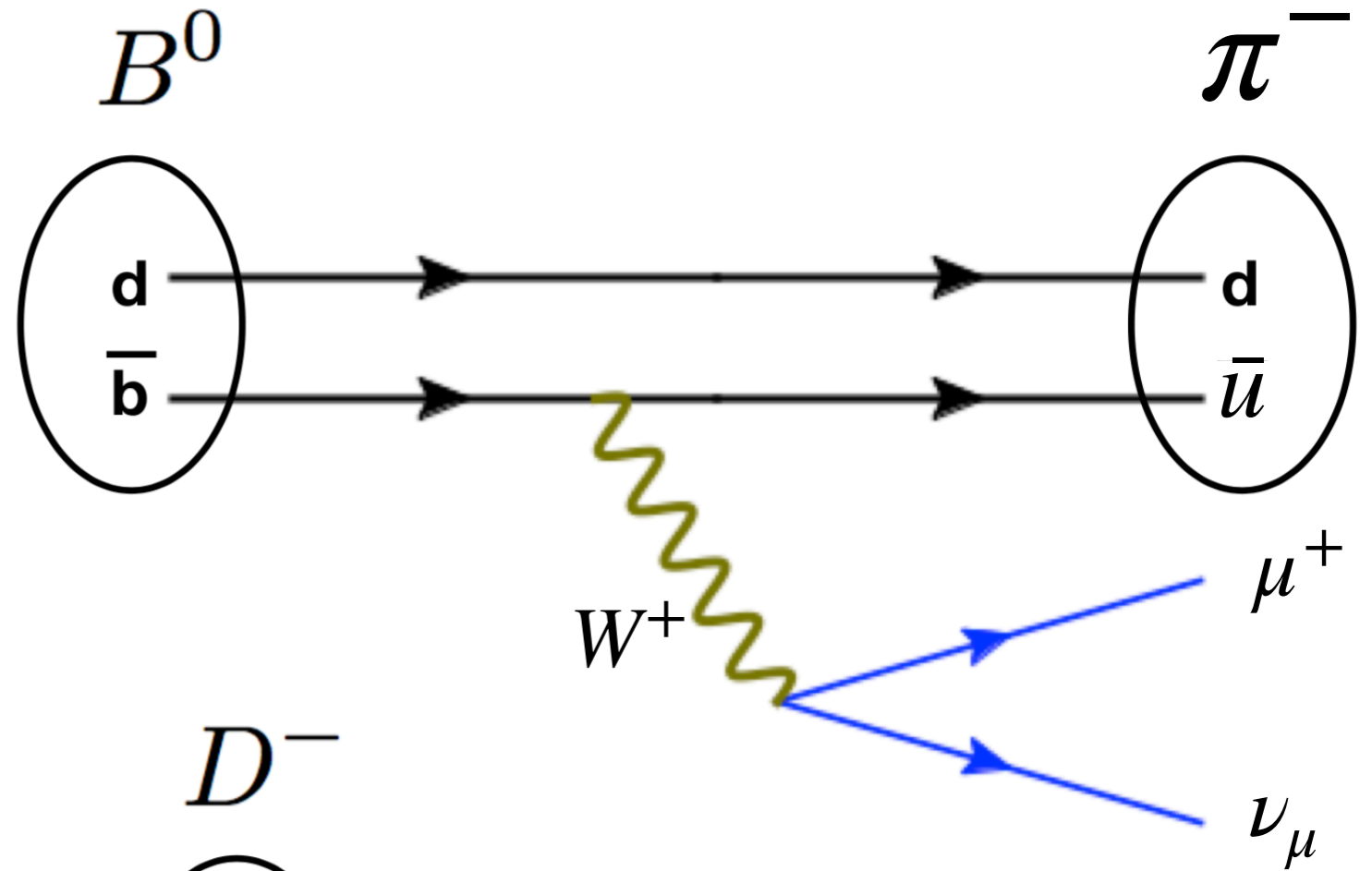
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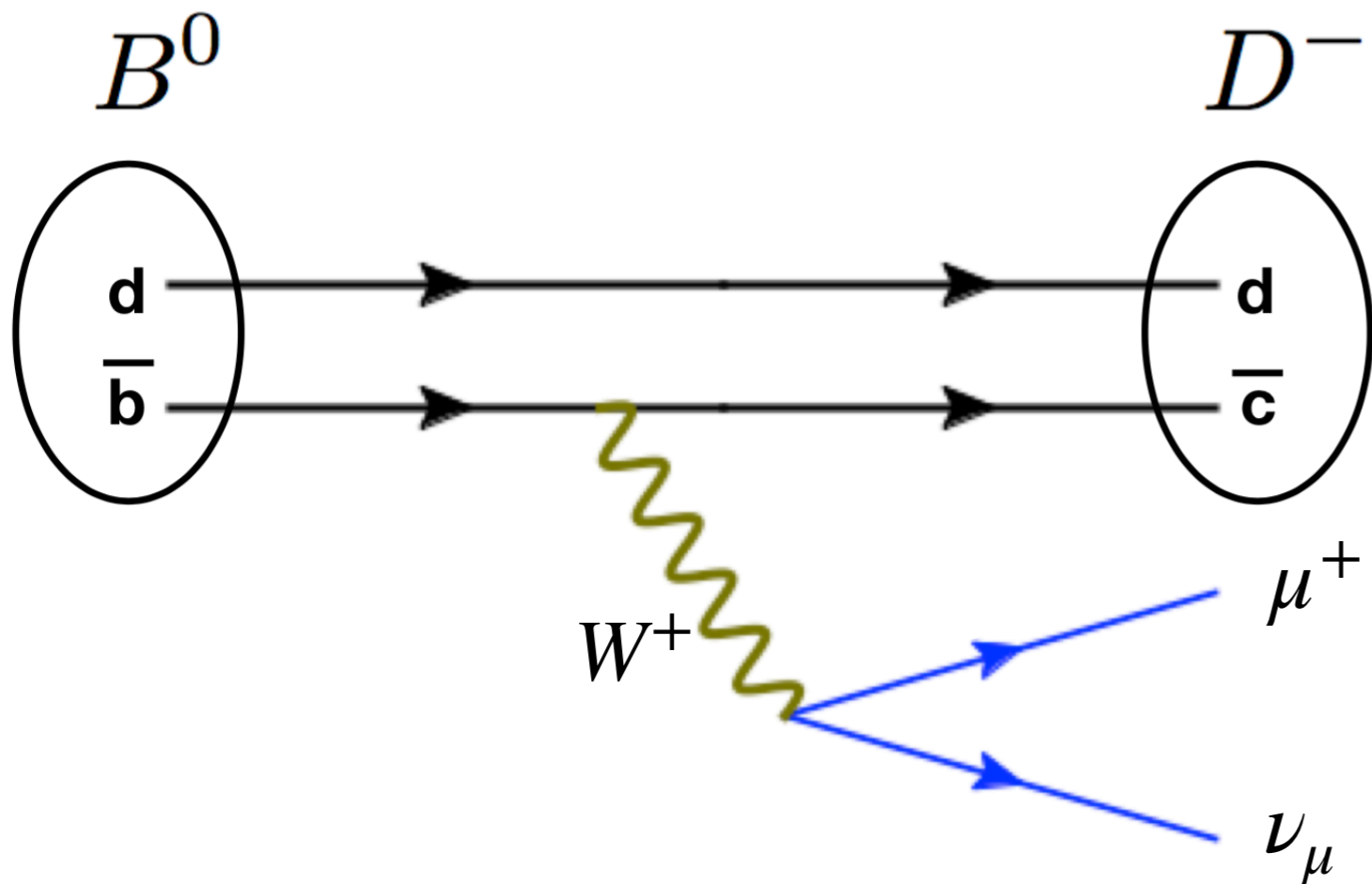
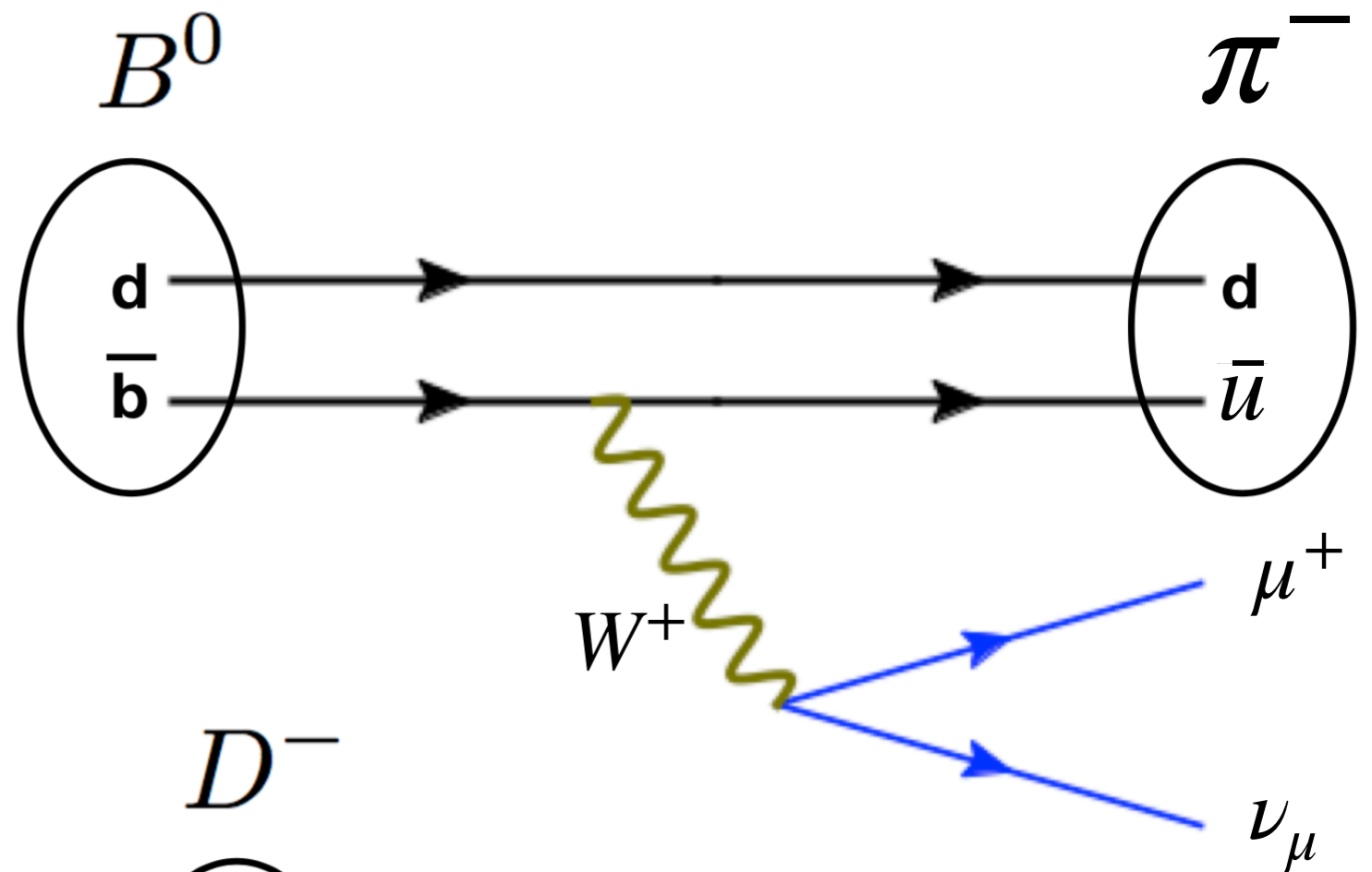
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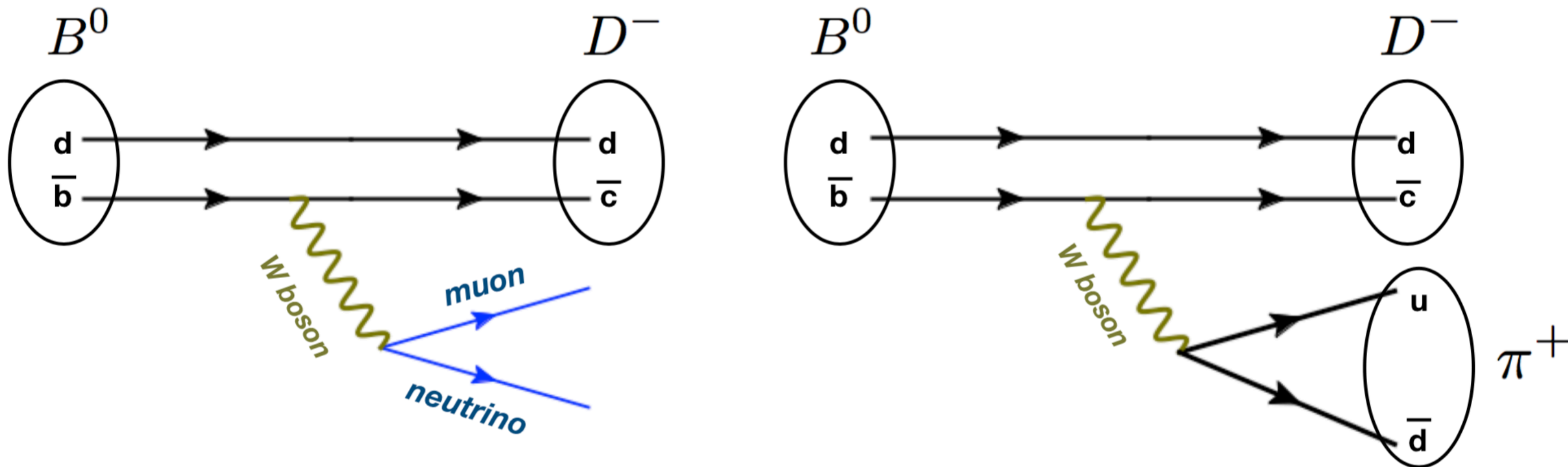
