

# DYqT: version 1.0

This is a note about the `DYqT` program, which computes the transverse-momentum ( $q_T$ ) spectrum of Drell–Yan lepton pairs with high invariant mass ( $M$ ) produced, via vector boson  $V$  ( $V = W^\pm, Z/\gamma^*$ ) decay, in  $pp$  or  $p\bar{p}$  collisions. The `DYqT` calculation combines the fixed-order result at high values of  $q_T$  ( $q_T \sim M$ ) up to  $\mathcal{O}(\alpha_S^2)$  with the resummation of the logarithmically enhanced contributions at small values of  $q_T$  ( $q_T \ll M$ ) up to next-to-next-to-leading logarithmic (NNLL) accuracy. The rapidity of the vector boson and the leptonic kinematical variables are integrated over the entire kinematical range. When referring to the program, please quote Refs. [1, 2].

## Overview

The program performs the resummation of the large logarithmic contributions that appear in the region where the vector boson transverse momentum  $q_T$  is much smaller than the invariant mass  $M$  ( $q_T \ll M$ ). The method to perform the resummation is presented in Refs. [3, 4]. The resummed result in the small- $q_T$  region ( $q_T \ll M$ ) is consistently matched to the fixed-order calculation that is valid at high  $q_T$  ( $q_T \sim M$ ). The fixed-order calculation implements the analytic results of Ref. [5]. We suggest the program to be used for transverse momenta  $q_T \lesssim M$ . When  $q_T \gtrsim M$  the use of the resummation formalism is no longer justified and one can use the standard fixed-order result.

The program can be used at NLL+LO and NNLL+NLO accuracy<sup>1</sup>. At NLL+LO accuracy the resummed part is evaluated at next-to-leading logarithmic (NLL) accuracy, and the fixed-order part is evaluated at the leading order (LO) (it is given by the  $\mathcal{O}(\alpha_S)$  terms with ‘ $V + 1$  parton’ in the final state). At NNLL+NLO accuracy the resummed part is evaluated at NNLL accuracy, and the fixed-order part is evaluated up to the next-to-leading order (NLO) (it includes all the terms with ‘ $V + 1$  parton’ and ‘ $V + 2$  partons’ up to  $\mathcal{O}(\alpha_S^2)$ ) at NLO ( $V + 1$  or 2 partons). At NNLL+NLO (NLL+LO) accuracy the DYqT calculation exactly recovers the total cross section at NNLO (NLO) upon integration over  $q_T$ .

## Input parameters

The mass and total width of the  $W$  and  $Z$  bosons are respectively  $m_W = 80.385$  GeV,  $\Gamma_W = 2.085$  GeV and  $m_Z = 91.1876$  GeV,  $\Gamma_Z = 2.4952$  GeV. As for the electroweak (EW) couplings, we use the so called  $G_\mu$  scheme, where the input parameters are  $G_F$ ,  $m_W$ ,  $m_Z$ . The Fermi constant is set to the value  $G_F = 1.16637 \times 10^{-5}$  GeV<sup>-2</sup>, and we use the following (unitarity constrained) values of the CKM matrix elements:  $V_{ud} = 0.97427$ ,  $V_{us} = 0.22536$ ,  $V_{ub} = 0.00355$ ,  $V_{cd} = 0.22522$ ,  $V_{cs} = 0.97343$ ,  $V_{cb} = 0.0414$ . All these values of EW parameters are taken from the PDG 2014 [9]. The EW couplings of the  $W$  and  $Z$  bosons to quarks and leptons are treated at the tree level, so that the above parameters are sufficient to fully specify the EW content of our calculation.

## Compilation

The DYqT program can be downloaded from  
<http://pcteserver.mi.infn.it/~ferrera/dyqt.html>

- To extract it type:

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<sup>1</sup>According to this notation [1, 2] for the resummed+matched expansion, the fixed-order labels, LO and NLO, refer to the perturbative accuracy in the large- $q_T$  region. Note, however, that the NNLL (NLL) part completely includes the perturbative contributions up to  $\mathcal{O}(\alpha_S^2)$  ( $\mathcal{O}(\alpha_S)$ ). Therefore, from the viewpoint of the perturbative accuracy in the small- $q_T$  region ( $q_T \ll M$ ), the NLL+LO and NNLL+NLO calculations should be denoted [6] as NLL+NLO and NNLL+NNLO, respectively.

```
tar -xzvf DYqT-v1.0.tgz
```

- To compile it simply use:  
make
- To run it type:  
./dyqt < infile

The program can be compiled with its own Parton Distribution Function (PDF) interface (set PDFROUTINES = NATIVE in the Makefile) or with the Les Houches Accord PDF interface (LHAPDF) (set PDFROUTINES = LHAPDF in the Makefile). In the latter case, the library libLHAPDF.a is needed (with the correct path set in the Makefile).