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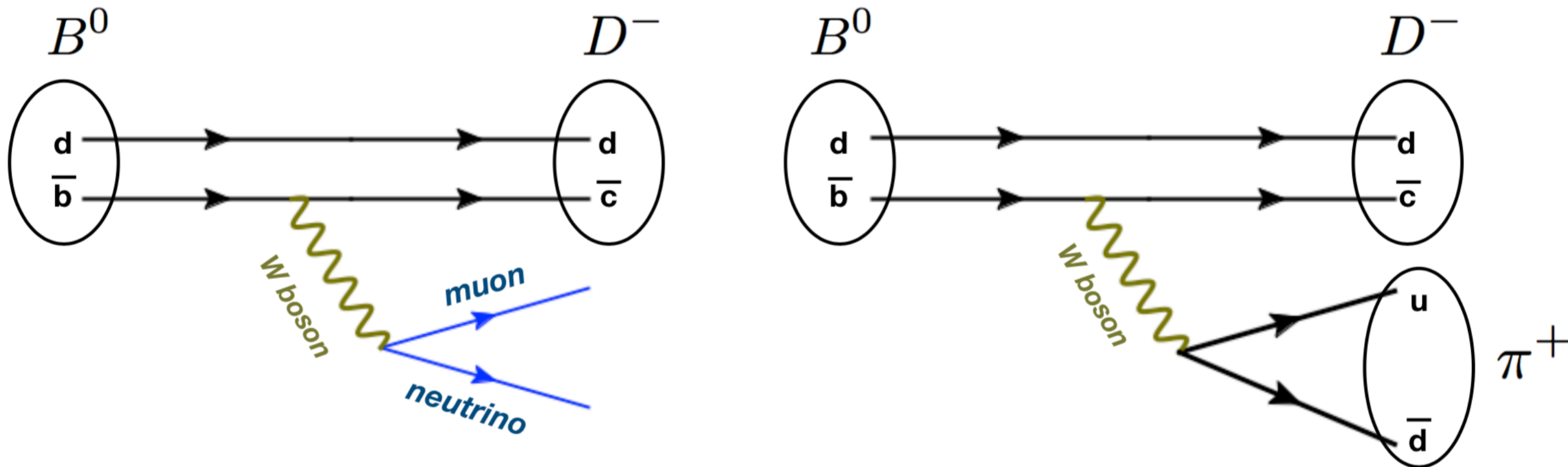
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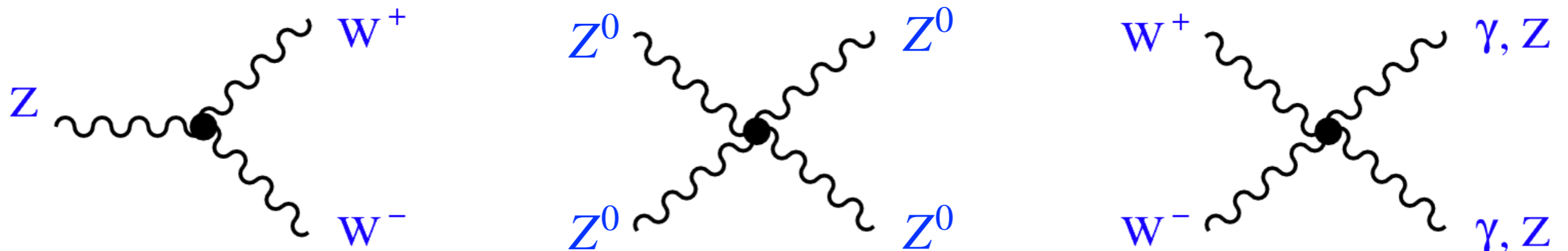
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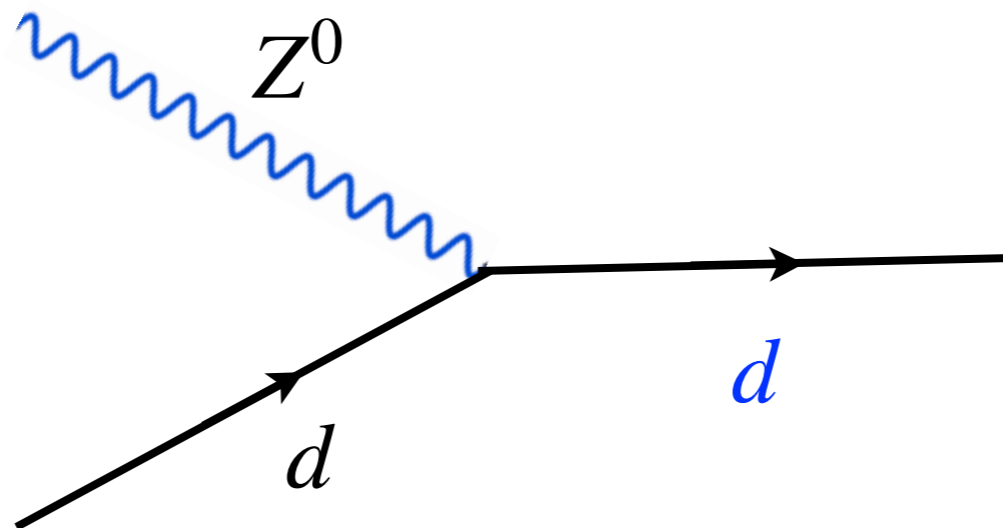


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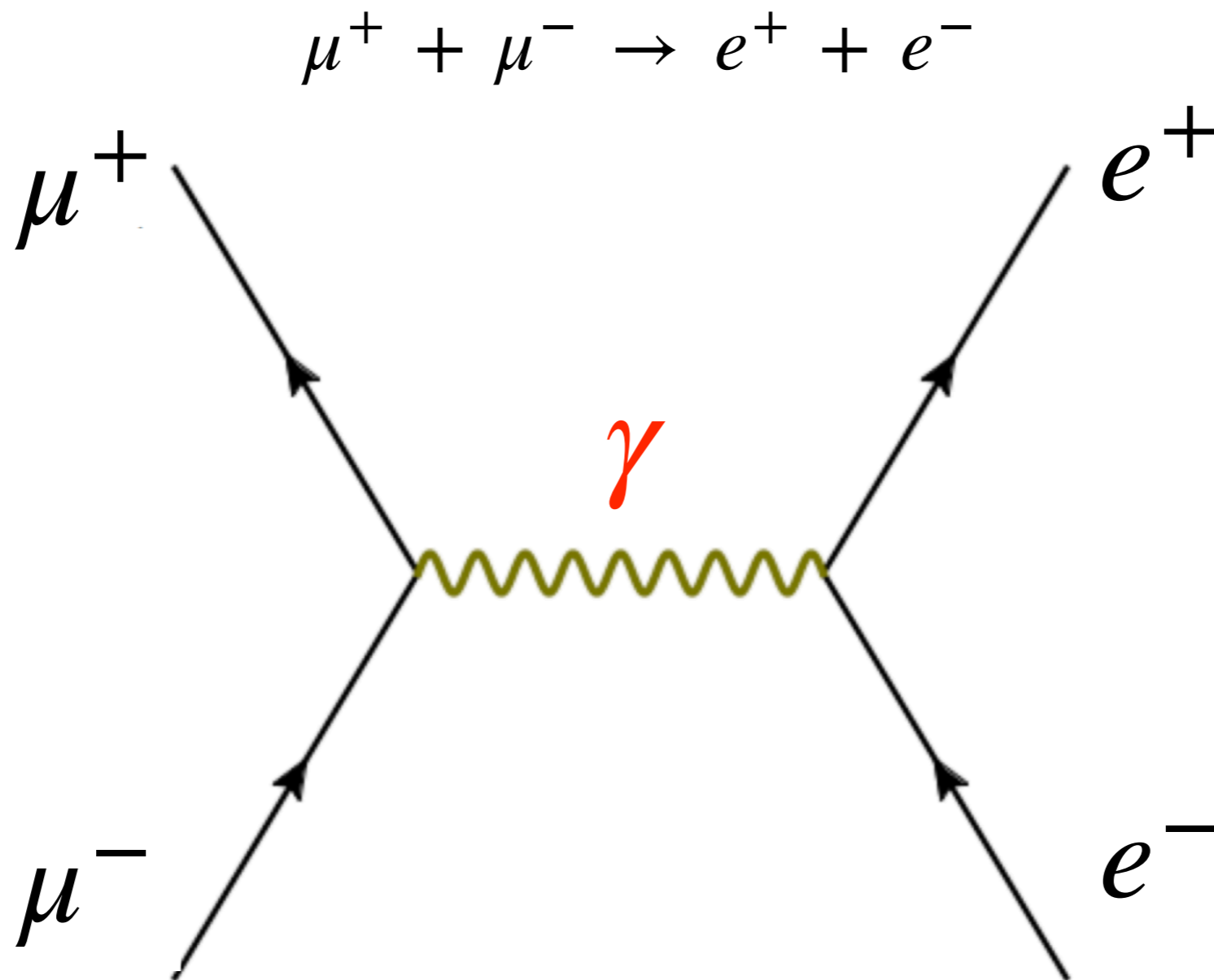
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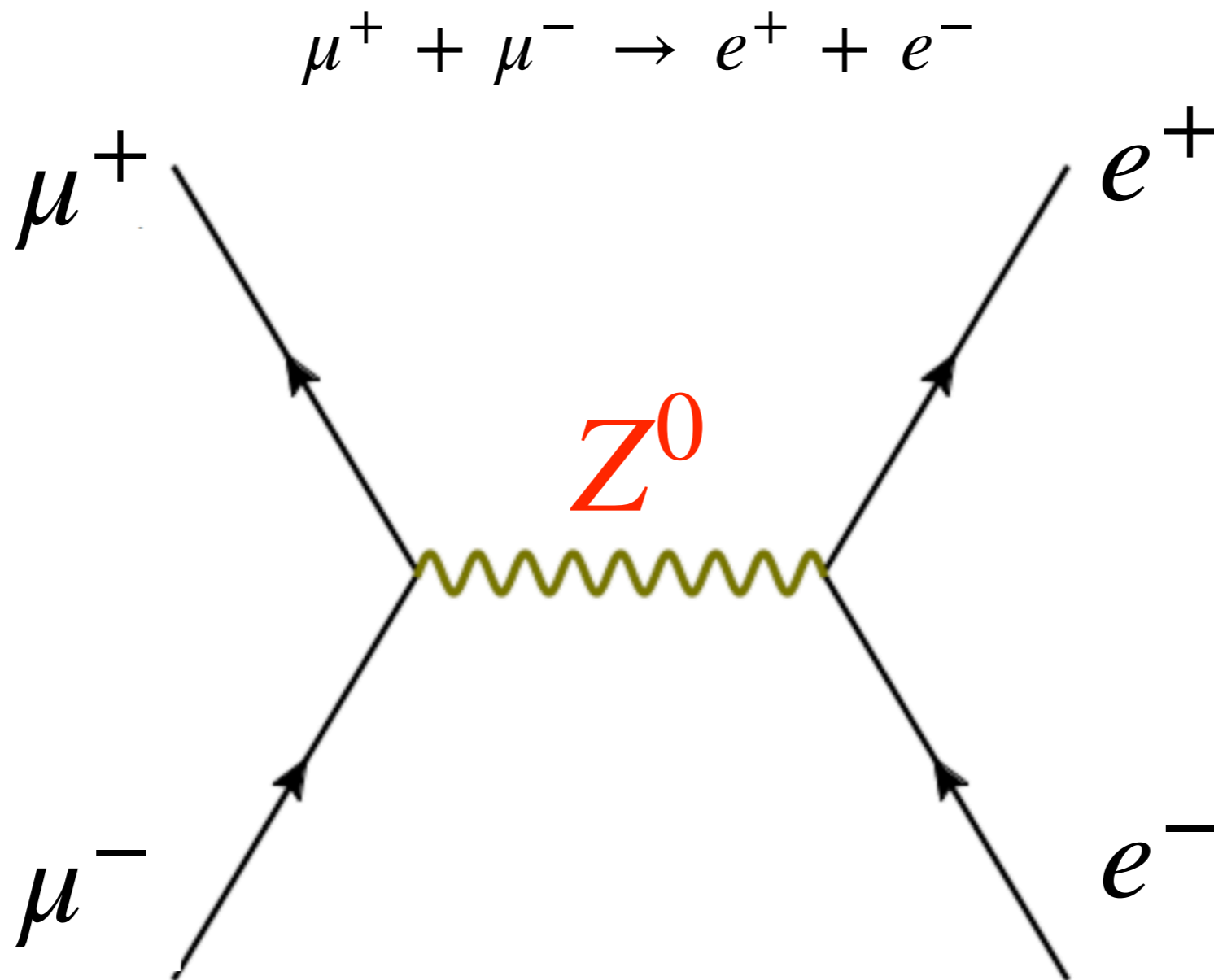