## The input file

This is a typical example of input file:

```
-1 ! Collider: pp (1), ppbar (-1)
3 ! Vector boson: photon (1),W+ and W- (2),W+ (21),W- (22),Z (3),Z/photon (5)
1 ! Narrow Width Approximation (NWA), only for W and Z prod.: false (0), true (1)
0 ! Remove Branching Ratio (only within the NWA): false (0), true (1)
91.1876d0 ! Lepton pair invariant mass [GeV] (dummy within the NWA)
2 ! Order of calculation: NLL+LO (1), NNLL+NLO (2)
test.dat ! Output file name
92 3 ! PDF number, loop for alpha_S (for native PDFs)
'MSTW2008nnlo68cl.LHgrid' 0 ! PDF name, member (for LHAPDF)
1.96d3 ! Centre--of--mass energy [GeV]
91.1876d0 91.1876d0 91.1876d0 ! Renormaliz., Factoriz., Resummation scales [GeV]
0.0d0 ! Non-perturbative smearing (g parameter)
0d0 20d0 2d0 ! qtmin qtmx qtbm
```

- **ic**: Integer variable setting the type of hadronic collisions:  $pp$  ( $ic=1$ ),  $p\bar{p}$  ( $ic=-1$ ).
- **prodflag**: Integer variable setting the type of vector boson produced:  
 $\gamma^*$  ( $prodflag=1$ ),  $W^+$  and  $W^-$  ( $prodflag=2$ ),  $W^+$  ( $prodflag=21$ ),  
 $W^-$  ( $prodflag=22$ ),  $Z$  ( $prodflag=3$ ),  $Z/\gamma^*$  ( $prodflag=5$ ),
- **fnwa**: Integer variable setting the use of the narrow width approximation (NWA). If  $fnwa=0$  the code computes the differential cross section  $M^2 d\sigma^V/dM^2/dq_T$  [pb/GeV], if  $fnwa=1$  the code computes the differential cross section  $d\sigma^V/dq_T$  [pb/GeV] within the NWA. The NWA is valid only for  $W$  and  $Z$  production ( $prodflag=2, 21, 22, 3$ ) and it consists in the substitution  $1/((M^2-m_V^2)^2+m_V^2\Gamma_V^2) \rightarrow \pi/(m_V\Gamma_V) \delta(M^2-m_V^2)$  in the corresponding cross section ( $m_V$  and  $\Gamma_V$  are respectively the vector boson mass and total width).

- **brflag**: Integer variable setting the  $W$  and  $Z$  leptonic branching ratios:  $\text{BR}(V \rightarrow l_1 l_2) = \Gamma_{V \rightarrow l_1 l_2} / \Gamma_V$ , where  $\Gamma_{V \rightarrow l_1 l_2}$  is the  $W$  or  $Z$  partial width due to the leptonic decays  $W \rightarrow l \bar{\nu}_l$  and  $Z \rightarrow l \bar{l}$ . If **brflag**=0  $\text{BR}(V \rightarrow l_1 l_2)$  is equal to the Standard Model value at tree level, if **brflag**=1 then  $\text{BR}(V \rightarrow l_1 l_2) = 1$ . This flag is valid only if **fnwa**=1.
- **amv**: Double precision variable that sets the mass of the lepton pair invariant mass  $M$  [GeV]. If **fnwa**=1 this is a dummy variable since  $M = m_V$ .
- **flag1**: Integer variable fixing the order of the calculation: NLL+LO (**flag1**=1) or NNLL+NLO (**flag1**=2).
- **runstring**: Character string which sets the output file name.
- **isetproton**, **nloop**: Integer variables for PDF choice (**isetproton**) and order of  $\alpha_S$  (**nloop**). These variables are valid with the native PDF interface. A list of available PDFs is given below. The number of loops to which  $\alpha_S$  should be evaluated has to be chosen accordingly.
- **name**, **mem**: Character string (**name**) which sets the PDF group and integer variable (**mem**) which sets the PDF member. These variables are valid with the LHAPDF interface.
- **sroot**: Double precision variable for centre-of-mass energy  $\sqrt{s}$  [GeV].
- **mur**, **muf**, **muq**: Double precision variables that set the renormalization, factorization and resummation scales [GeV]: they can be different from one another but they should always be set of the order of  $M$ .
- **g**: Double precision variable for non perturbative smearing. The smearing is applied as an additional factor  $\exp\{-gb^2\}$  in the resummed part, where  $b$  is the impact parameter variable that is Fourier conjugated to  $q_T$ . The choice **g**=0 means that no smearing is applied to the perturbative result.
- **qtmin**, **qtmax**, **qtbin**: Double precision variables setting minimum, maximum and step [GeV] in loop over the transverse momenta of the vector boson.