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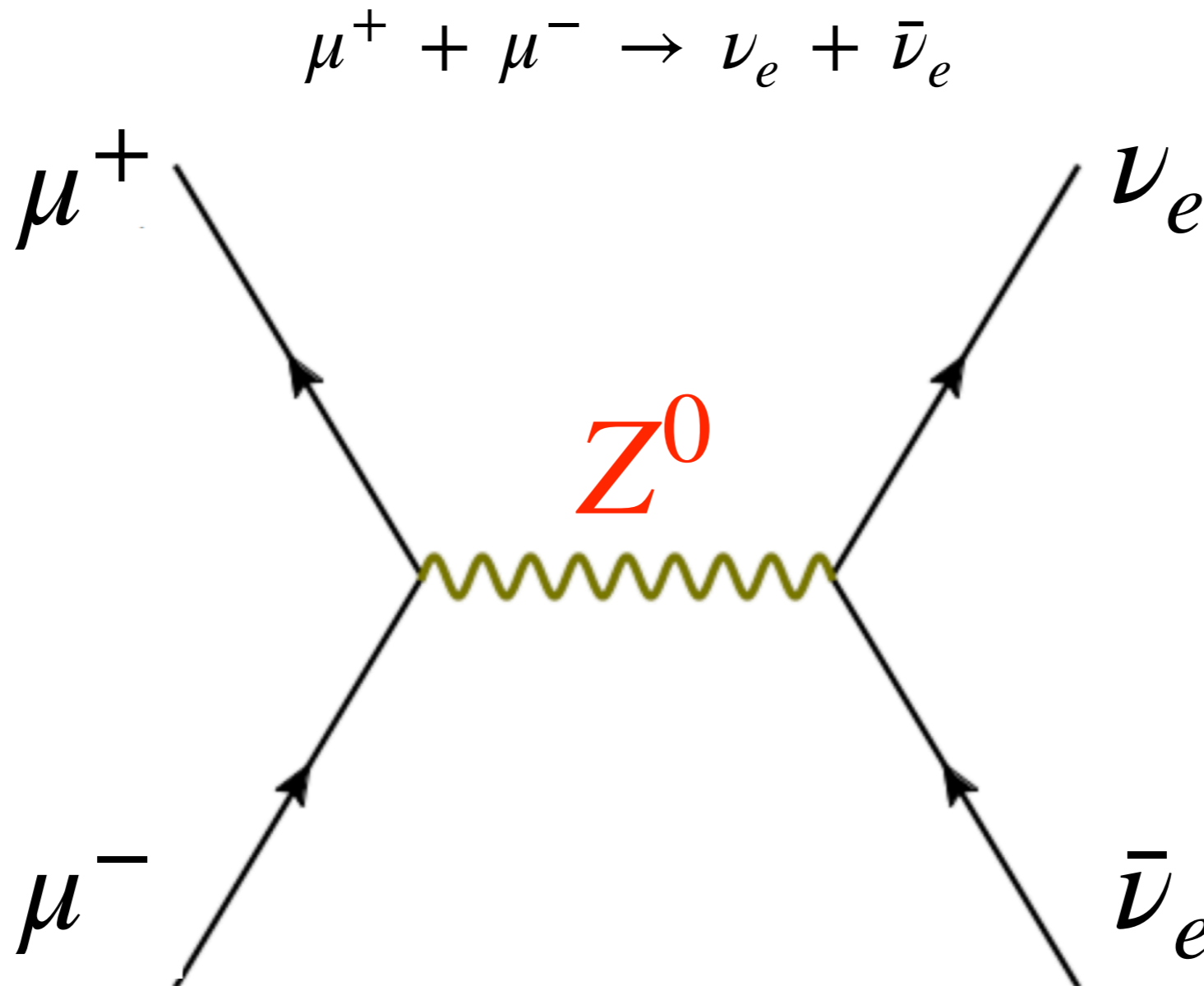
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The Z boson also mediates processes involving **neutrinos**



The weak boson Z

We can now summarise the **weak interaction vertices** involving the Z boson

with quarks

$$u + \bar{u} \rightarrow Z^0, \quad d + \bar{d} \rightarrow Z^0, \quad s + \bar{s} \rightarrow Z^0, \dots$$

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with leptons

$$e^+ + e^- \rightarrow Z^0, \quad \mu^+ + \mu^- \rightarrow Z^0, \quad \nu_e + \bar{\nu}_e \rightarrow Z^0, \dots$$

$$e^- + Z^0 \rightarrow e^-, \quad \nu_e + Z^0 \rightarrow \nu_e, \quad \tau^+ + Z^0 \rightarrow \tau^+, \dots$$

$$Z^0 \rightarrow e^- + e^+, \quad Z^0 \rightarrow \tau^+ + \tau^-, \quad Z^0 \rightarrow \nu_\mu + \bar{\nu}_\mu, \dots$$

Any allowed reaction when **particles are interchanged by antiparticles** is also **allowed**

The weak interactions

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- ☑ The strength of the weak interaction is **larger** between quarks of the **same generation** than between quarks of **different generation**
- ☑ From the point of view of the interactions with **leptons** and **charged quarks**, the Z boson behaves as if it was a **heavy photon**