## Output

At the beginning, the code will perform a fit of the chosen PDFs at the given factorization scale and obtain the necessary Mellin moments. Then the program computes the cross section for the given values of  $q_T$ . The results are printed in the standard output and written in a file whose name is set in the input file. An example of output corresponding to a calculation at NNLL+NLO accuracy is shown below. The transverse momentum, the purely resummed result, asymptotic and fixed-order results are displayed in the first four columns, respectively. The last column displays the final matched result. The

results are given in pb/GeV. Running on a AMD Athlon 64-bit 2.6 GHz CPU, it takes about 50 minutes to obtain this output. The same calculation at NLL+LO accuracy takes instead about 5 minutes.

```
(
( PROGRAM DYqT (v1.0) Date: 28/03/2011 Time: 00:00:37
(
( Z Production
( BR(Z)= 0.0336386054
( alphas(mZ^2)= 0.117069888 alphas(1 GeV^2)= 0.387710006
(
( input file:
( ic= -1
( V= 3
( NWA= 1
( removeBR= 0
( q= 91.1876
( order= 2
( filename=test.dat
( PDF,loops= 92 3
( LHAPDF name,mem=MSTW2008nnlo68cl.LHgrid 0
( sqrt(s)= 1960.
( muR,muF,muQ= 91.1876 91.1876 91.1876
( NP g-par= 0.
( qtmin,qtmax,qtbin= 0. 20. 2.
(
(-----
(      qt          resum          asym          fixed          matched
(-----
(
1.0000000E+00  1.6687015E+01  8.2387225E+01  8.2536101E+01  1.6835892E+01
3.0000000E+00  2.3222481E+01  3.8746025E+01  3.8872153E+01  2.3348609E+01
5.0000000E+00  1.8255223E+01  2.1748443E+01  2.1840246E+01  1.8347025E+01
7.0000000E+00  1.3658863E+01  1.3999289E+01  1.4091829E+01  1.3751402E+01
9.0000000E+00  1.0315014E+01  9.7373869E+00  9.8436618E+00  1.0421289E+01
1.1000000E+01  7.9230646E+00  7.1133317E+00  7.2375642E+00  8.0472970E+00
1.3000000E+01  6.1840501E+00  5.3728592E+00  5.5169394E+00  6.3281303E+00
1.5000000E+01  4.8924724E+00  4.1560807E+00  4.3192093E+00  5.0556010E+00
1.7000000E+01  3.9134823E+00  3.2715204E+00  3.4520544E+00  4.0940164E+00
1.9000000E+01  3.1579074E+00  2.6088257E+00  2.8049882E+00  3.3540700E+00
```

## Native Parton Distribution Functions

A list of available parton densities for the native PDF interface is given below. A similar list is reported in the file `pdf_nat.f`. New PDFs can be easily added in that code by the user. Alternatively the user can set the use of the LHAPDF interface in the `Makefile`.

```
C
C Iset distribution
c
c 0 CTEQ4M NLO (MS)
c 1 -----
c 2 CTEQ4L LO
c 3 grv-98 NLO (MS)
c 4 MRST ft08a-98 NLO
c 5 MRST ft09a-98 NLO
c 6 MRST ft11a-98 NLO
c 7 MRST ft24a-98 NLO
c 8 MRST ft23a-98 NLO
c 9 MRST lo05a-98 LO
c 10 MRST lo09a-98 LO
c 11 MRST lo10a-98 LO
c 12 MRST lo01a-98 LO
c 13 MRST lo07a-98 LO
C 14 CTEQ5M Standard MSbar scheme
C 15 CTEQ5D Standard DIS scheme
C 16 CTEQ5L Leading Order
C 17 CTEQ5HJ Large-x gluon enhanced
C 18 CTEQ5HQ Heavy Quark
C 19 CTEQ5F3 Nf=3 FixedFlavorNumber
C 20 CTEQ5F4 Nf=4 FixedFlavorNumber
C 21 CTEQ5M1 Improved CTEQ5M
C 22 CTEQ5HQ1 Improved CTEQ5HQ
c 24 HMRS b
c 25 MRS S0
C 30 MRST 99 default (MS)

C MRST2000 set:

C 31 VNV000 new NLO (g-up)
C 32 VNV001 NNLO average
C 33 VNV002 NNLO AA
C 34 VNV003 NNLO BB
C 35 VNV004 NNLO AB
C 36 VNV005 NNLO BA
```

C 37 VNV006 LO

C MRST2001 NLO set

C 41 alf119 central gluon

C 42 alf117 lower a\_s

C 43 alf121 higher a\_s

C 44 j121 better fit to jet data

C MRST2001 NNLO set

C 45 vnvalf1155 'average' evolution

C 46 vnvalf1155a 'fast' evolution

C 47 vnvalf1155b 'slow' evolution

C 48 vnvalf1180j better fit to jet data

C MRST2002 new LO set

C 49 lo2002

C CTEQ6

C 50 cteq6l

C 51 cteq6m

C CTEQ6.6

C 55 cteq6.6m

C MRST2002 new updated set

c 61 mrst2002 NLO

c 62 mrst2002 NNLO

C MRST2004 set

c 71 mrst2004 NLO

c 72 mrst2004 NNLO

C MSTW2008 set

c 90 mstw2008 LO

c 91 mstw2008 NLO

c 92 mstw2008 NNLO

## References

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